FUNCTIONAL CONNECTOME: PROBING THE COMPLEXITY OF THE WORKING BRAIN

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Ask not what the brain can do for the computer. Ask what the computer can do for the brain. Sebastian Seung

BrainyQuote[®]

Brains, Dynamics & Computation: A Workshop on Network Neuroscience

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A network is mainly a collection of nodes/vertices and edges/connections

Nothing exists in isolation—network are everywhere



Internet Networks

Figs are taken from the wiki and other different resources on internet





Brain Networks



Other examples:

6. Power-grid

7. Gene regulatory networks

Could you think of something else?



NETWORKS: ADJACENCY MATRIX

 $A_{ij} = w_{ij}$, if *i* and *j* have a link, $A_{ij} = 0$, otherwise, $w_{ij} = weight of link betw$ *i*and*j*

Binary undirected network

Binary directed network

0 1 0 0 0 0 1 0









CONNECTOME

The connectome is the complete description of the structural connectivity (the physical wiring) of an organism's nervous system.

Olaf Sporns (2010)

¹ Structural Connectome

Maps of anatomical connectivity based on isolate specific fiber tracts.

Methods: Parcellation of the brain volume or DTI



2 Functional Connectome

Maps of functional connectivity can be used to identify brain regions with spontaneous activity that is positively correlated (yellow or red) or negatively correlated (blue or green) with any other region.



Ref. Frontiers in Medicine, Mapping Symptoms to Brain Networks with the Human Connectome

Methods: Neuroimaging toolkits, mainly on the basis of time series obtained from the functional magnetic resonance imaging (fMRI), electroencephalogram (EEG), magnetoencephalogram (MEG), positron emission tomography (PET).



FUNCTIONAL CONNECTOME: TIME SERIES

* The time series recorded in electroencephalography (EEG) or magnetoencephalography (MRI) represents the activity of neurons

*When a neuron is activated or "fires," an electrical current cascades down the cell

*When numerous neurons fire simultaneously, sensors on the scalp can perceive this voltage shift—a mechanism that underpins(EEG). The range of this voltage signals is in the order of micro Volts. They are often referred to as "brain waves"

*Also changes in blood oxygenation level-dependent (BOLD) responses occurred is measured via functional Magnetic Resonance Imaging (fMRI)

*fMRI has good spatial resolution but lacks in the time resolution

***** EEG lacks in spatial resolution but has good time resolution

Refs. [1] Ogawa S., Lee T. M., Kay A. R., Tank D. W. (1990). Brain magnetic resonance imaging with contrast dependent on blood oxygenation. Proc. Natl. Acad. Sci. U.S.A. 87, 9868–9872. [2] Front. Neurosci., 05 June 2019 Sec. Neural Technology Volume 13 -2019 | https://doi.org/10.3389/fnins.2019.00585 [3] https://www.bitbrain.com/blog/ what-is-an-eeg





Functional Connectome: Time series

Brain wave patterns include: delta (0.5-4 hz), theta (4-8hz), alpha (8-12 hz), beta (12-35 hz), and gamma (32-100 hz) waves

THE FREQUENCY OF BRAIN WAVES





Why Functional Connectome?

*The network-based evaluation of functional brain networks can can reveal specific spatial changes in brain activity during neurological disorders like epilepsy.

Network analysis can be used as an adjunct to clinical diagnosis and as a screening tool for therapeutic trials.

*

Functional Connectome could also be useful in understanding the underlying mechanism for the decision making and the memory formation in brain

https://onlinelibrary.wiley.com/doi/10.1684/epd.2020.1203



FUNCTIONAL CONNECTOME (FC)



functional connectivity) or causal interactions (effective connectivity) among various neural units.

Ref. [1] Hlinka, J., et al (2011). Functional connectivity in resting-state fMRI: is linear correlation sufficient? NeuroImage, 54(3), 2218–25. doi:10.1016/j.neuroimage.2010.08.042; [2] Giovanni Chiarion et al. Connectivity Analysis in EEG Data: A Tutorial Review of the State of the Art and Emerging Trends

*Brain connectivity patterns from fMRI/EEG data are classified as statistical dependencies (coupling/



Connections in FC

(1)<u>Correlation</u>: (Most traditional method for testing functional connectivity, which is defined by measuring the the Pearson's correlation, Time domain, coupling, Undirected FC)

$$r_{xy} = rac{\sum_{t=1}^T (x_t - ar{x})(y_t - ar{y})}{\sqrt{\sum_{t=1}^T (x_t - ar{x})^2} \sqrt{\sum_{t=1}^T (y_t - ar{y})^2}}$$

(2) <u>Mutual information</u> (Quantifies the shared information (undirected) between two random variables, time/frequency domain, coupling, Undirected FC). For two discrete random variables X and Y, their mutual information takes the following form:

$$\mathrm{MI}\left(X,Y\right) = \sum_{x \in S_x} \sum_{y \in S_y} p\left(x,y\right) \ \log \ \left(\frac{p\left(x,y\right)}{p\left(x\right) p\left(y\right)}\right),$$

where S_x and S_y are possible values of X and Y, p(x, y) is the probability that the pair (X, Y) takes values x in S_x and y in S_y , and p(x) and p(y) are two marginal probabilities of X and Y.

