

# WHAT WE CAN LEARN FROM ATMOSPHERIC NEUTRINOS

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# Goals for the Future / Plan of Talk





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- Using atmospheric neutrinos to constrain new physics



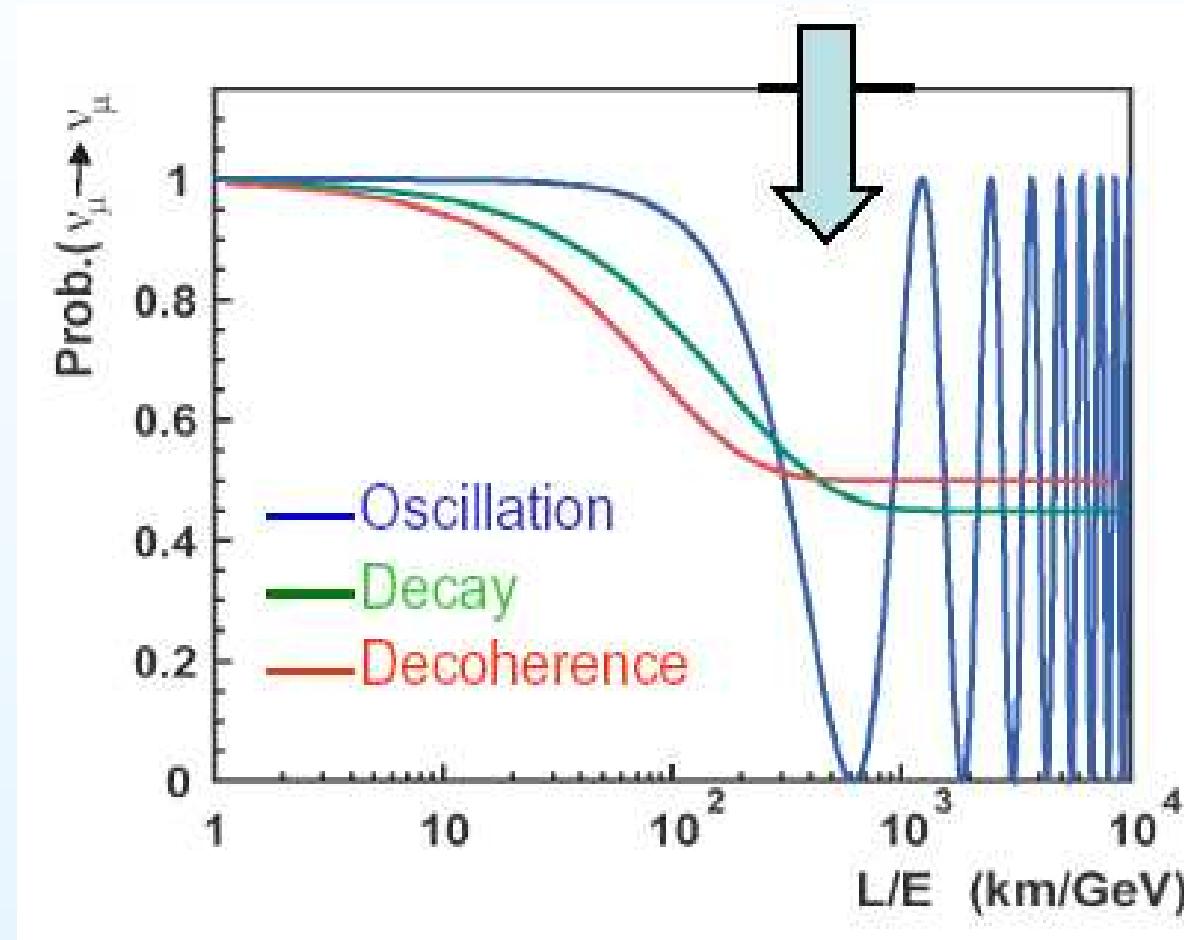
# Confirmation of Oscillations of Atmospheric Neutrinos





# Confirmation of Oscillations of Atmospheric Neutrinos

- Smoking Gun Signal for  $\nu_\mu - \nu_\tau$  Oscillations



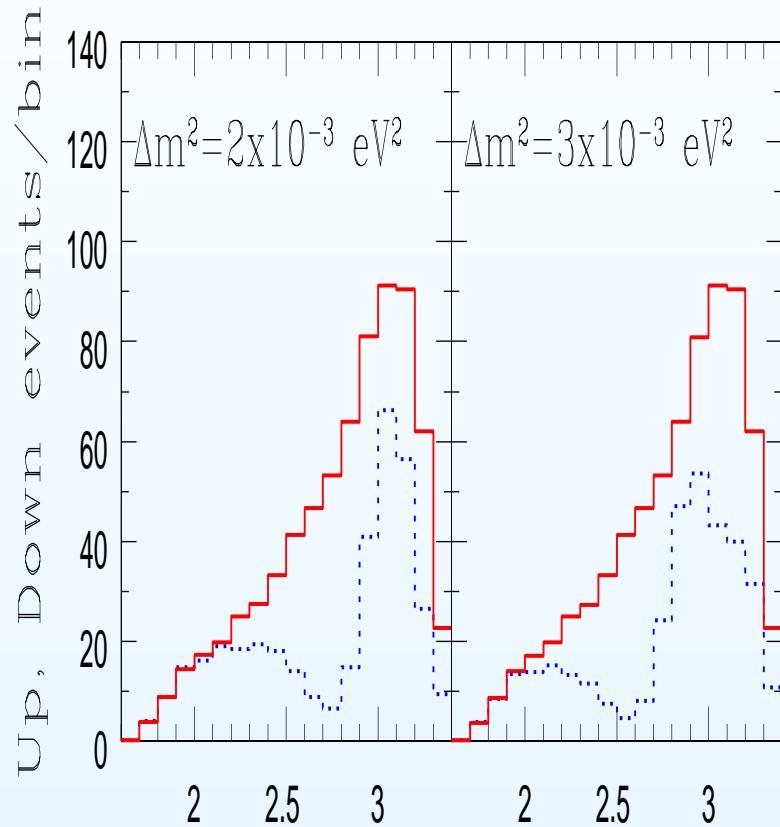
SK collab, Koshio talk, NANP '05

- Its important to observe the characteristic “dip” in  $L/E$





# Confirmation of Oscillations of Atmospheric Neutrinos

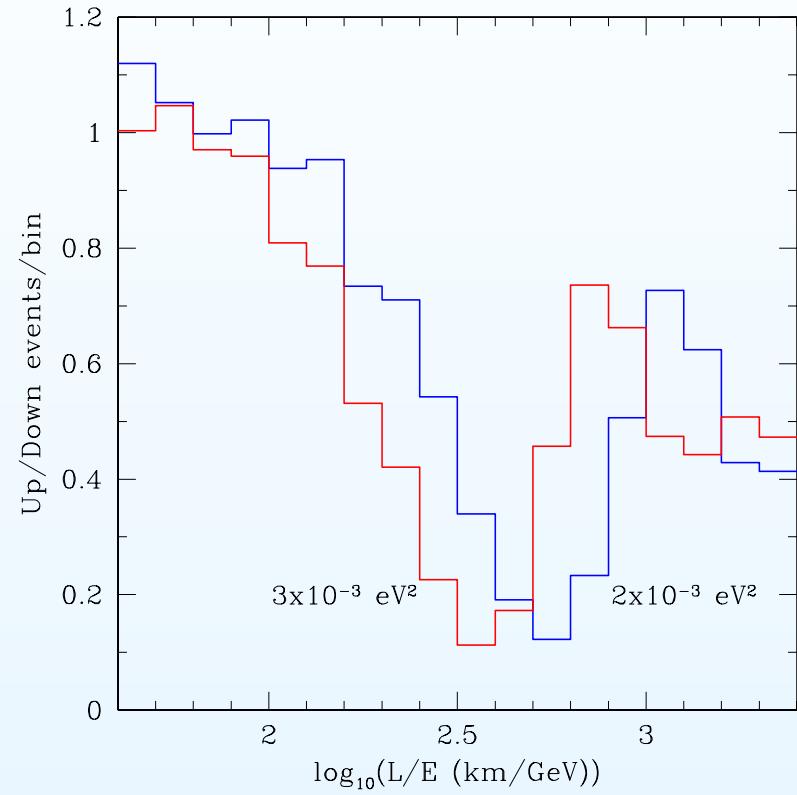
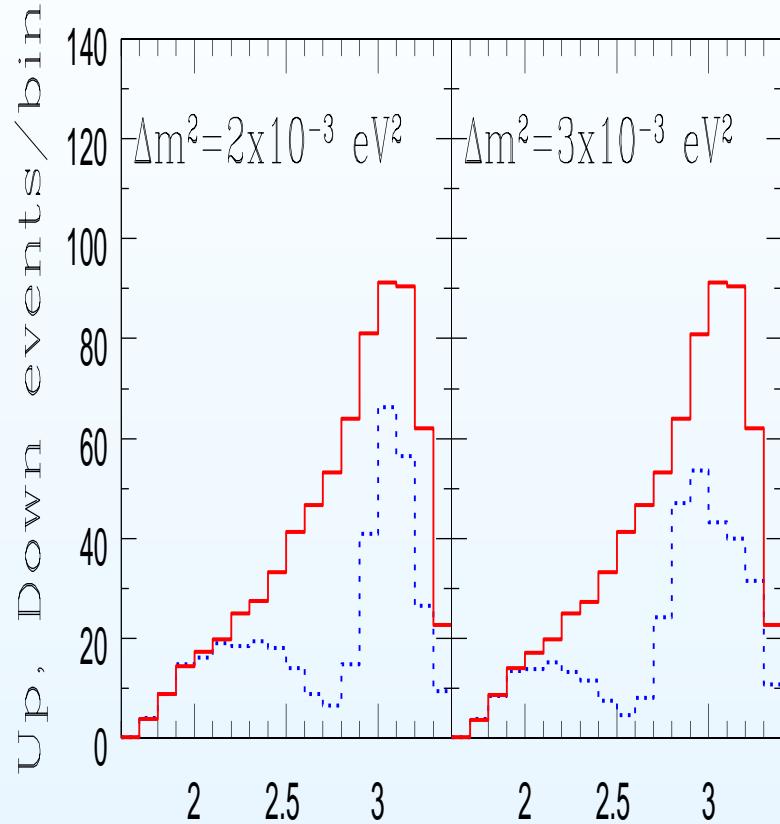


$$\log_{10}(L/E \text{ (km/GeV)})$$

INO collaboration



# Confirmation of Oscillations of Atmospheric Neutrinos



$$\log_{10}(L/E \text{ (km/GeV)})$$

- The first oscillation dip should be clearly observable INO collaboration





# Precision Measurement of $\Delta m_{31}^2$ and $\theta_{23}$





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Experiment	$ \Delta m_{31}^2 $	$\sin^2 \theta_{23}$
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MINOS+CNGS	13%	38%
T2K (5 yrs)	6%	22%
NO $\nu$ A (5 yrs)	13%	42%
Combination	4.5%	20%

Huber et al hep-ph/0403068





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Combination	4.5%	20%
SK20 (1.84 MTy)	17%	24%
INO (250 kTy)	10%	30%

Huber et al hep-ph/0403068

Gonzalez-Garcia et al, hep-ph/0408170

INO Collaboration





# Three Generation Oscillation Probabilities





# Muon Neutrino Survival Probability

$$\lim_{\Delta m_{21}^2 \rightarrow 0} P_{\mu\mu}(L, E) = 1 - P_{\mu\mu}^1(L, E) - P_{\mu\mu}^2(L, E) - P_{\mu\mu}^3(L, E)$$

$$P_{\mu\mu}^1(L, E) = \sin^2 \theta_{13}^M \text{sin}^2 2\theta_{23} \sin^2 \frac{(A + \Delta m_{31}^2) - (\Delta m_{31}^2)^M}{8E} L$$

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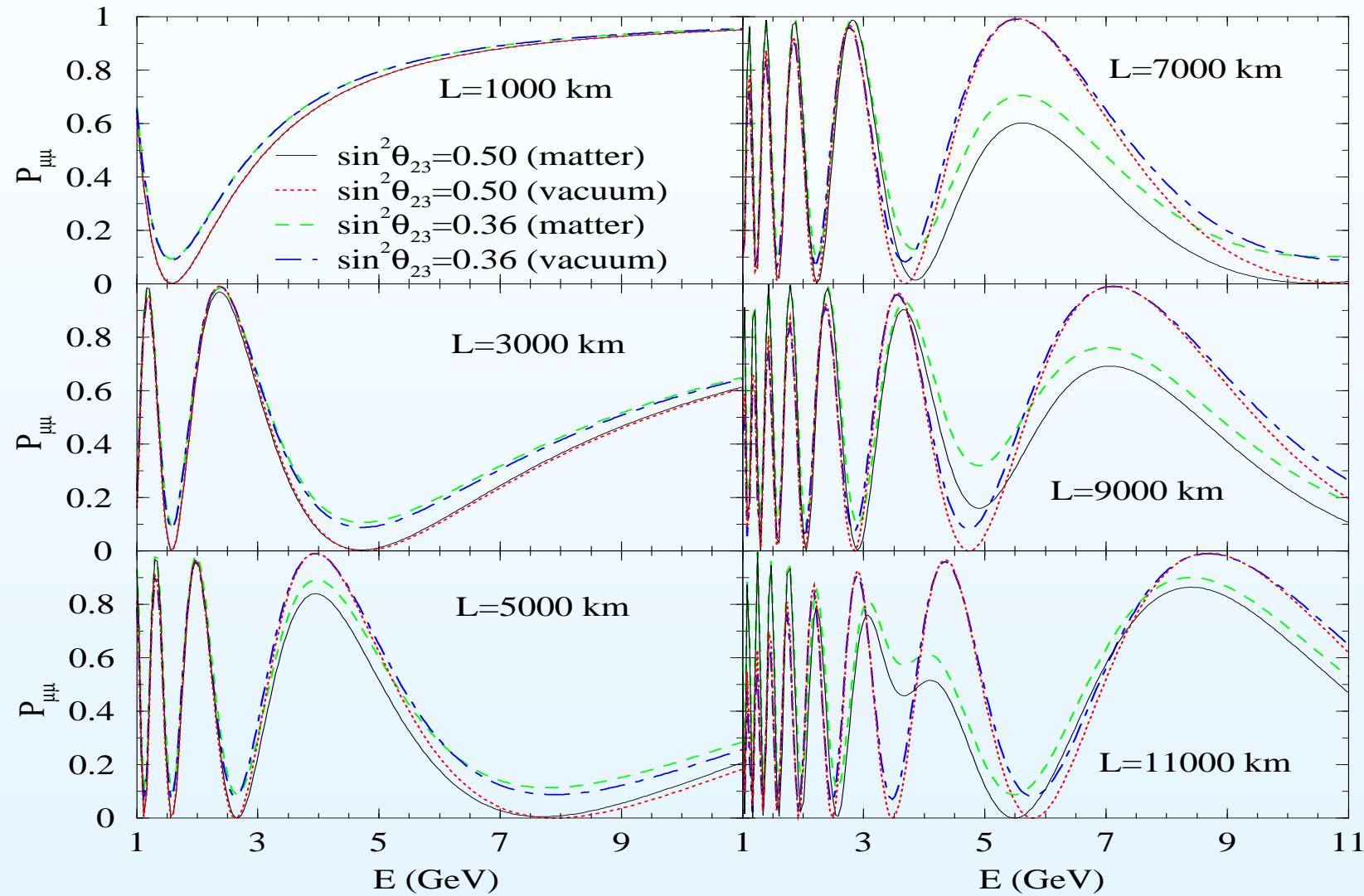
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- Dependence on  $\theta_{23}$  in the form  $\sin^4 \theta_{23}$
- Octant sensitivity is expected to be good





