

KEY

Section 1: Algebra

1.1 $1 \pm i\sqrt{6}, \pm \sqrt{3}$

1.2 a,c

1.3 a,b,c

1.4 (1625)(34)

1.5 a,b,c

1.6 (a) 4, (b) 2

1.7

$$\begin{bmatrix} 1 & 1 & 1 & 1 \\ 0 & 1 & 2 & 3 \\ 0 & 0 & 1 & 3 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

1.8 a,b

1.9 b,c

1.10 $\alpha = 1/4, \beta = 0$

Section 2: Analysis

2.1 yes, 0

2.2 (a) convergent, (b) convergent

2.3 a,b,c

2.4 a,c

2.5 (a) not uniformly convergent

(b) uniformly convergent

(c) not uniformly convergent

2.6 $4/e$

2.7 a,b,c

2.8 $\pi/16$

2.9 3

2.10 a,b,c

Section 3: Topology

3.1 b

3.2 a,c

3.3 a,b

3.4 b,c

3.5 a,c

3.6 a

3.7 b,c

3.8 none

3.9 none

3.10 $\{N, M\}, \{B\}, \{H\}$

Section 4: Applied Mathematics

4.1 $my'' = mg - c(y')^2$

4.2 $x' = y; y' = -Py - Qx$

4.3 $8\pi^2/15$

4.4 $(n+1)a_{n+1} = (p-n)a_n, n \geq 0$

4.5 $y = (1+x)^p$

4.6 (a) Elliptic, (b) Hyperbolic

4.7 0

4.8 $(x/a, y/a, z/a)$

4.9 $12\pi a^6/5$

4.10 $u_t = u_{xx}$

Section 5: Miscellaneous

5.1 $(2^{n+1} - 1)/(n+1)$

5.2 $(2n)!/n^2$

5.3 $2/3$

5.4 a,b,c

5.5 $\sin \theta \cos \theta$

5.6 $1 - \log 2$

5.7 $2\sqrt{2}$

5.8 $\frac{1}{2} - \frac{1}{(n+2)!}; \frac{1}{2}$

5.9 $abc + 1 = 0$

5.10 $(2/3, 0)$

Note:

Accept any correct equivalent form of the answers.