Ref. [1] Hlinka, J., *et al* (2011). Functional connectivity in resting-state fMRI: is linear correlation sufficient? NeuroImage, 54(3), 2218–25. doi:10.1016/j.neuroimage.2010.08.042; [2] Giovanni Chiarion *et al*. Connectivity Analysis in EEG Data: A Tutorial Review of the State of the Art and Emerging Trends



Connections in FC

(3) <u>Phase Synchronization Index</u> : (Coupling, undirected FC) Given time-series *x*(*t*) and y(t) the Phase Locking Value (PLV) is defined as follows:

 $PLV = \left| E\left[e^{i(\Phi_x(t) - \Phi_y(t))} \right] \right|, \quad \text{Where,} \quad \Phi_x(t) = \arctan \frac{x(t)}{x(t)}, \quad x(t) \text{ is the Hilbert Transform of } x(t),$ similarly phase of y(t) can be defined.

(4) **Coherence** (Spectral representation of correlation in the frequency domain, It captures how strongly two signals co-vary at each frequency, coupling, could be directed or undirected)

(5) Granger causality: (causality, Directed FC)

(6) Transfer entropy: (causality, Directed FC)

Ref. [1] Hlinka, J., *et al* (2011). Functional connectivity in resting-state fMRI: is linear correlation sufficient? NeuroImage, 54(3), 2218–25. doi:10.1016/j.neuroimage.2010.08.042; [2] Giovanni Chiarion *et al.* Connectivity Analysis in EEG Data: A Tutorial Review of the State of the Art and Emerging Trends; https://pmc.ncbi.nlm.nih.gov/articles/PMC8928656/; https://pmc8928656/; https://pmc8928656/; https://



Methods...

Which method is best?

*Wei Zhang et al reported that Mutual Information Better Quantifies Brain Network Architecture in Children with Epilepsy, Comput Math Methods Med. 2018 Oct 22;2018:6142898. doi: 10.1155/2018/6142898

However, in most cases simple linear correlation is enough (Hlinka, J., et al)

*The connectivity measures are in general affected by the volume-conduction effect.

1 In practice, an appropriate threshold can give a correct/meaningful connectivity.

Ref: Front. Comput. Neurosci., 11 May 2017 Volume 11 - 2017 | https://doi.org/10.3389/fncom.2017.00036,; Hlinka, J., et al (2011). Functional connectivity in resting-state fMRI: is linear correlation sufficient? NeuroImage, 54(3), 2218–25. doi:10.1016/j.neuroimage.2010.08.042; Giovanni Chiarion et al. Connectivity Analysis in EEG Data: A Tutorial Review of the State of the Art and Emerging Trends

Fig. From https://reflect.ucl.ac.uk/ad-veturi/2021/06/08/modelling-brain-connectivity-using-graph-theory/

Thresholding methods:

(1) Absolute Thresholding: Simplest method bested considering the connections based on a threshold value (say ths).

$$A_{ij} = egin{cases} 1 & ext{if} \, w_{ij} \gtrsim ext{.ths} \ 0 & ext{otherwise} \end{cases}$$

(2) Largest connected component: Percolation-based Thresholding Method

13 Ref. Thresholding functional connectomes by means of mixture modeling, 2018 May 1;171:402-414. doi: 10.1016/j.neuroimage.2018.01.003

 θ_0

From: [Esfahlani, F.Z., Sayama, H. (2018). A Percolation-Based Thresholding Method with Applications in Functional Connectivity Analysis. In: Cornelius, S., Coronges, K., Gonçalves, B., Sinatra, R., Vespignani, A. (eds) Complex Networks IX. CompleNet 2018. Springer Proceedings in Complexity. Springer, Cham. https://doi.org/10.1007/978-3-319-73198-8 19].