# Large Matter Effects in $\nu_\mu$ Survival Probability

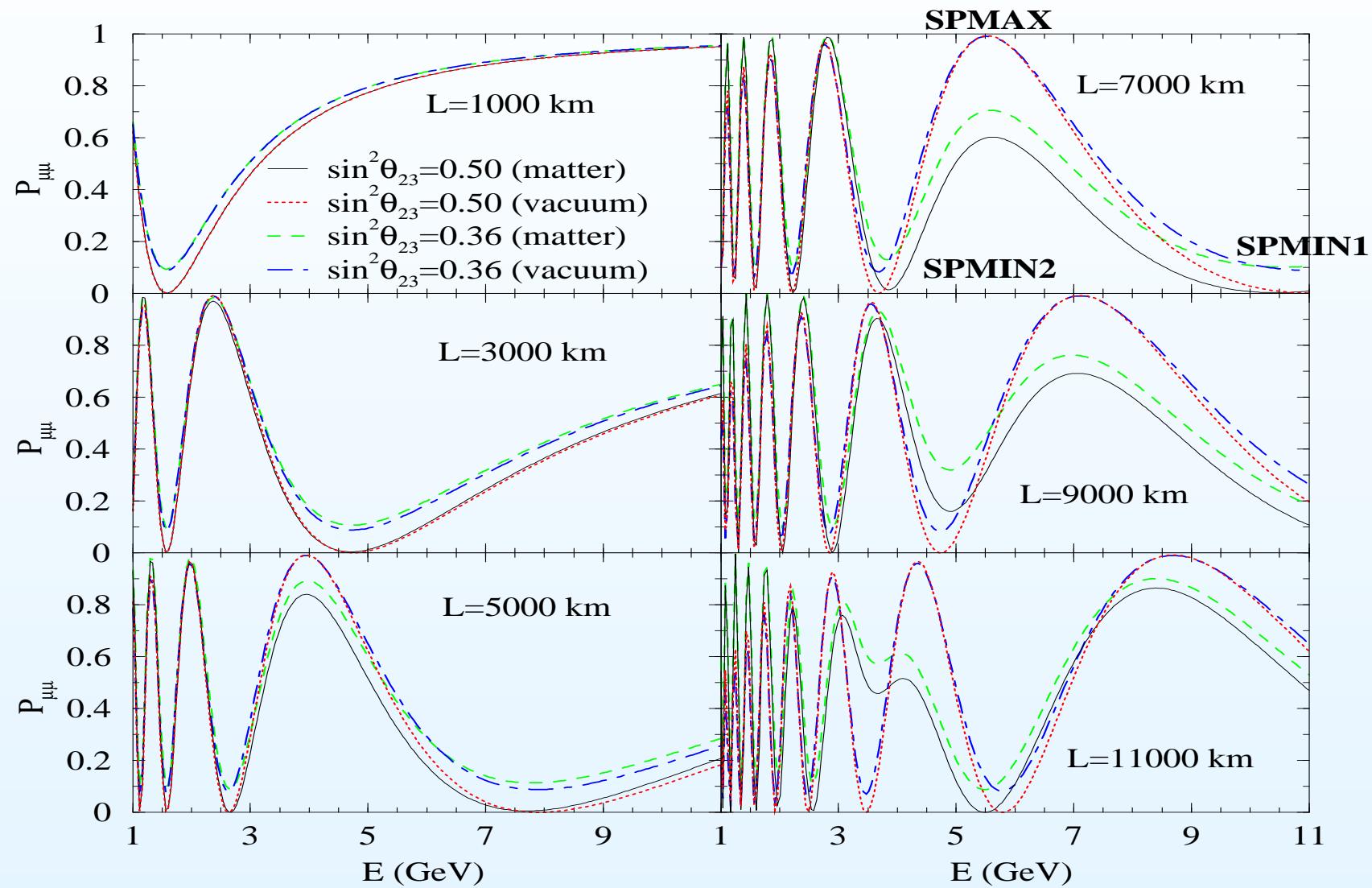


S.C. and P. Roy, hep-ph/0509197





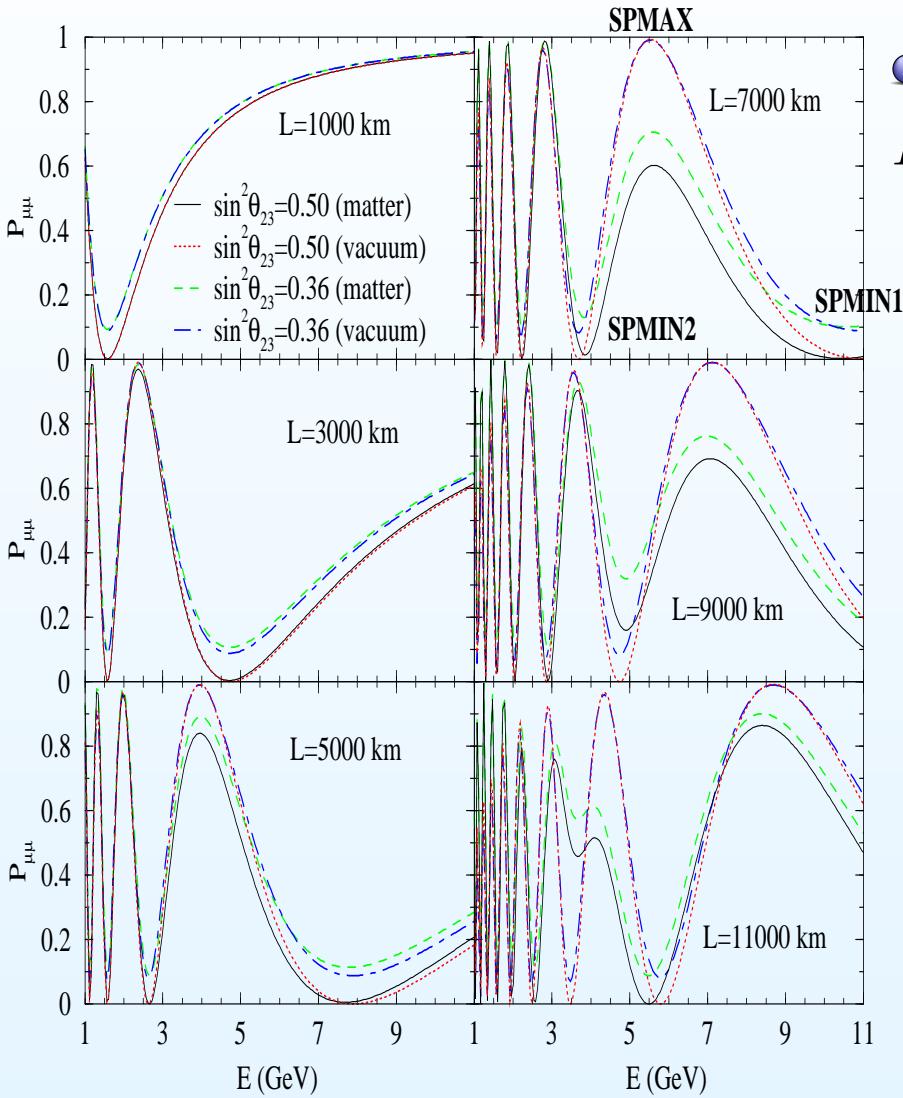
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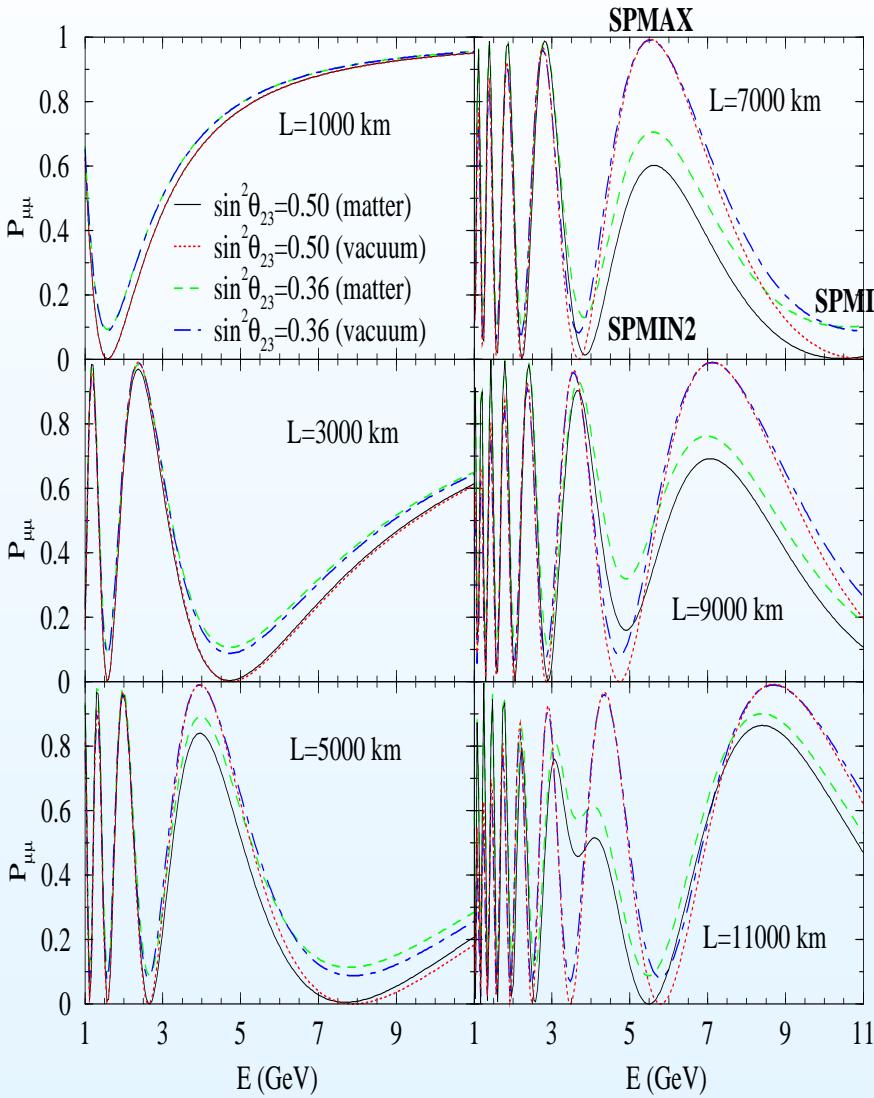
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Max effect for  $L \simeq 7000$  km and  
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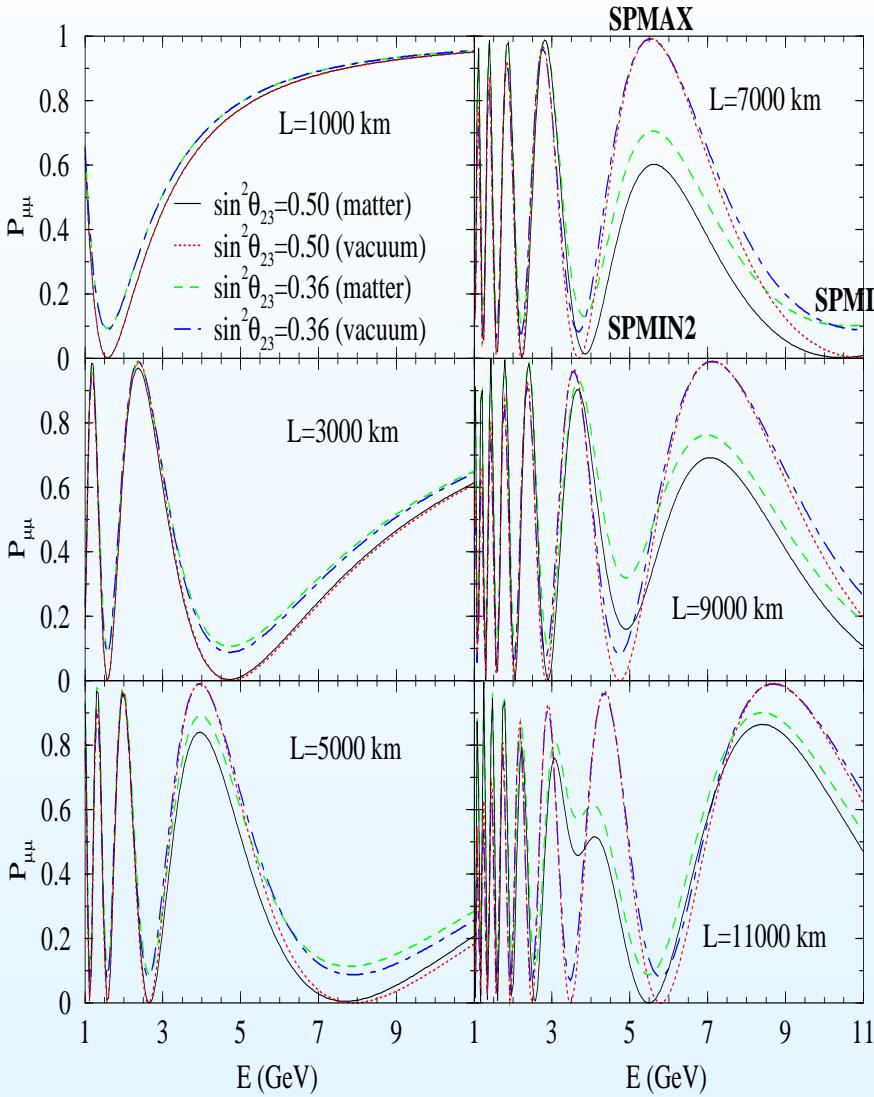
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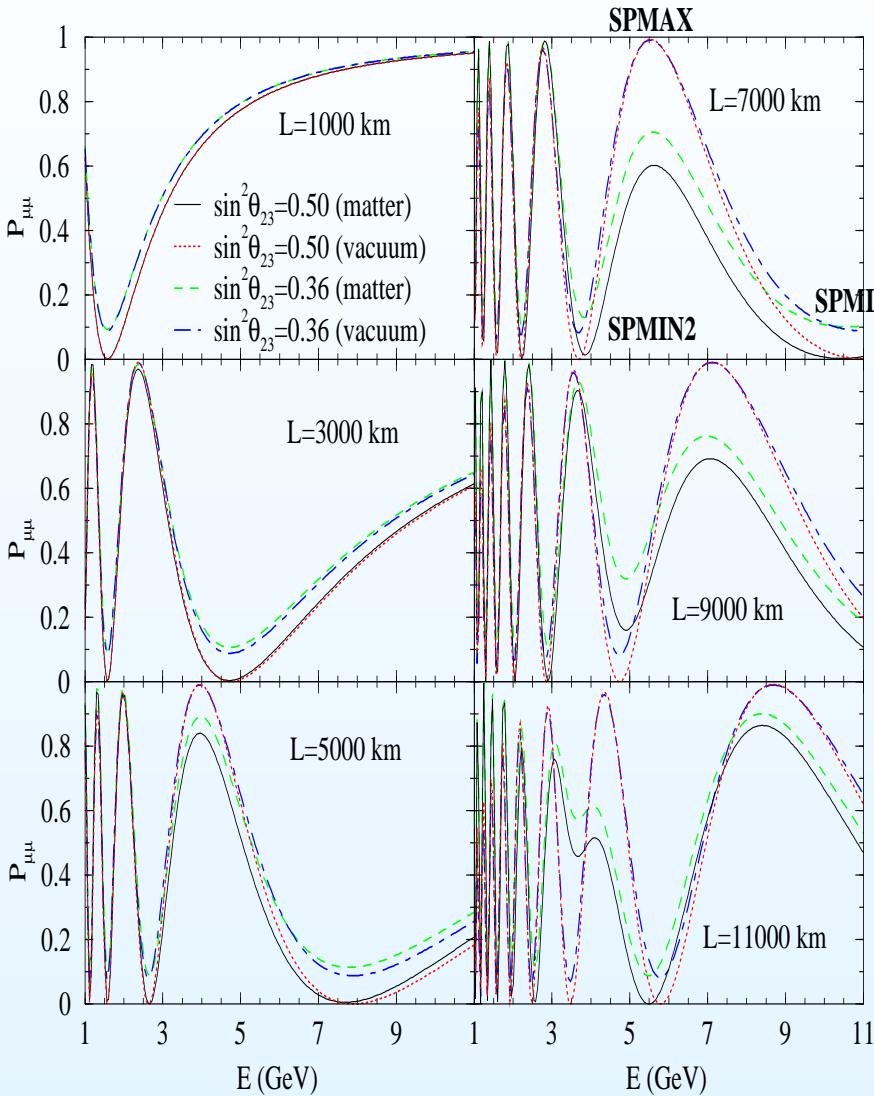
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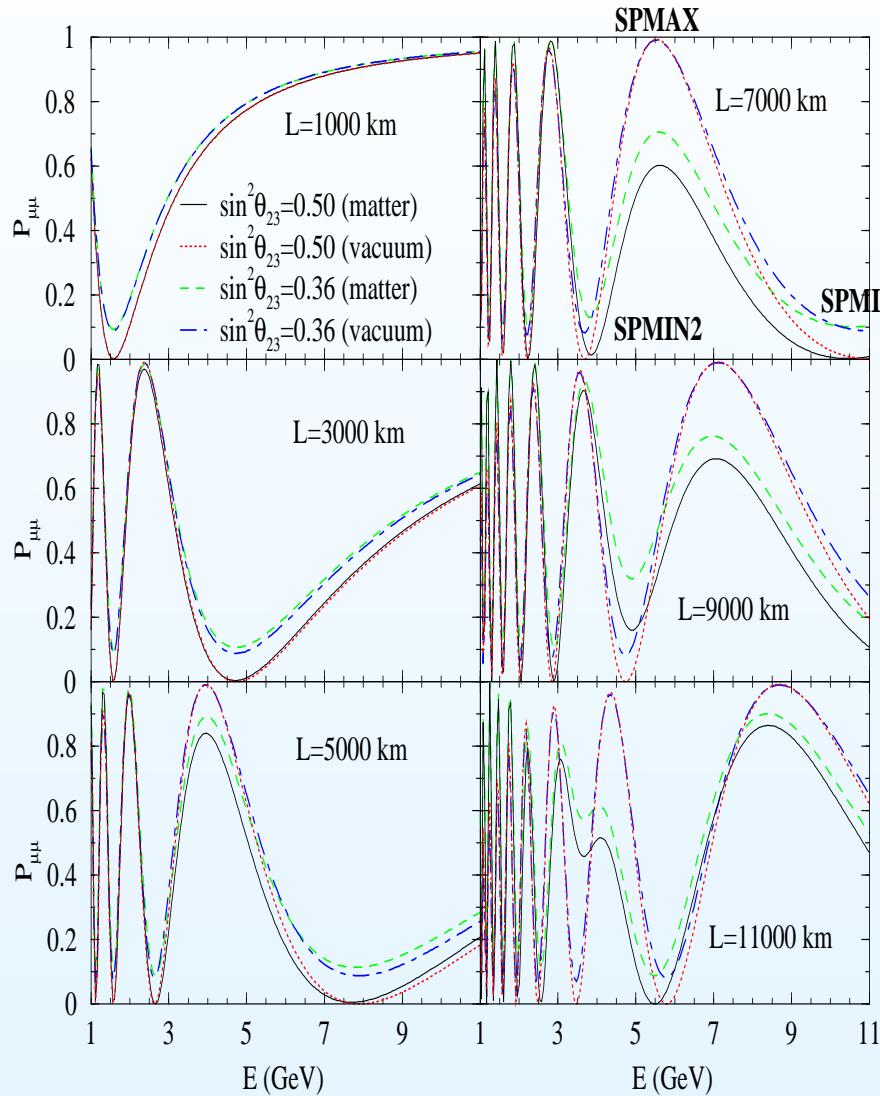
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- Matter effects depend on the value of  $\sin^2 \theta_{23}$



