## Homework 1. January 12, 2018.

- 1. Compute the simiplicial homology of the Klein bottle using the cell-structure described in class.
- 2. Compute the simplicial homology of the triangular parachute obtained from a two-simplex  $\Delta^2$  by identifying its three vertices to a single point.
- 3. The *n*-sphere  $S^n$  has a  $\Delta$ -complex structure using two *n*-simplices and identifying their boundaries via the identity map. Calculate the simplicial homology using this  $\Delta$ -complex structure. (If this is confusing, first try  $S^2$ .)

RECALLING FUNDAMENTAL GROUPS

- 4. Problem 5, p 38, Hatcher.
- 5. Problem 7, p 38, Hatcher.
- 6. Problem 12, p 39, Hatcher.