Fig. A schematic illustration of the percolation-based thresholding method. The basic idea of the percolation-based thresholding method is to identify the minimum number of edges that maintain the giant component identified in the original weighted network [Esfahlani, F.Z., Sayama, H. (2018). A Percolation-Based Thresholding Method with Applications in Functional Connectivity Analysis. In: Cornelius, S., Coronges, K., Gonçalves, B., Sinatra, R., Vespignani, A. (eds) Complex Networks IX. CompleNet 2018. Springer Proceedings in Complexity. Springer, Cham. https://doi.org/

10.1007/978-3-319-73198-8_19]

Thresholding methods..

(3) Proportional thresholding (Density Thresholding): A top percentage of all partial correlation values in a subject-specific functional connectome is selected. The main aim of this approach is to keep the number of connections fixed for all the individuals in order to eliminate the impact of network density on the comparison of graph metrics across groups. This method for sparsifying functional connectomes is currently the most popular approach in the field, which might be due to its simplicity. Good for comparison.

(4) Minimum spanning tree (MST): backbone of the functional brain network:

(5) Permutation testing: A null distribution of connections estimated from time series with shuffled subject labels (confidence levels computed on the population level). The correlation matrix is then thresholded at a chosen significance level in the light of this null distribution, for each connection independently

Ref. Farahani F V, et al. Application of GraphTheoryforIdentifying ConnectivityPatternsinHumanBrain Networks: ASystematicReview. Front. Neurosci. 13:585. doi:10.3389/fnins.2019.00585

Fig. Different types of MST. Ref. "Functional brain networks in the schizophrenia spectrum and bipolar disorder with psychosis, npj <u>Schizophrenia</u> volume 6, Article number: 22 (2020)"

<image>

Fig. From https://reflect.ucl.ac.uk/adveturi/2021/06/08/modelling-brainconnectivity-using-graph-theory/

MEG + EEG ANALYSIS & VISUALIZATION

Open-source Python package for exploring, visualizing, and analyzing human neurophysiological data: MEG, EEG and more. <u>https://mne.tools/mne-connectivity/stable/</u> <u>index.html</u>

Network Analysis in Python

All help headers

Network construction Network measures List of measures

Network models

Network comparison

Network visualization

Datasets and demos

Network Based Statistic Toolb

Brain Connectivity Toolbox

Or

ownload the Toolbox

Search this site

The Brain Connectivity Toolbox (<u>brain-connectivity-toolbox.net</u>) is a MATLAB toolbox for complex-network analysis of structural and functional brain-connectivity data sets.

Getting started

Reference and citation

Complex network measures of brain connectivity: Uses and interpretations. Rubinov M, Sporns O (2010) NeuroImage 52:1059-69.

MATLAB

Complex Network Measures: Network's perspective to study brain Node Pegree

 k_i = Number of links node *i* has

Degree/ https://symbio6.nl/en/blog/

 $k_{i} = \sum_{j} A_{ij} \qquad \text{Number of links } L = \frac{\sum_{i} k_{i}}{2}$ $\text{Average degree } \langle k \rangle = \frac{k_{i}}{N} = \frac{2L}{N}$ $\langle k \rangle_{max} = N - 1$

Degree Distribution

https://symbio6.nl/en/blog/theory/definition/degree-distribution

Complex Network Measures: Network's perspective to study brain Finding Important Nodes: Centrality

Fig. Basic concept of network centralities. (A) Hubs (connector or provincial) refer to nodes with a high nodal centrality, which can be identified using different the gray colored node, although their degrees are equal. The participation coefficient of a node represents the distribution of its connections among separate similar to the degree centrality, but they are generally distinct. Note that the size of the nodes in all cases is proportional to the node degree, and the red nodes

Complex Network Measures: Network's perspective to study brain Clustering

The clustering coefficient is a measure of the degree to which nodes in a network tend to cluster together.

Global Clustering:

 $3n_{\Delta}$

The clustering coefficient of a graph is closely related to the transitivity of a graph, as both measure the relative frequency of triangles.

Modularity

Modular Networks have denser connections in modules & sparser connections between modules. **Modularity** (Q) is then defined as the fraction of edges that fall within groups, minus the expected number of edges within groups for a random graph with the same node degree distribution as the given network, given as follows for a partition p: $Q(p) = \sum_{k=1}^{N_m} \Big \lceil rac{w_k}{2} \Big
brace$

where N_m is the number of modules, W is the total weight of the network, w_i is the sum of the connectional weights between all nodes in module *i* and W_i is the sum of the all regional functional connection strengths in module *i*. Q_{max} is the largest network modularity resulting from a specific partition p [https://pmc.ncbi.nlm.nih.gov/articles/PMC6987957/]

$n_{\Lambda} =$ Number of existing triangles

$N_{\Delta} = \mathbf{N}_{umber of possible triangles}$

C_{Λ} is often called ratio of transitive triplets

$$\left[\frac{w_i}{W} - \left(\frac{W_i}{2W}
ight)^2
ight]$$

Modularity and community structure in networks M. E. J. Newman

Complex Network Measures: Network's perspective to study brain Path-length & Efficiency

The distance between two nodes (path-length, L_{ii}) is the number of the edges along the shortest path connecting them.