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- Sign of the earth matter effects depends on both  $E$  and  $L$
- Matter effects depend on the value of  $\sin^2 \theta_{23}$

- Most important to choose the bins properly in both  $E$  and  $L$





# Very Large Matter Effects in $\nu_\mu \leftrightarrow \nu_e$ Probability



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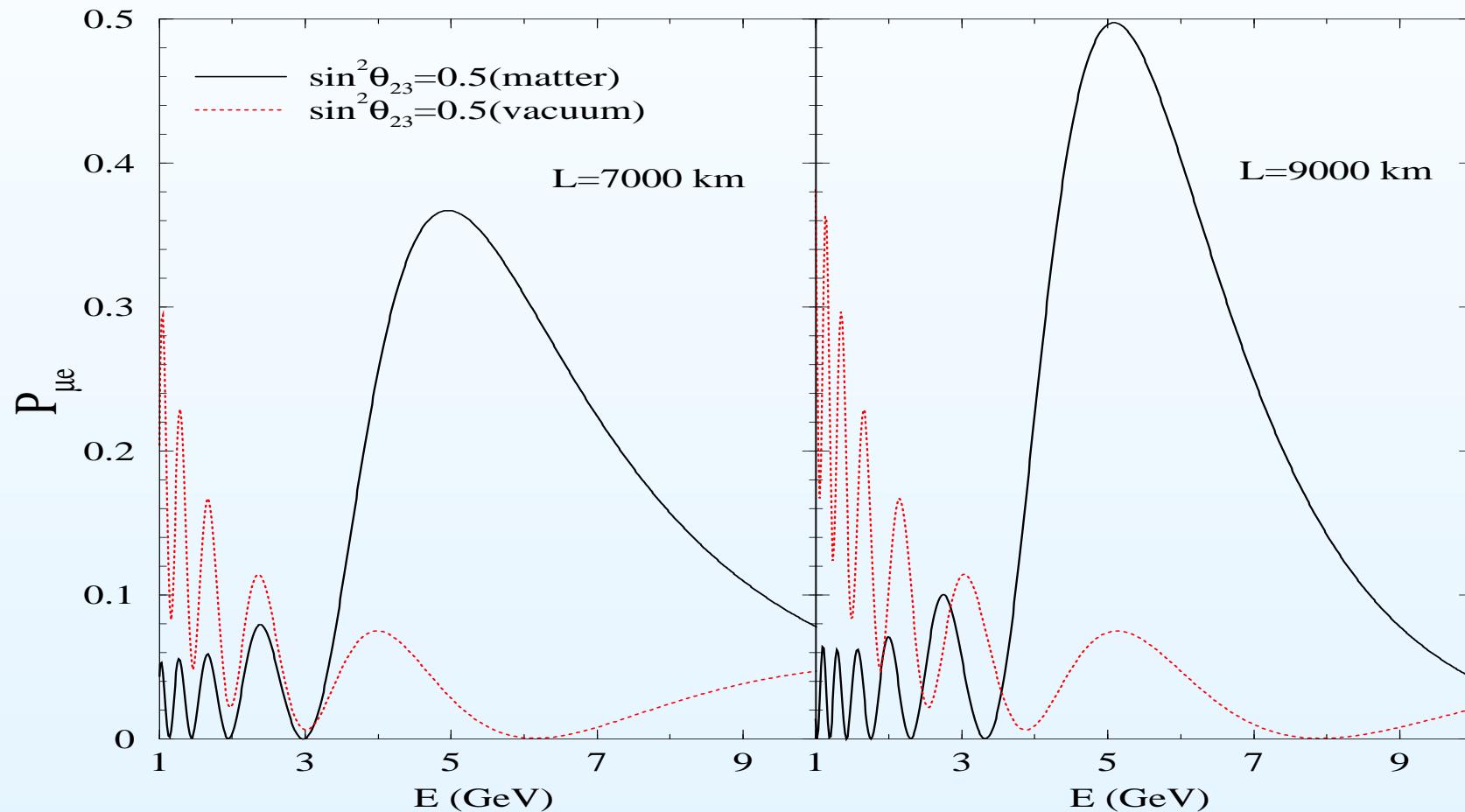
$$\lim_{\Delta m_{21}^2 \rightarrow 0} P_{\mu e}(L, E) = \sin^2 \theta_{23} \sin^2 2\theta_{13}^M \sin^2 \frac{(\Delta m_{31}^2)^M L}{4E}$$





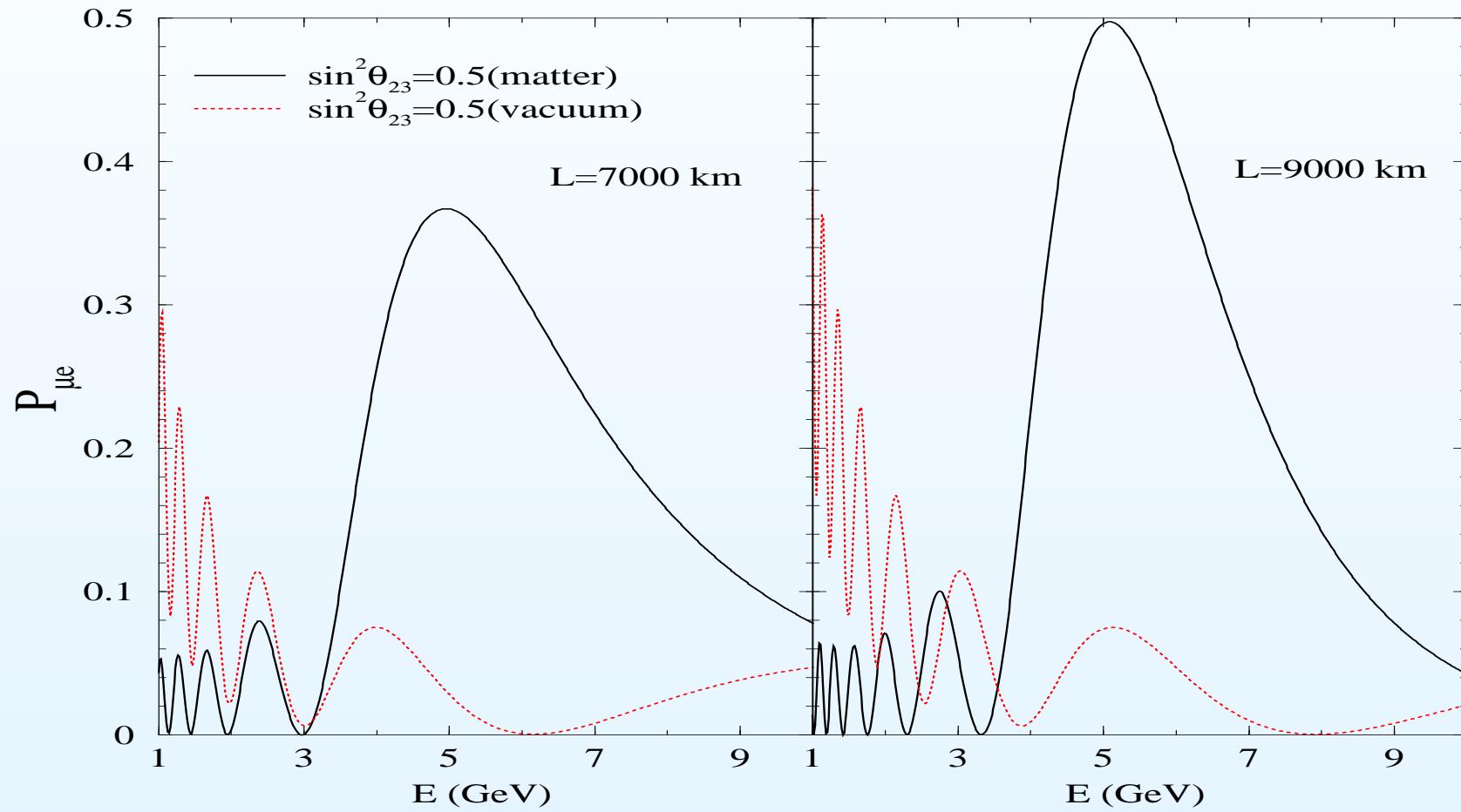
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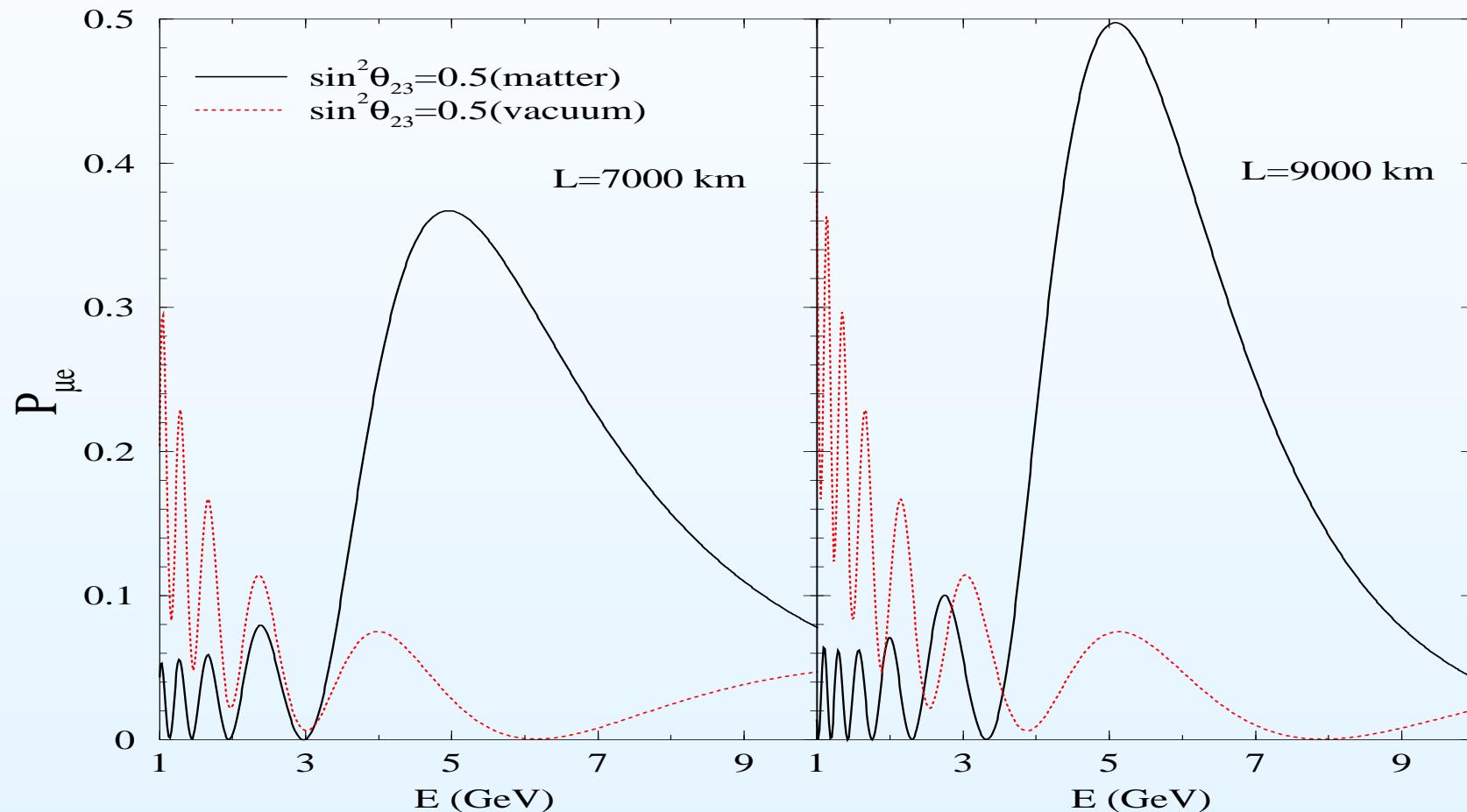
- Above  $\sim 3$  GeV, matter effects increase  $P_{\mu e}$  for all  $E$  and  $L$





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- Sub-dominant  $\Delta m_{21}^2$  oscillations in  $P_{\mu e}$  is also crucial





# Atmospheric Neutrino Events





# Atmospheric Neutrino Events

Change in number of muon events:

$$\begin{aligned} N_\mu &= N_\mu^0 P_{\mu\mu} + N_e^0 P_{e\mu} \\ &= N_\mu^0 \left[ P_{\mu\mu} + \frac{1}{r} P_{e\mu} \right]; \quad (\text{where } r = \frac{N_\mu^0}{N_e^0}) \end{aligned}$$

$$1 - \frac{N_\mu}{N_\mu^0} \simeq (P_{\mu\mu}^1 + P_{\mu\mu}^2) + (P_{\mu\mu}^3)' s_{23}^2 (s_{23}^2 - \frac{1}{r})$$

$$(P_{\mu\mu}^3)' = \sin^2 2\theta_{13}^M \sin^2 \frac{(\Delta m_{31}^2)^M}{4E} L$$

- Can be used to study maximality and octant of  $\theta_{23}$
- Can be used to study the neutrino mass hierarchy
- $\Delta m_{21}^2$  and  $\delta_{CP}$  bring in small effects





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Change in number of electron events:

$$\begin{aligned}\frac{N_e}{N_e^0} - 1 &\simeq \sin^2 2\theta_{12}^M \sin^2 \left( \frac{(\Delta m_{21}^2)^M L}{4E} \right) \times (r \cos^2 \theta_{23} - 1) \\ &+ \sin^2 2\theta_{13}^M \sin^2 \left( \frac{(\Delta m_{31}^2)^M L}{4E} \right) \times (r \sin^2 \theta_{23} - 1) \\ &+ \sin \theta_{23} \cos \theta_{23} r \operatorname{Re} \left[ A_{13}^* A_{12} \exp(-i\delta_{CP}) \right]\end{aligned}$$





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- $\theta_{13}$ -driven oscillation effect





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- Can be used for studying the neutrino mass hierarchy





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- “interference” term which depends on  $\delta_{CP}$
- It might cancel the effect of the  $\Delta m_{21}^2$  and  $\theta_{13}$  terms depending on the value of  $\delta_{CP}$  – bad bad bad...





# Atmospheric Neutrino Events

Change in number of electron events:

$$\begin{aligned}\frac{N_e}{N_e^0} - 1 &\simeq \sin^2 2\theta_{12}^M \sin^2 \left( \frac{(\Delta m_{21}^2)^M L}{4E} \right) \times (r \cos^2 \theta_{23} - 1) \\ &+ \sin^2 2\theta_{13}^M \sin^2 \left( \frac{(\Delta m_{31}^2)^M L}{4E} \right) \times (r \sin^2 \theta_{23} - 1) \\ &+ \sin \theta_{23} \cos \theta_{23} r \operatorname{Re} \left[ A_{13}^* A_{12} \exp(-i\delta_{CP}) \right]\end{aligned}$$

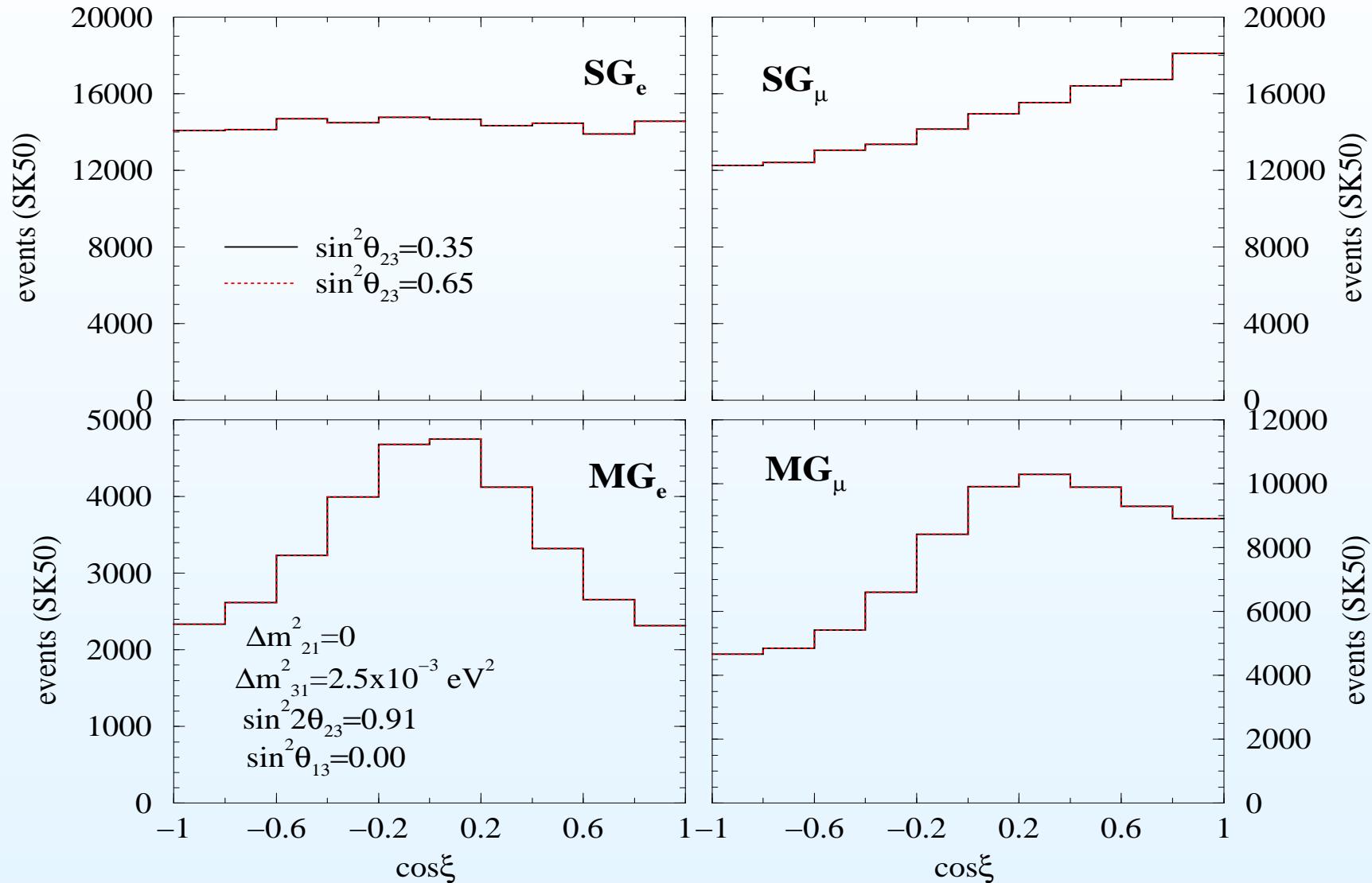
- “interference” term which depends on  $\delta_{CP}$
- It might cancel the effect of the  $\Delta m_{21}^2$  and  $\theta_{13}$  terms depending on the value of  $\delta_{CP}$  – bad bad bad...
- But it might tell us if  $\delta_{CP} = 0$  or  $\pi$  (Fogli et al. hep-ph/0506083)



# Atmospheric Neutrino Events in MTon Water Detector

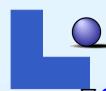
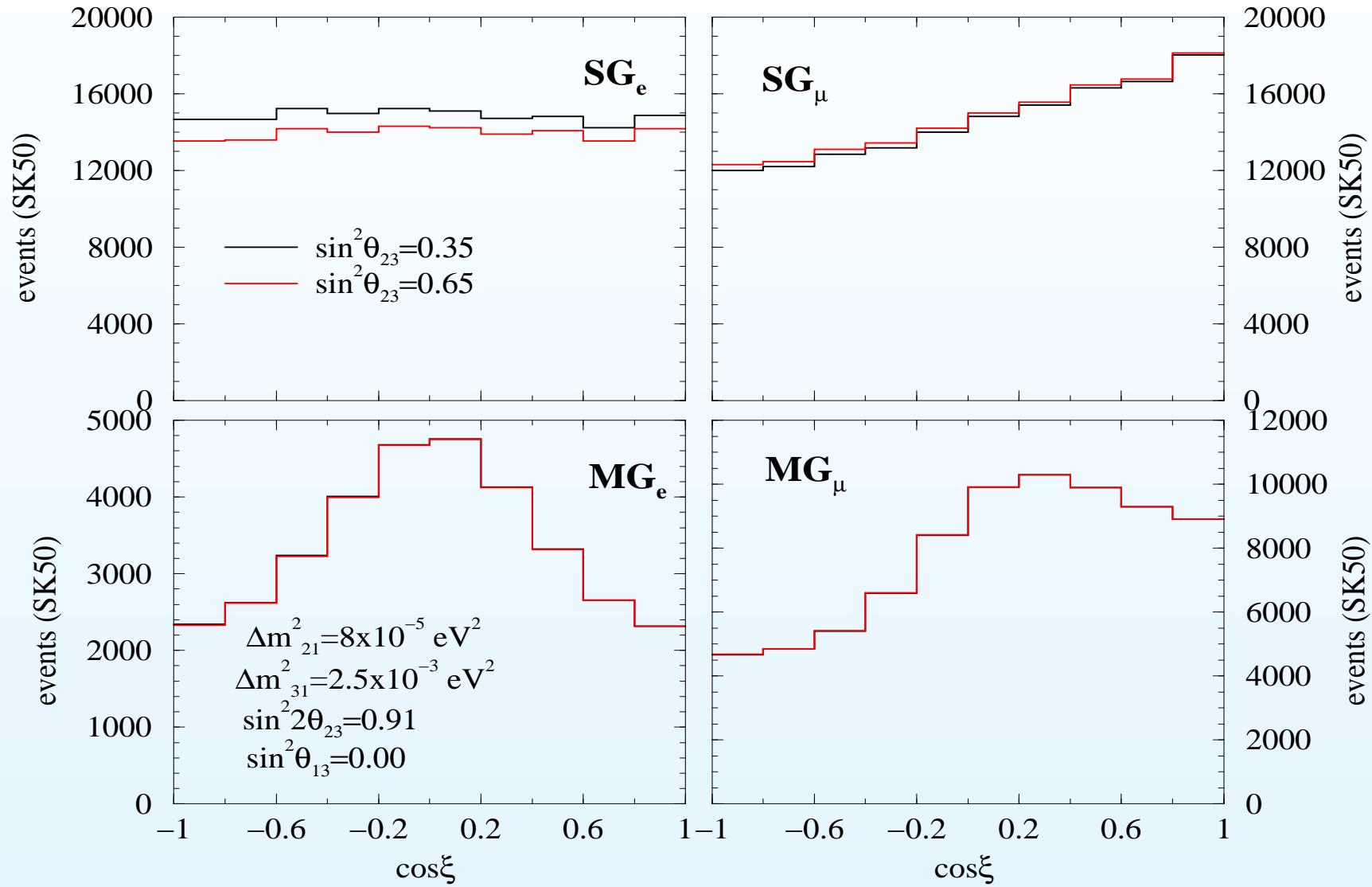


# Atmospheric Neutrino Events in MTon Water Detector



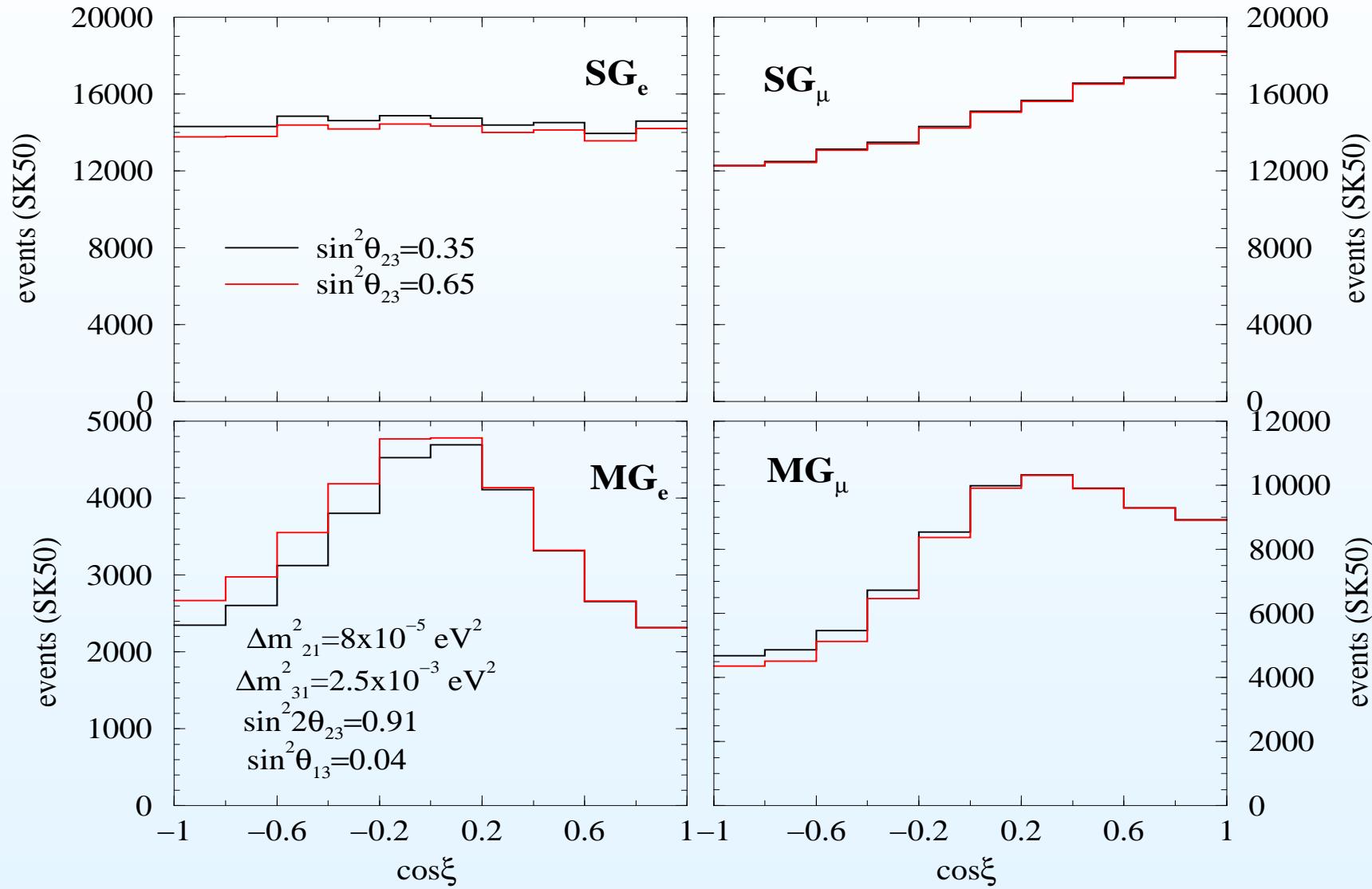
L These are just 2-gen  $\nu_\mu \rightarrow \nu_\tau$  oscillations