Example:
$$L_{12} = 1, L_{13} = 2, L_{24} = 1$$

For $L_{ij} = 1, A_{ij} = 1$
For $L_{ij} = 2, A_{ik} * A_{kj} = 1$

For $L_{ij} = n, A_{ik} * A_{kl} * ... * A_{lj} = 1$
No. Of paths of length 2 i.e. $L_{ij}^2 = \sum_{k=1}^{N} N_{kk}$

If two nodes are disconnected the pathlength between them will be infinite **Diameter: Largest path length between any pair of nodes in a network** The efficiency of a network is the summation of inverse of the all the shortest pathlengths

$$E = \sum_{ij} \frac{1}{N(N-1)} *$$

$$A_{ik} * A_{kj} = B_{ij}$$
, where, $B = A^2$

j

A

Rich-club and core:

Core act as a crucial hub that integrates the more loosely connected peripheral nodes, ensuring efficient network functionality

Bullmore, E., & Sporns, O. (2012). The economy of brain network organization. Nature reviews. Neuroscience, 13(5), 336–49

NULL MODELS FOR STATISTICAL VALIDATIONS

Regular Networks Lattice

Random Networks

Erdős Pál Alfréd Rényi

A mathematician is a device for turning coffee into theorems Alfred Renyi

Each pair of nodes is connected with probability p

Globally connected network

Fig. A random network, from wiki

NULL MODELS FOR STATISTICAL VALIDATIONS

Modular networks: Stochastic Block Methods (SBMs)

Ref. A review of stochastic block models and extensions for graph clustering <u>Applied Network Science</u> volume 4, 122 (2019)

Multilayer Networks

(a) A multilayer network consists of different networks encoded by layers, each one represented by a (possibly directed and weighted) adjacency matrix. (b) The rank-4 multilayer adjacency tensor, representing intra- and inter-layer connectivity, is generally flattened by matricization to a rank-2 tensor, generally known as supra-adjacency matrix, without loss of information. Manlio De Domenico GigaScience, Volume 6, Issue 5, May 2017, gix004, https://doi.org/10.1093/gigascience/gix004

understanding

Brain Networks are highly clustered

Fig. Modularity in the resting state networks compared to the corresponding random networks for the EEG data with 101 ROIs

Brain Networks: Has hubs and are Homophilic

Fig. Assortativity in the resting state networks compared to the corresponding random networks for the resting state EEG data with 101 ROIs.

Fig. Average betweenness centrality in the resting state networks compared to the corresponding random networks for the resting state EEG data with 101 ROIs.

A. Singh*, Lakshana Balaji & Mitanshu Sukhvani

It's a small-world

SEGREGATION:

Clustering, Motifs, Modularity

+

The spatial organization of brain networks. (a) Localized network, in which nodes link based on spatial proximity; (b) Small-world network, a coexistence of a majority local and a small fraction of long range connections; (c) Random connectivity. These structural patterns represent a trade-off between cost and efficiency: localized is cost-effective but inefficient in terms of information dissemination, random exhibits maximum efficiency, but at a high cost, small-world optimally balances the two.

*Replicating the structural behavior the functional connectome has also been found to show the smallworld phenomenon [https://www.sciencedirect.com/science/article/pii/S1389945718308967#sec3]

INTEGRATION:

Brain Diseases and Network topology

Disrupted Brain Functional Organization in Epilepsy Revealed by Graph Theory Analysis

Jie Song, Veena A Nair, Wolfgang Gaggl, Vivek Prabhakaran

(1) Global efficiency is significantly increased in the epilepsy group across a range of different connection densities

Overall global efficiency is higher for the Epileptic patients. Whereas, the medial temporal lobe and PCG show decreased global efficiency, and PCC, angular gyrus, thalamus, and cerebellar vermis show increased global efficiency.

(2) Increased number of functional connections in the epilepsy patients.

Default Mode Network (DMN) and Brain related diseases

DMN is a large-scale distributed brain network which plays a critical role in cognition, including episodic memory formation and monitoring internal thoughts

DMN impairments are prominent in psychiatric disorders.

DMN is also found particularly sensitive to Alzheimer's disease pathology and the ensuing loss of episodic memory and related cognitive functions.