# Atmospheric Neutrino Events in MTon Water Detector



$\Delta m_{21}^2$ -driven oscillations bring in octant sensitivity in SGe events

# Atmospheric Neutrino Events in MTon Water Detector



$\theta_{13}$  brings in more octant sensitivity through matter effects

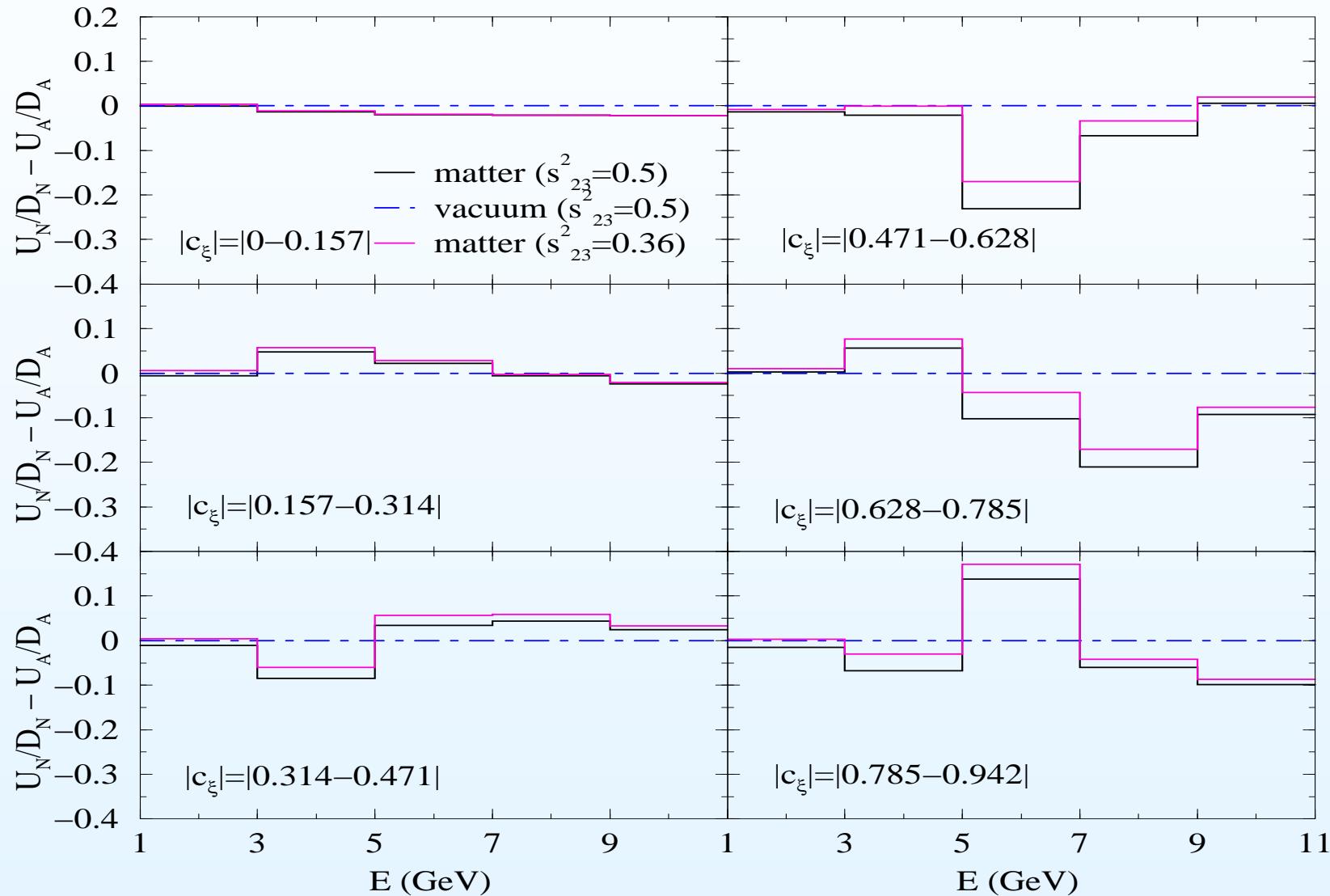


# Atmospheric Neutrino Events in INO-ICAL





# Atmospheric Neutrino Events in INO-ICAL



S.C and P. Roy hep-ph/0509197



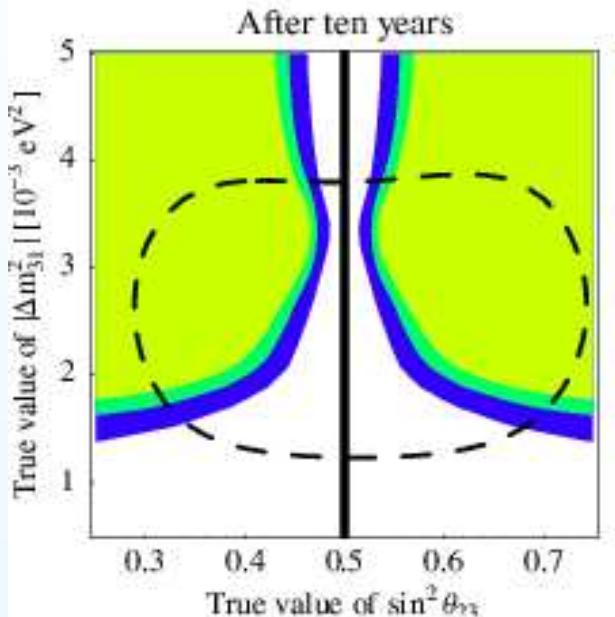


# Testing Maximality of $\theta_{23}$





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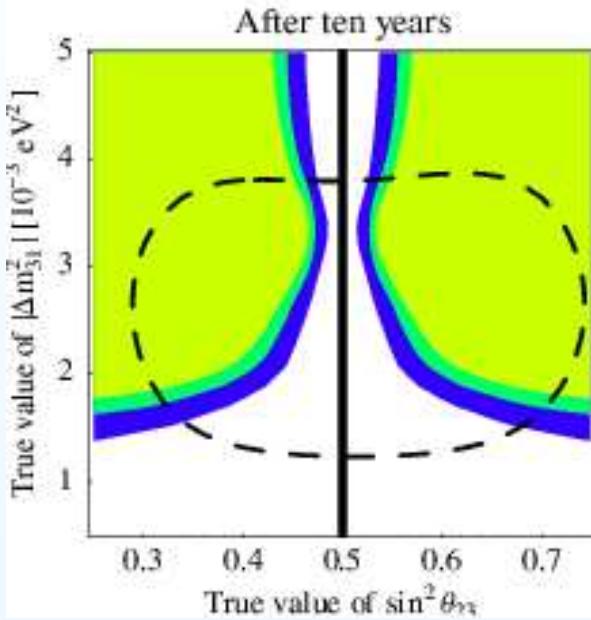
$|D|$  within 14%  
LBL combined

Antusch, et al,  
hep-ph/0404268



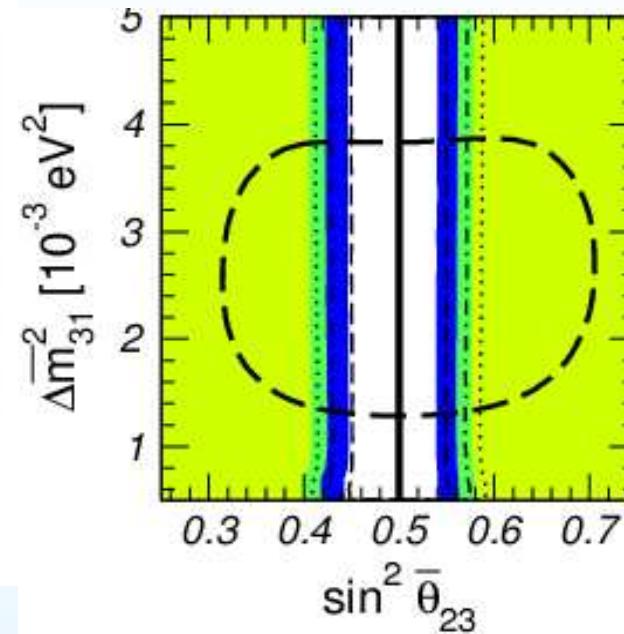


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LBL combined

Antusch, et al,  
hep-ph/0404268

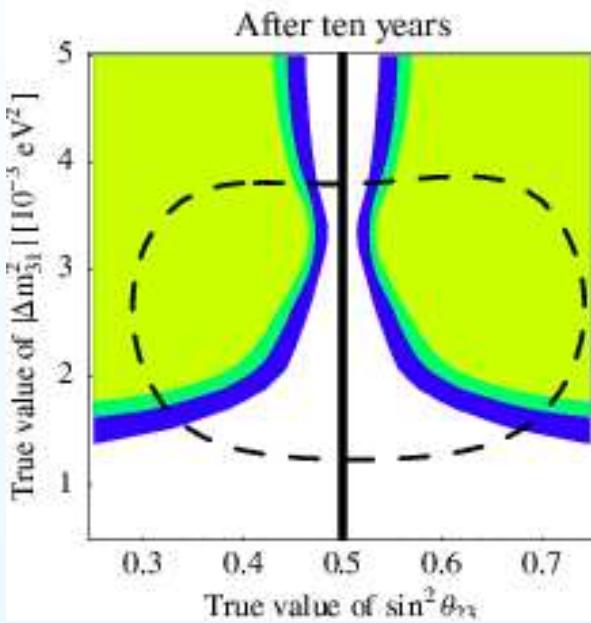


$|D|$  within 19%  
SK50  
Gonzalez-Garcia, et al,  
hep-ph/0408170



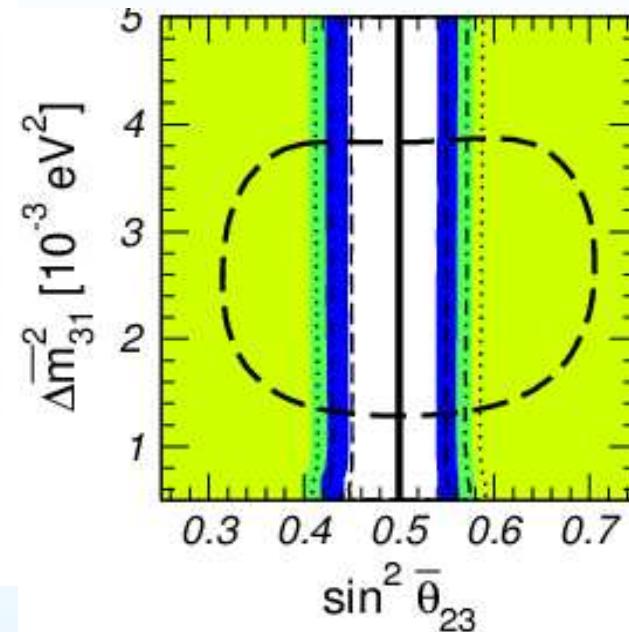


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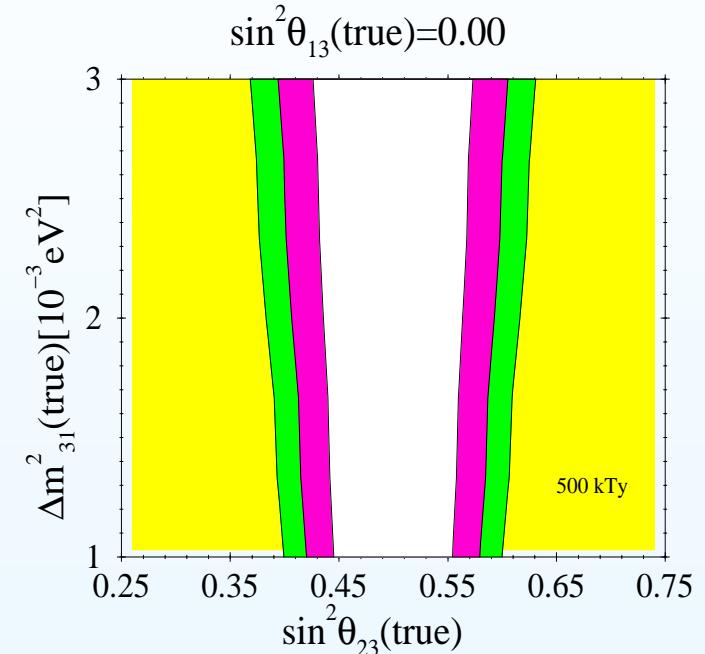


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Antusch, et al,  
hep-ph/0404268



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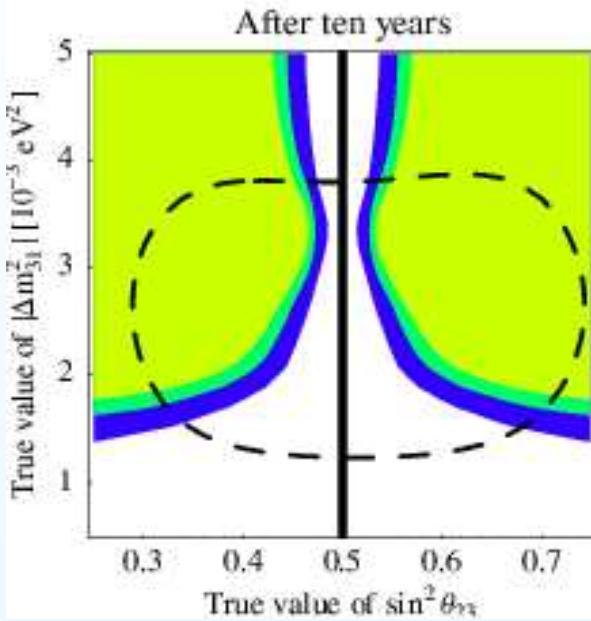


$|D|$  within 25%  
INO-ICAL 500 kTy  
S.C. and P. Roy,  
hep-ph/0509197



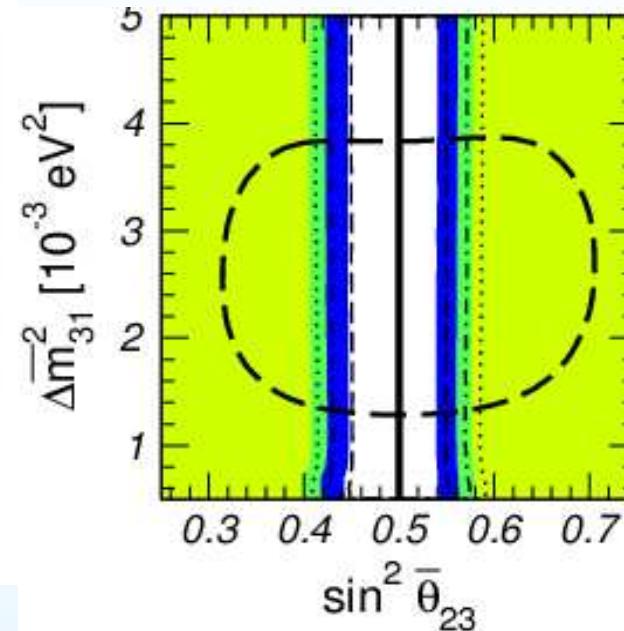


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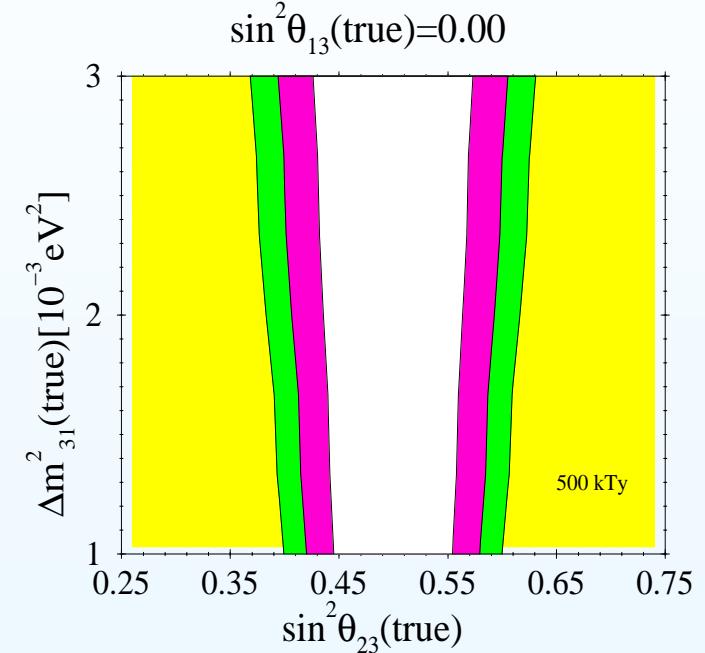
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hep-ph/0404268



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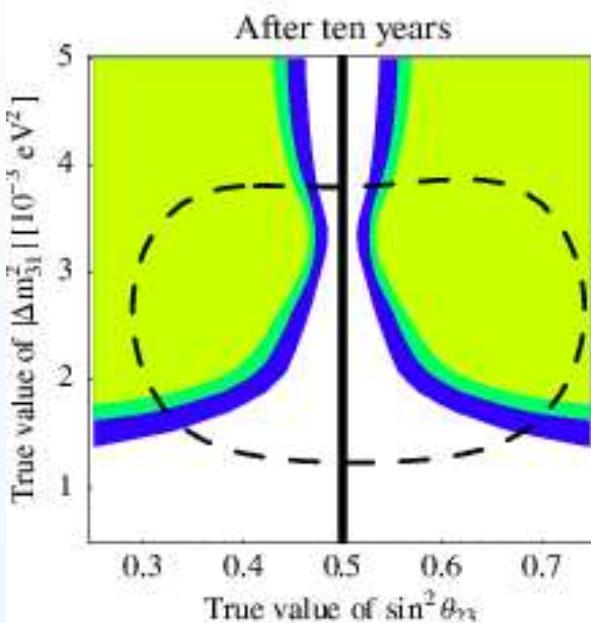
S.C. and P. Roy,  
hep-ph/0509197