Neuroimage. 2022 Jan 21;250:118927. doi: 10.1016/j.neuroimage.2022.118927

cortex, AMPFC antero-median prefrontal cortex, VMPFC ventro-median prefrontal cortex, TP temporal pole, BF basal forebrain, T thalamus, PH parahippocampal region, CbH cerebellar hemisphere, CbT cerebellar tonsil, Amy amygdala, MidB midbrain. *n* = 20 participants <u>Communications Biology</u> volume 2, 370 (2019)

0.115

0.11

0.105

0.175

0.17

0.165

0.385

0.38

0.37

0.365

DMN-Othe

> 0.38 Id 0.375

Network based understanding of progression of the Alzheimer's Disease (AD)

Individuals with AD exhibited degeneration of specific brain hubs, reduced clustering coefficients and path lengths very close to the values of random networks (Supekar et al., 2008; Sanz-Arigita et al., 2010; Dai et al., 2015; delEtoile and Adeli, 2017),

The cognitive impairment in the AD was associated with a weakness in modular interconnectivity and hubs destruction (Brier et al., 2014) and significant alterations within the default network (Toussaint et al., 2014; Zhong et al., 2014).

These findings were in parallel with a global decrease in long-distance functional connections especially between frontal and caudal brain regions (Sanz-Arigita et al., 2010).

Ref. Farahani F V, et al. Application of GraphTheoryforIdentifying ConnectivityPatternsinHumanBrain Networks:ASystematicReview. Front.Neurosci.13:585. doi:10.3389/fnins.2019.00585

AGING AND THE BRAIN NETWORK

The lifespan trajectories of functional network efficiency and modularity. Absolute network properties based on the correlation thresholding method, and relative network properties are based on density thresholding networks [Dev Cogn Neurosci. 2013 Nov 28;7:76–93. doi: <u>10.1016/j.dcn.2013.11.004</u>]

Multilayer Brain Networks: Frequency-based decomposition

Manlio De Domenico GigaScience, Volume 6, Issue 5, May 2017, gix004, <u>https://doi.org/10.1093/gigascience/gix004</u>

Multilayer Brain Networks: Time based decomposition

Manlio De Domenico GigaScience, Volume 6, Issue 5, May 2017, gix004, https://doi.org/10.1093/ gigascience/gix004

Multilayer functional brain networks are more informative than the monolayer networks

*De Domenico et al. also calculated centrality measures (i.e., measures of the importance of network components; Newman, 2010) on the frequency-based multiplex networks to demonstrate the existence of hubs that had not been classified previously as important brain regions for functional integration.

Hubs of the control group were located in anterior cingulate, superior frontal, insula, and superior temporal cortices; however, hubs for schizophrenic patients were distributed over frontal, parietal, and occipital cortices.

The accuracy of the classification using the network features among the healthy and schizophrenic patients had better accuracy in multilayer frame than the monolayer.

*These results revealed that frequency-based multiplex networks include relevant information about the functional organization of brain networks that is not captured by using a classical monolayer approach.

Is the Functional Connectome a Reflection of Anatomical **Brain Connectivity?**

- Functional correlations can be found between left motor cortex and right cerebellum (Buckner et al., The organization of the human cerebellum estimated by intrinsic functional connectivity 2011), two structures that are multiple steps away from one another in anatomical terms (figure).
- * The eccentric representations of primary visual cortex in left and right hemispheres correlate, without the presence of direct anatomical connections (Vincent et al., 2007) 10.1038/nature05758.).

No one-to-one mapping between Structural and functional connectome

Understanding brain networks and brain organization, Luiz Pessoa

From: Brain Networks and Cognitive Architectures, Steven E Petersen, Olaf Sporns.

are functionally related.

Future scope and Challenges

Control State Patterns/reliability: Functional networks differ across individuals due to genetics, development, learning, or even moment-to-moment variability. Therefore, it is hard to consider FC a robust and actionable clinical tool.

Contract Security in Predicting Brain Waves: In adults, brain waves can often be associated with specific cognitive functions. However, in a developing brain, interpreting brain waves and understanding their correlations is more challenging.

*****<u>A Field in Fast Transition</u>: While the functional connectome provides insights into cognition, the emergence of improved experimental techniques and analytical methods is likely to reshape our understanding of the brain.

This continual evolution makes it a long-lasting and vital field in neuroscience.

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All the group members of Complex Systems Lab @ IISER Tirupati

Clockwise from left: Prateek Yadav (iPhD), Kartik Dahake (PhD), Amod Rai (PhD), Ritish Khetrapal (DST-Project associate-I), Sheksha (Project student)

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