- Sensitivity to  $|D| \equiv |(\sin^2 \theta_{23} - 0.5)|$  comparable to LBL expts



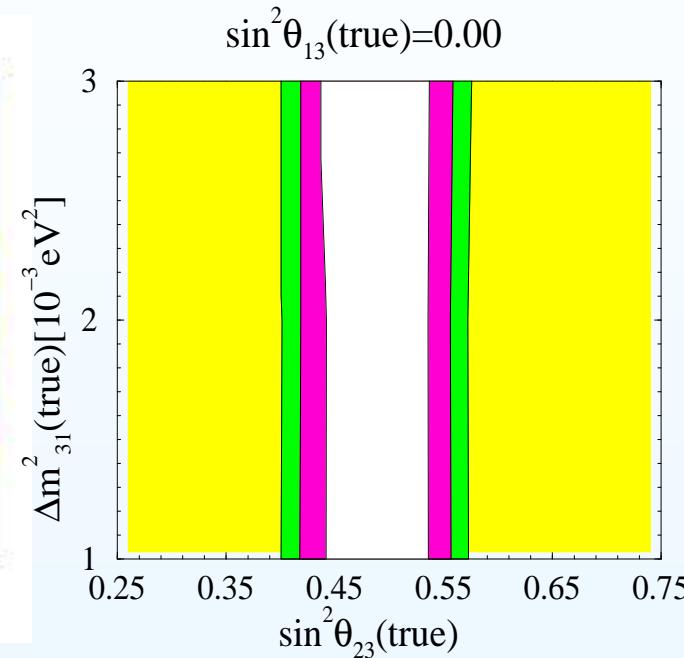


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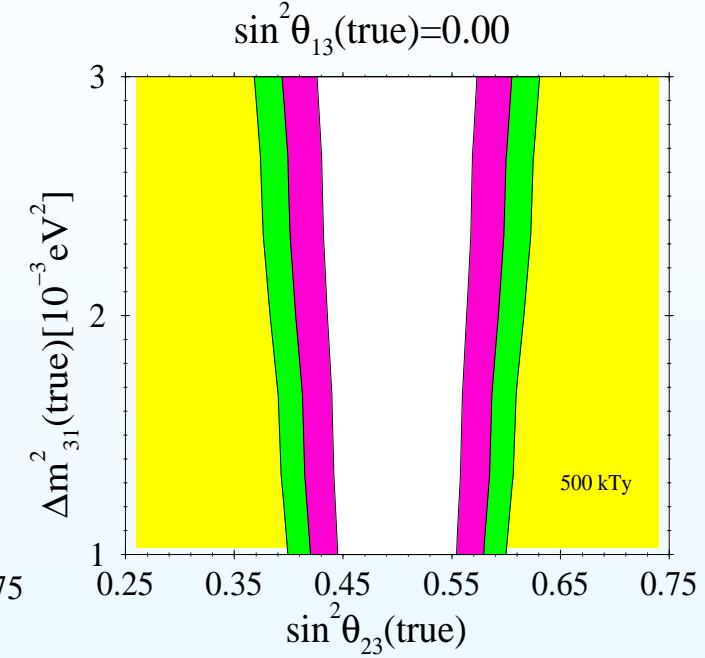


$|D|$  within 14%  
LBL combined

Antusch, et al,  
hep-ph/0404268



$|D|$  within 20%  
SK50  
preliminary



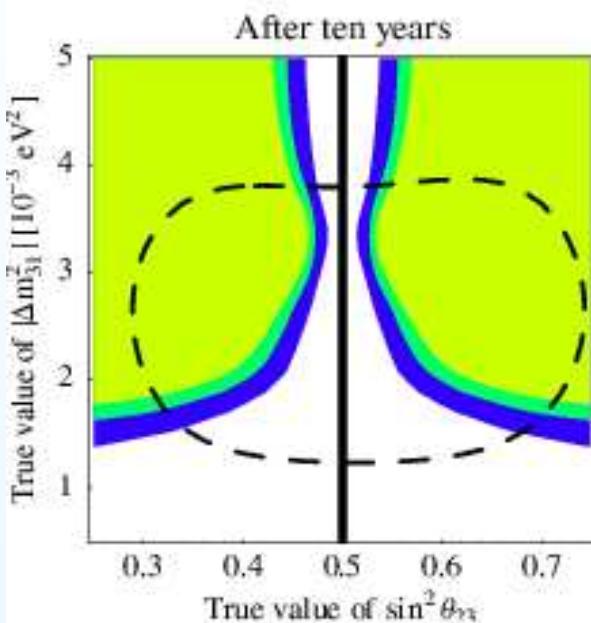
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S.C. and P. Roy,  
hep-ph/0509197

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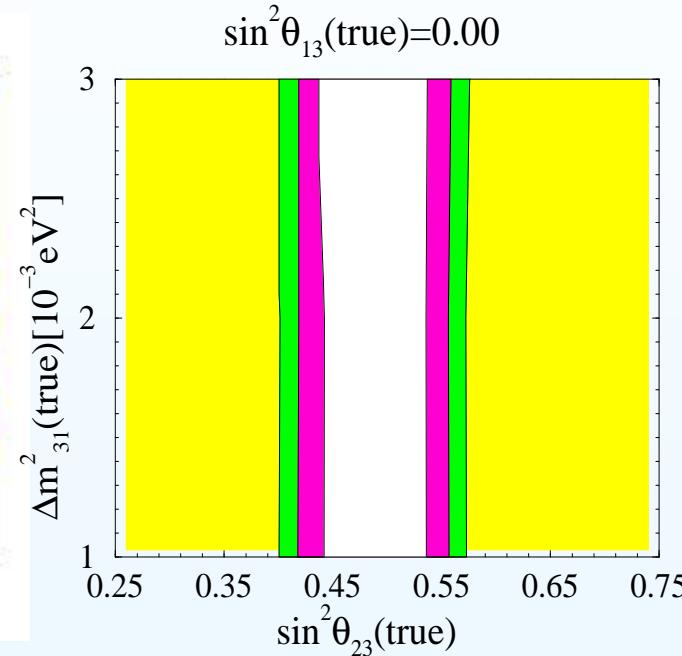




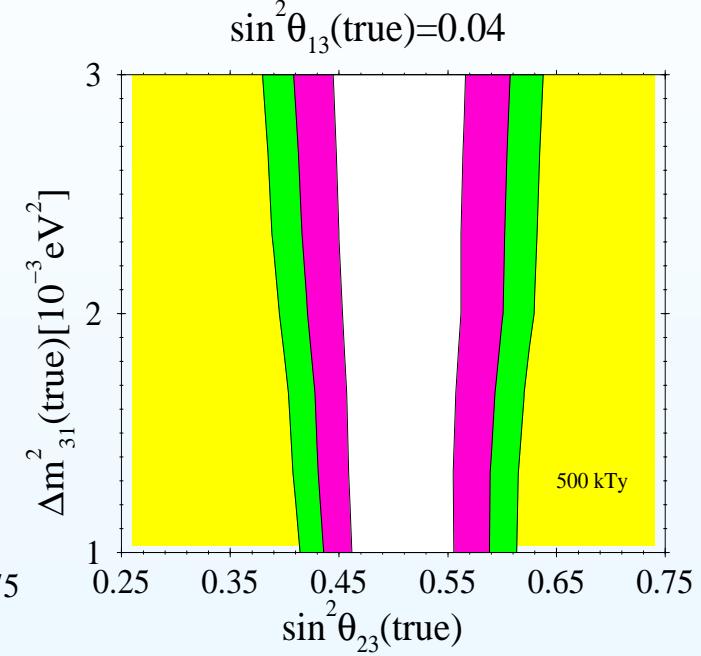
# Testing Maximality of $\theta_{23}$



$|D|$  within 14%  
LBL combined  
Antusch, et al,  
hep-ph/0404268



$|D|$  within 20%  
SK50  
preliminary



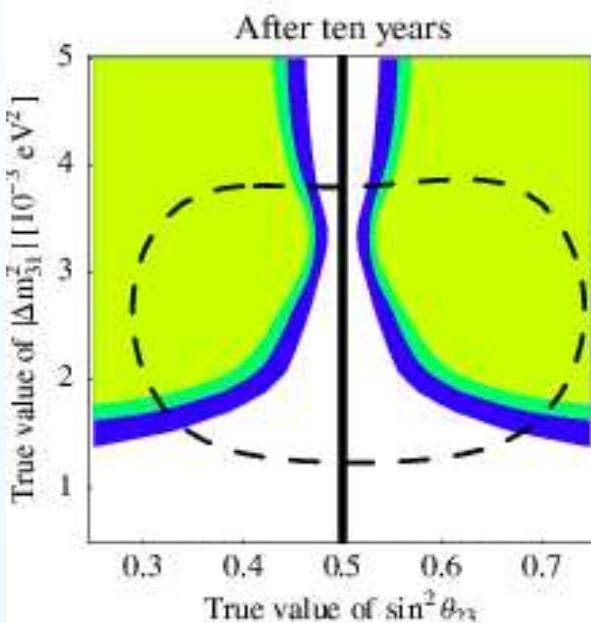
$|D|$  within 23%  
INO-ICAL 500 kTy  
S.C. and P. Roy,  
hep-ph/0509197

- Sensitivity to  $|D|$  in INO-ICAL improves marginally with  $\theta_{13}$



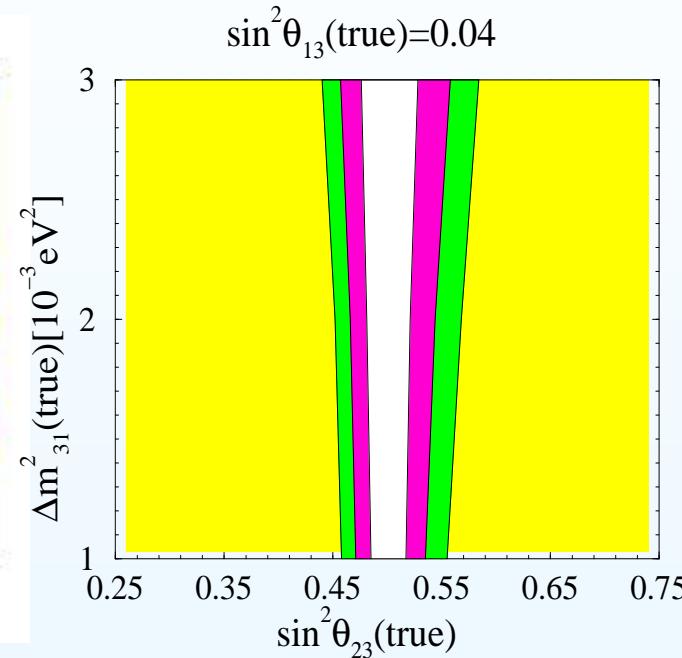


# Testing Maximality of $\theta_{23}$

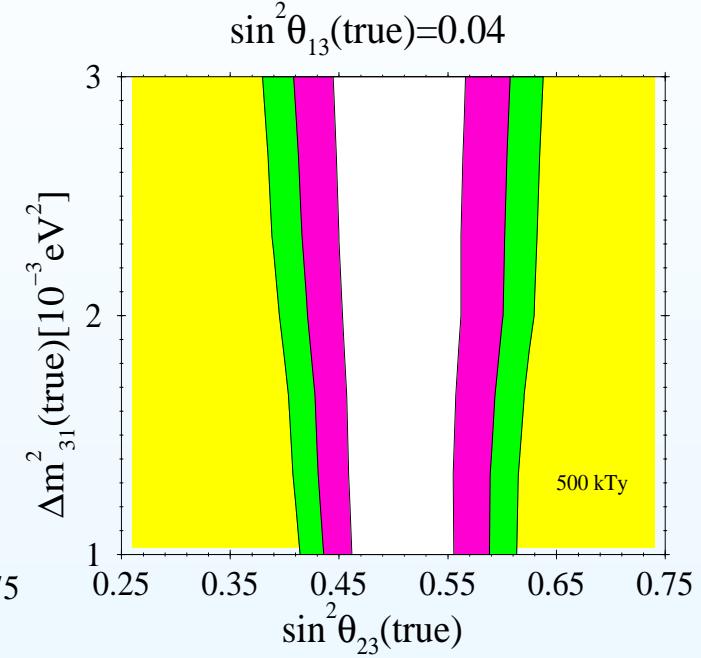


$|D|$  within 14%  
LBL combined

Antusch, et al,  
hep-ph/0404268



$|D|$  within 11%  
SK50  
preliminary



$|D|$  within 23%  
INO-ICAL 500 kTy  
S.C. and P. Roy,  
hep-ph/0509197

- Sensitivity to  $|D|$  in INO-ICAL improves marginally with  $\theta_{13}$
- Sensitivity to  $|D|$  in SK50 improves remarkably with  $\theta_{13}$

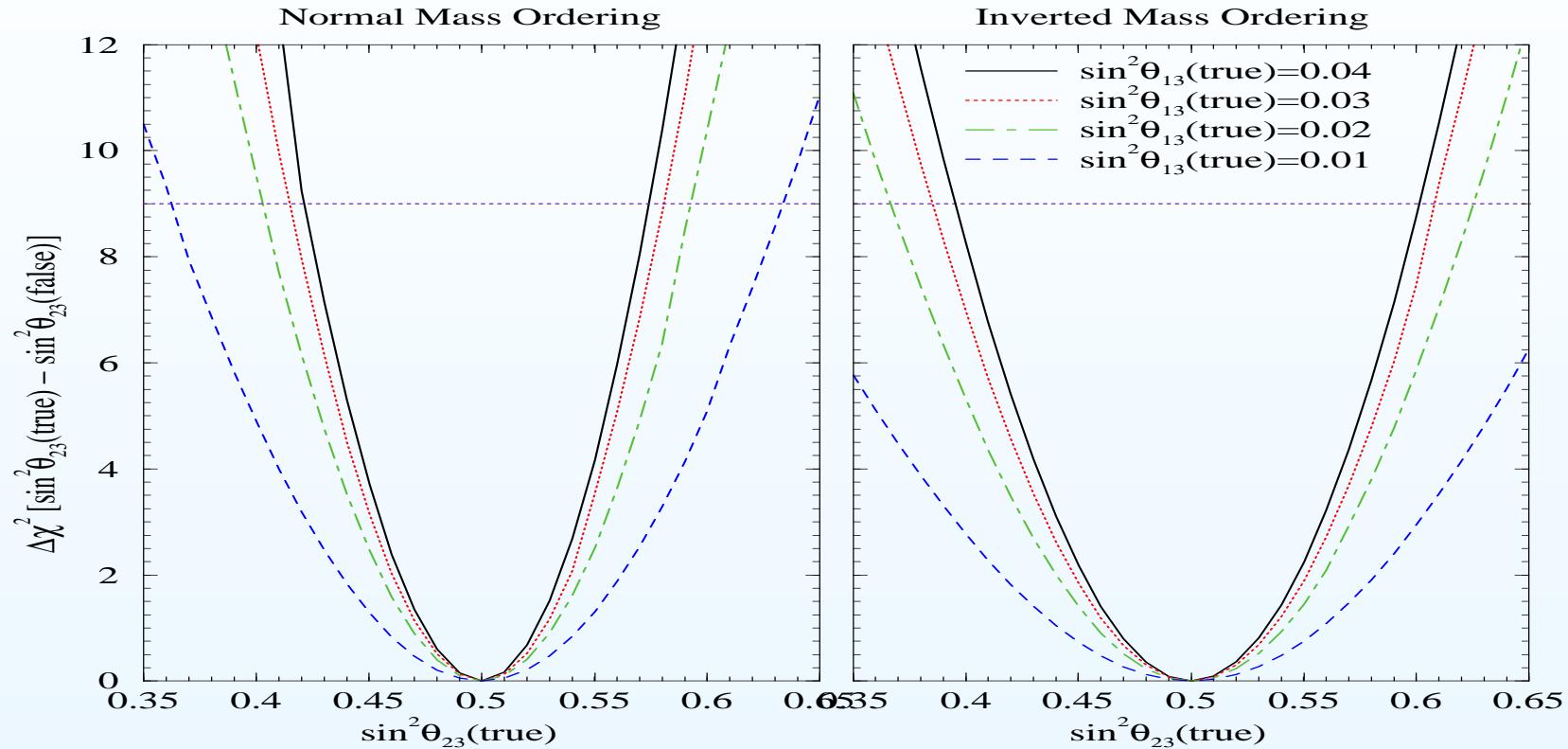




# Resolving the $\theta_{23}$ Octant Ambiguity



# Resolving the $\theta_{23}$ Octant Ambiguity with INO-ICAL



1 MTonyr

S.C and P. Roy hep-ph/0509197

- $\sin^2\theta_{23}(\text{false})$  can be excluded at  $3\sigma$  if:

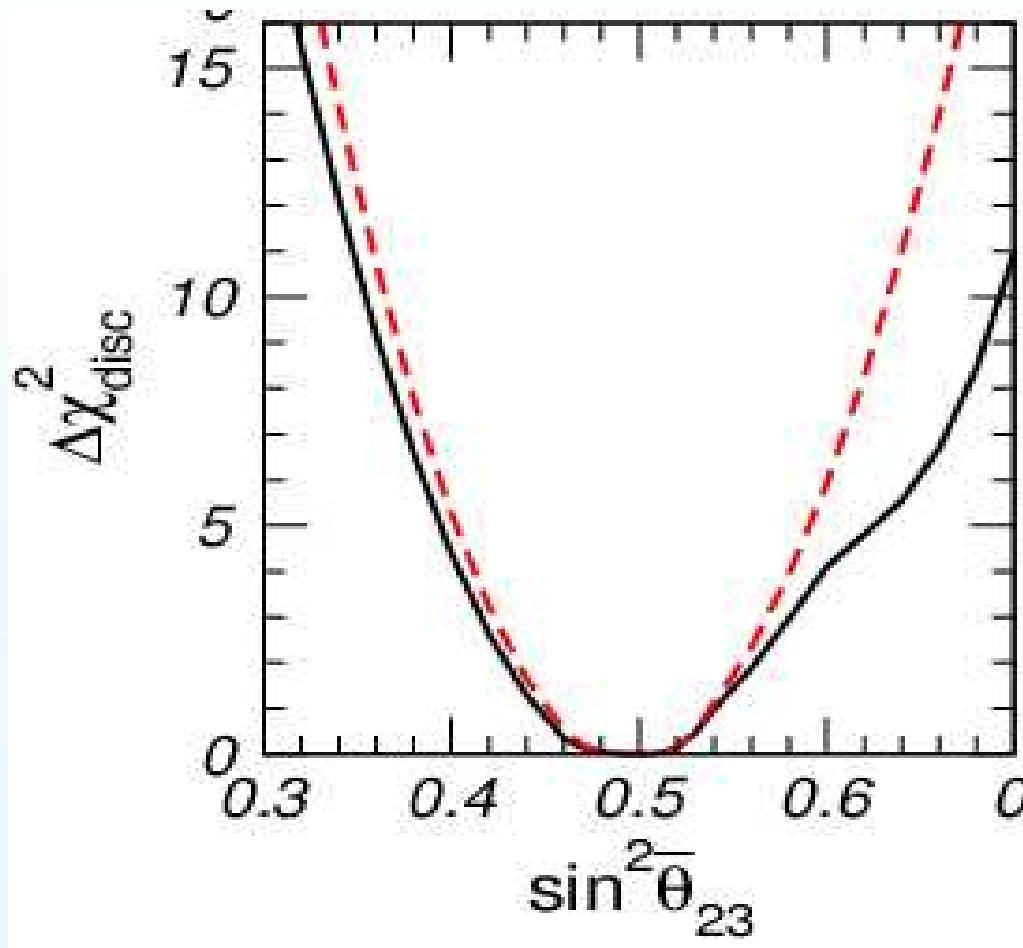
$\sin^2\theta_{23}(\text{true}) < 0.402$  or  $> 0.592$  for  $\sin^2\theta_{13}(\text{true}) = 0.02$ ,

$\sin^2\theta_{23}(\text{true}) < 0.421$  or  $> 0.573$  for  $\sin^2\theta_{13}(\text{true}) = 0.04$ .





# Resolving the $\theta_{23}$ Octant Ambiguity with SK50



Gonzalez-Garcia et al, hep-ph/0408170

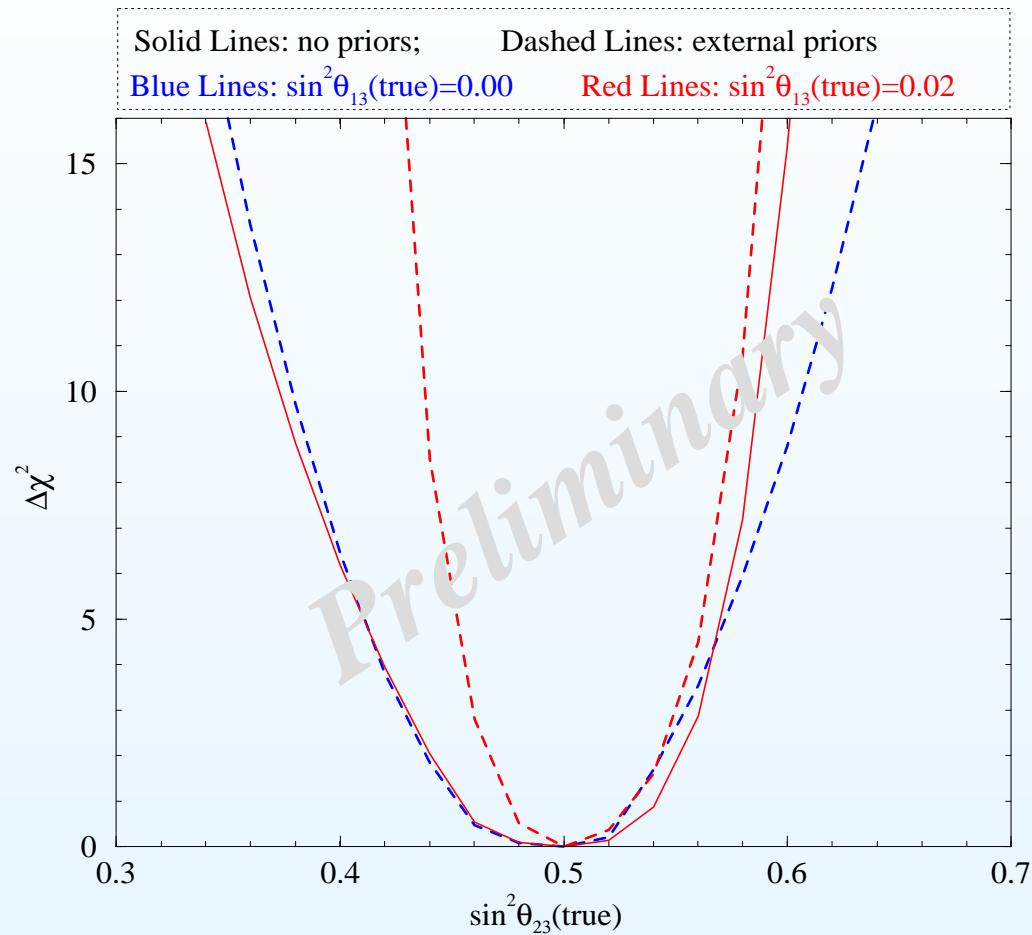
- $\sin^2 \theta_{23}$  (false) can be excluded at  $3\sigma$  if:

$$\sin^2 \theta_{23}(\text{true}) < 0.36 \text{ or } > 0.62 \text{ for } \sin^2 \theta_{13}(\text{true}) = 0.00.$$





# Resolving the $\theta_{23}$ Octant Ambiguity with SK50



- $\sin^2 \theta_{23}(\text{false})$  can be excluded at  $3\sigma$  if:

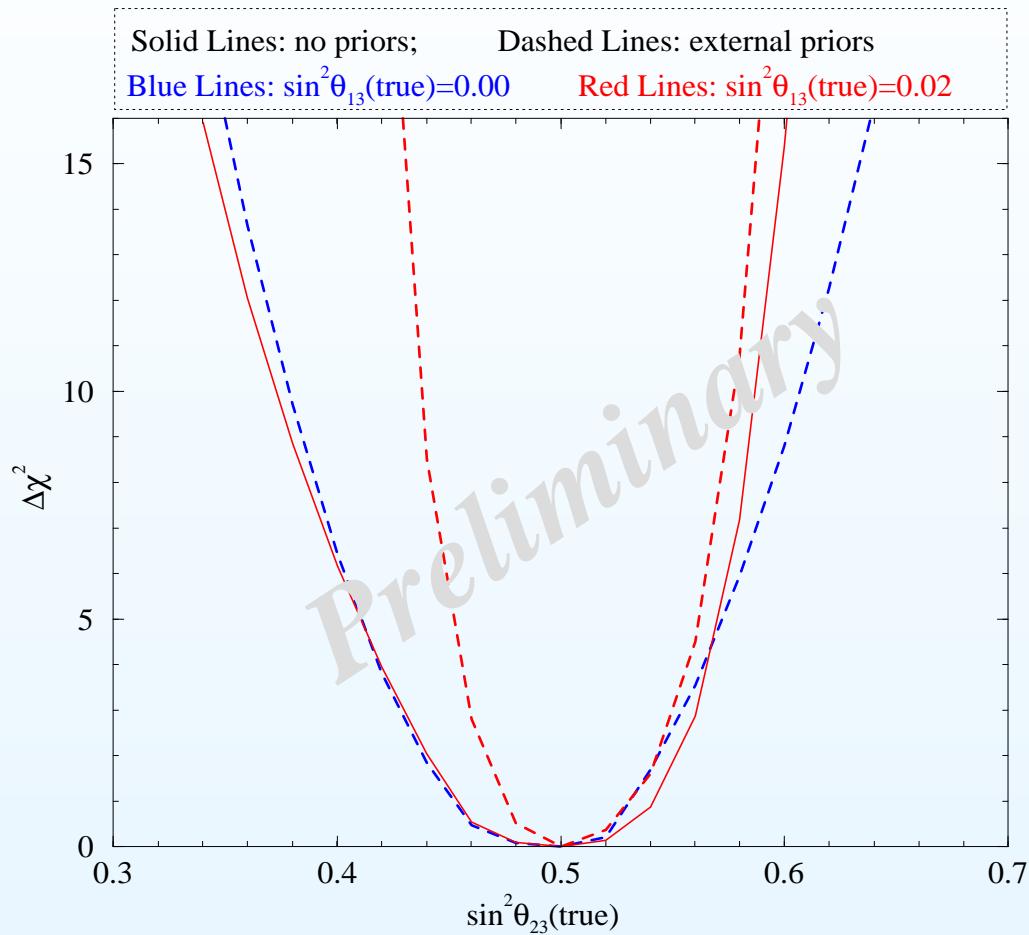
$\sin^2 \theta_{23}(\text{true}) < 0.384$  or  $> 0.601$  for  $\sin^2 \theta_{13}(\text{true}) = 0.00$ .

$\sin^2 \theta_{23}(\text{true}) < 0.438$  or  $> 0.574$  for  $\sin^2 \theta_{13}(\text{true}) = 0.02$ .





# Resolving the $\theta_{23}$ Octant Ambiguity with SK50



Sensitivity to octant of  $\theta_{23}$  improves remarkably as  $\theta_{13}$  increases from zero.

- $\sin^2 \theta_{23}(\text{false})$  can be excluded at  $3\sigma$  if:

$$\sin^2 \theta_{23}(\text{true}) < 0.384 \text{ or } > 0.601 \text{ for } \sin^2 \theta_{13}(\text{true}) = 0.00.$$

$$\sin^2 \theta_{23}(\text{true}) < 0.438 \text{ or } > 0.574 \text{ for } \sin^2 \theta_{13}(\text{true}) = 0.02.$$

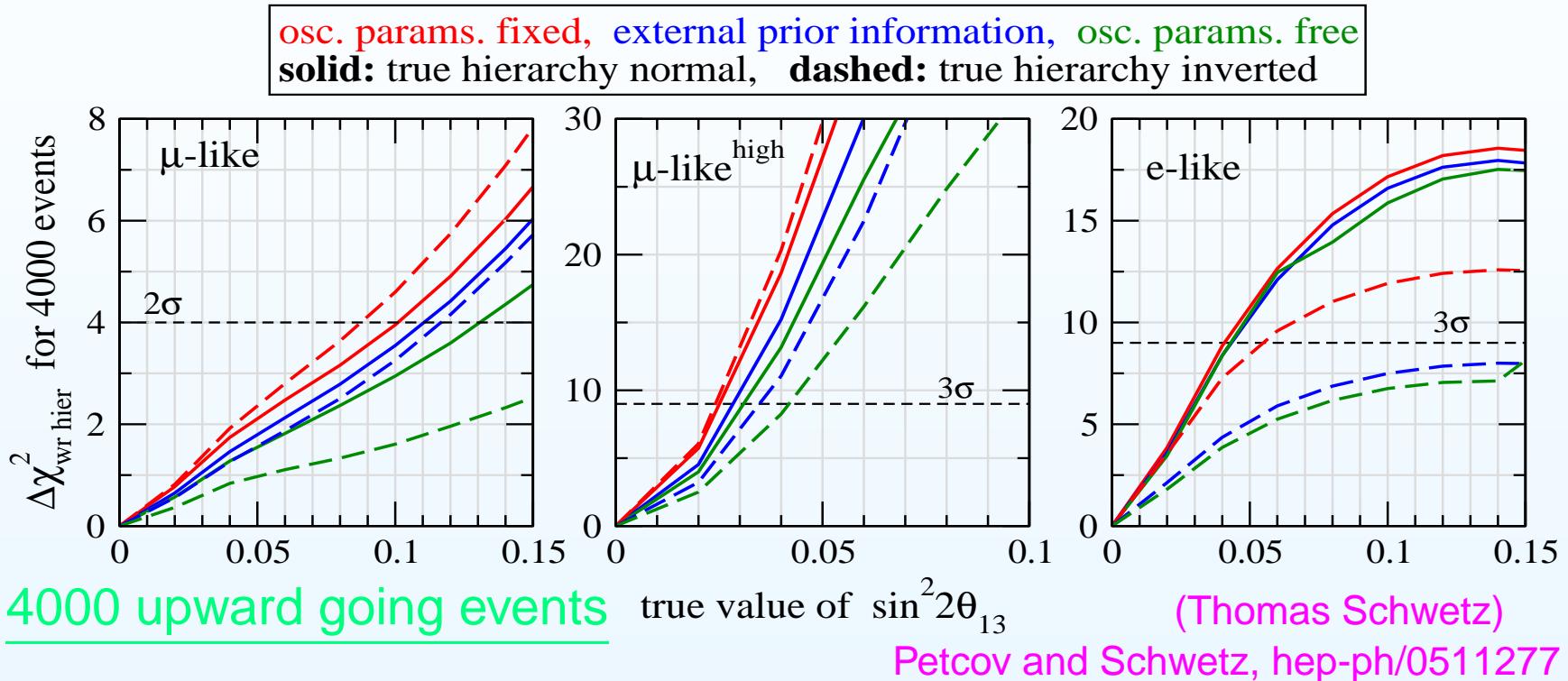




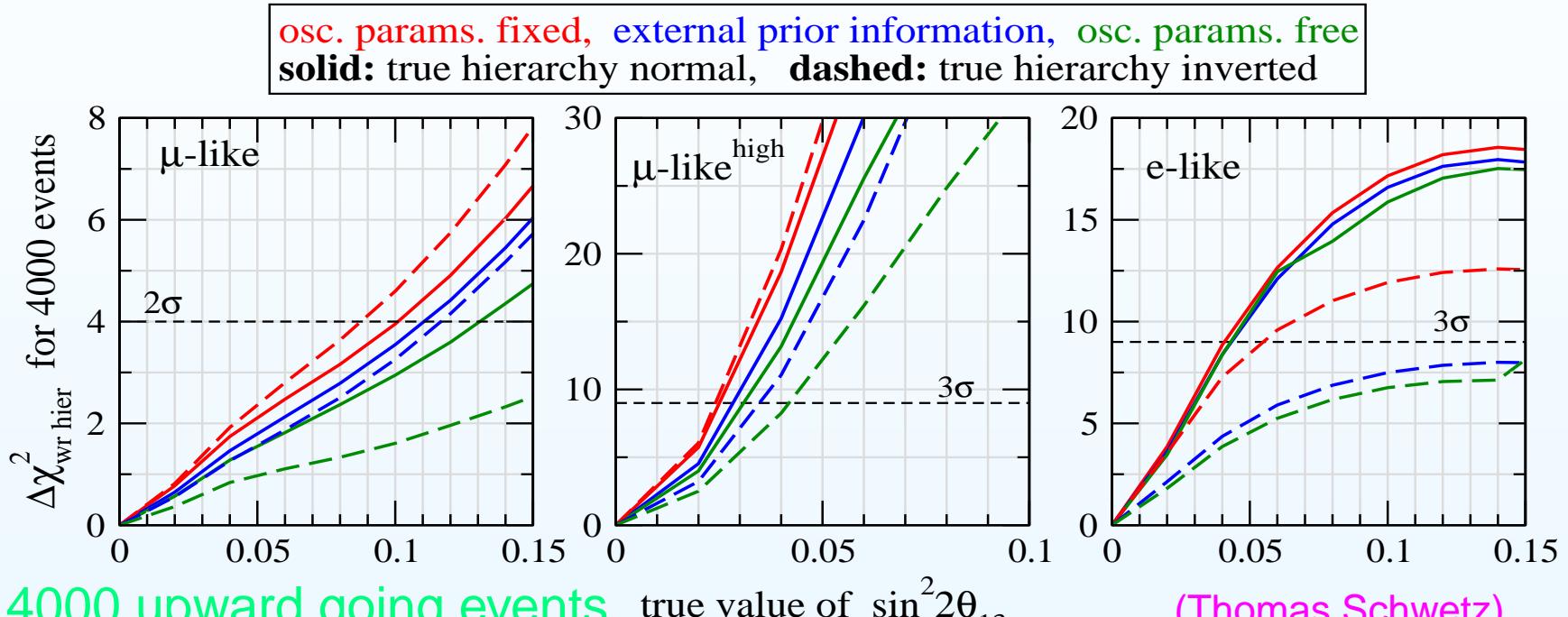
# Resolving the $sgn(\Delta m_{31}^2)$ Ambiguity



# Resolving the $sgn(\Delta m_{31}^2)$ Ambiguity with INO-ICAL

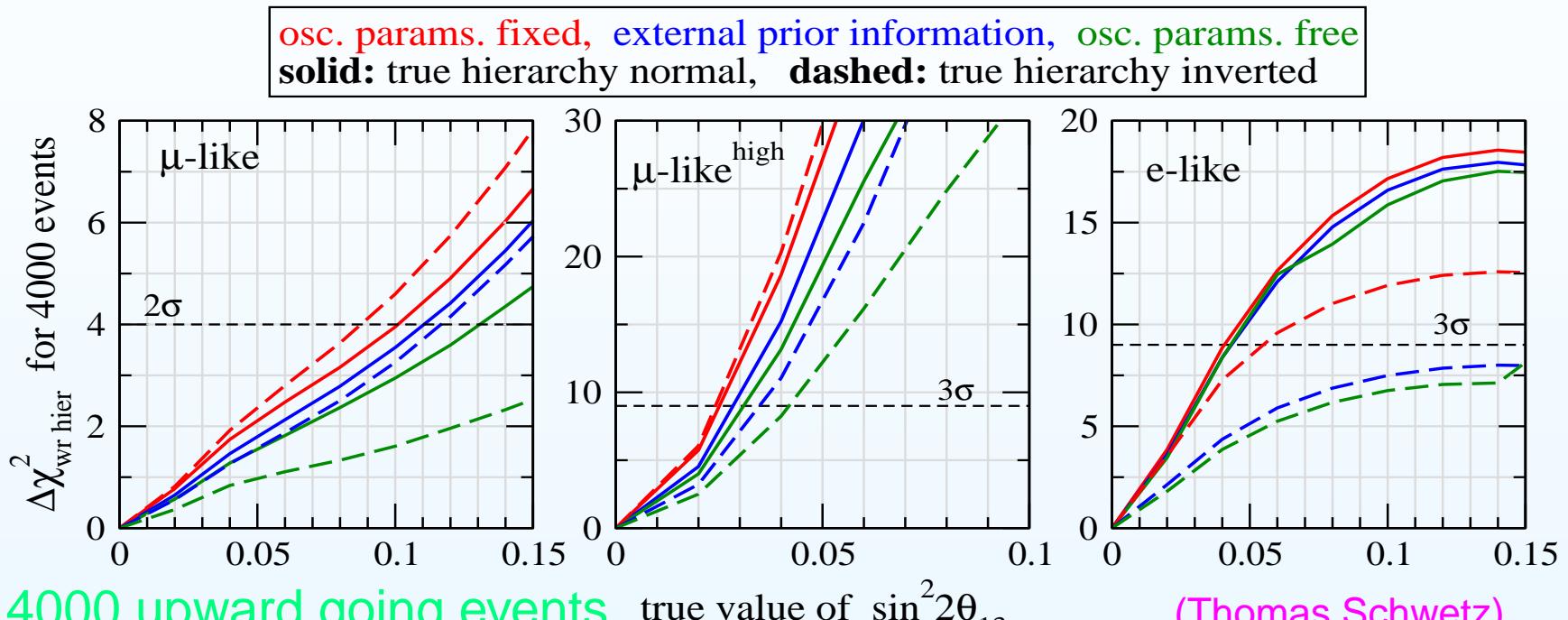


# Resolving the $\text{sgn}(\Delta m_{31}^2)$ Ambiguity with INO-ICAL



- The wrong hierarchy can be ruled out at  $2\sigma$  with 4000 upward going events for  $\sin^2 2\theta_{13} = 0.1$  ( $\sin^2 \theta_{13} = 0.026$ ) and  $\sin^2 \theta_{23} = 0.5$

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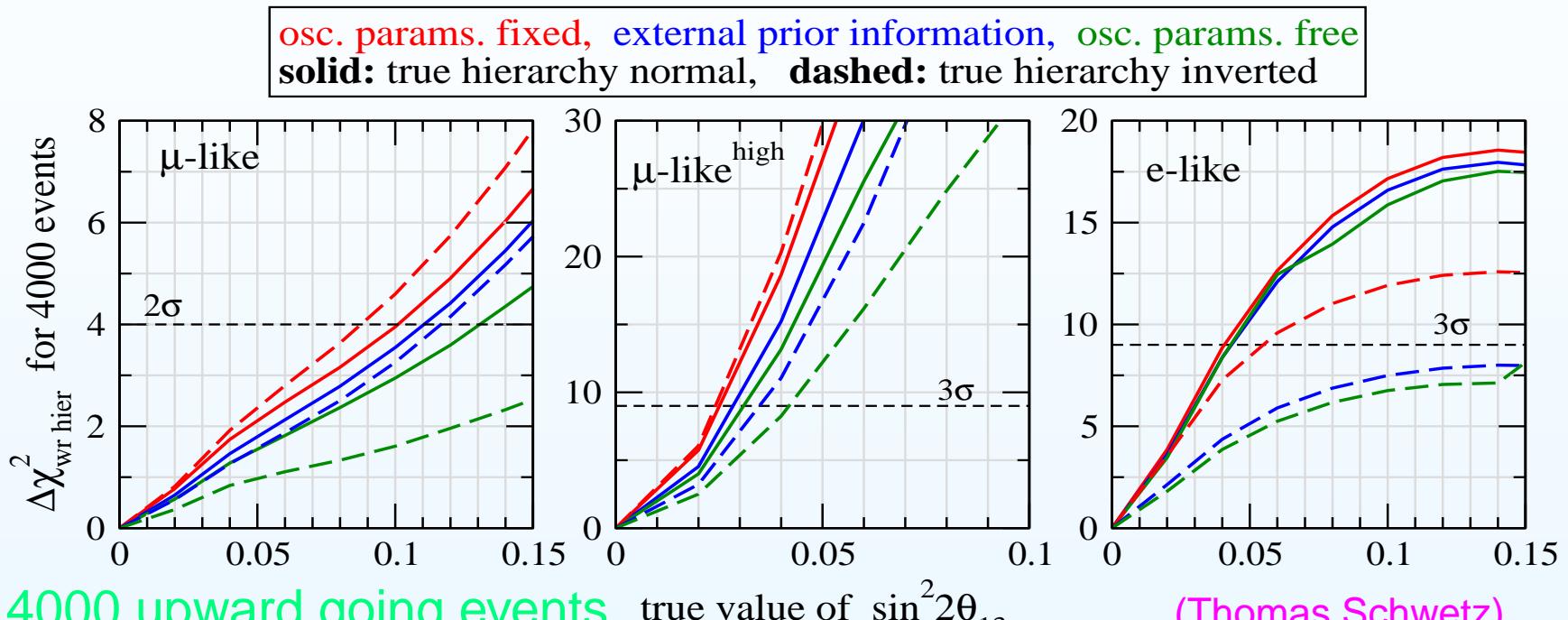
Polamares-Ruiz,Petcov (2003)

Indumathi, Murthy (2004)

Ghoshal,Gandhi,Goswami,Mehta,UmaSankar (2004)



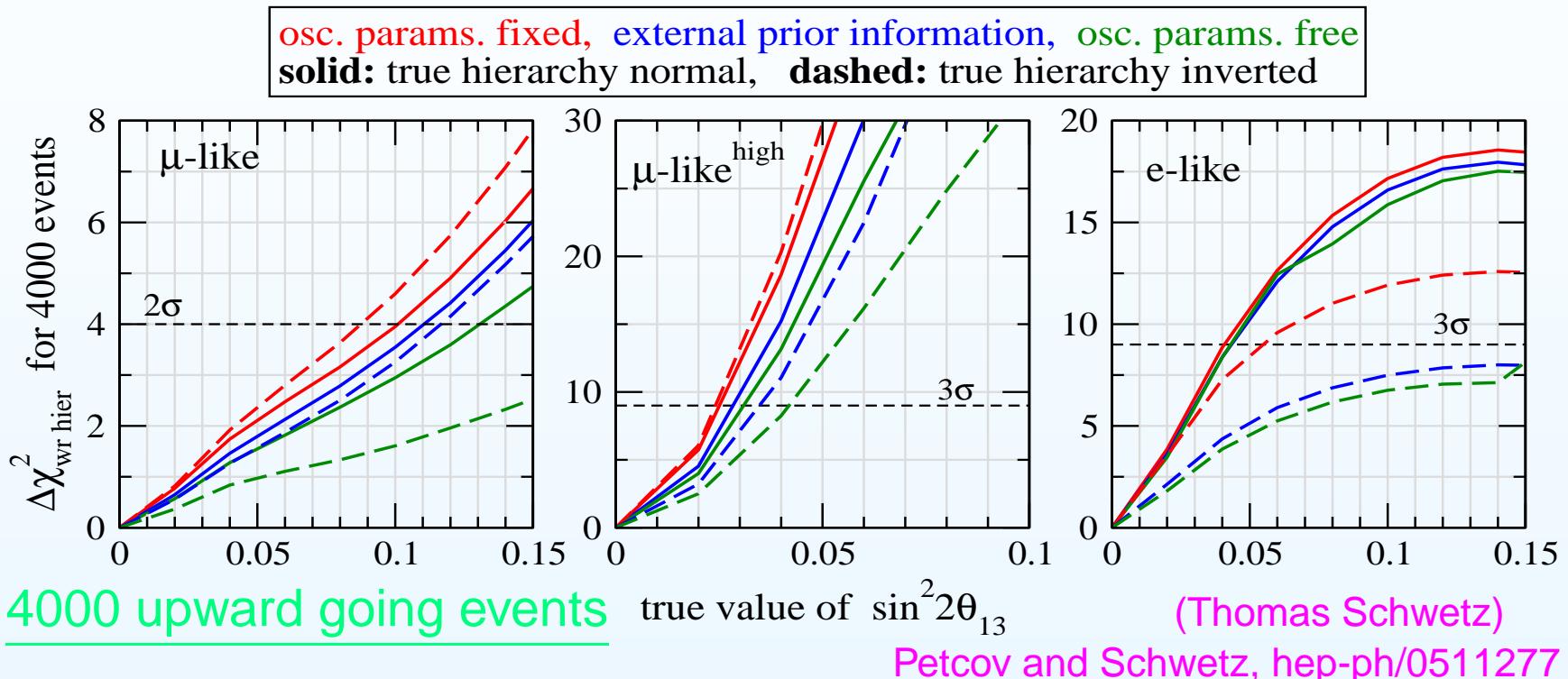
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- Sensitivity increases with  $E$  and  $L$  resolution



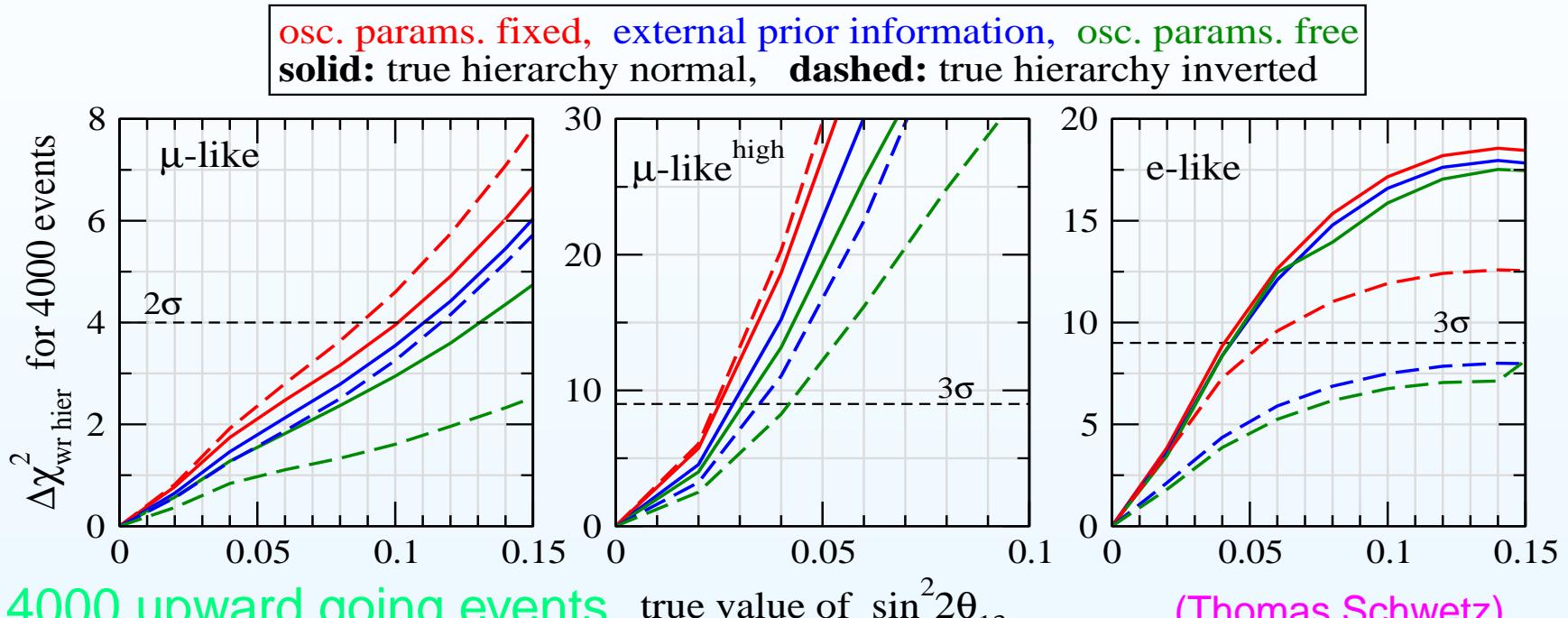
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- Sensitivity increases if it were possible to detect electrons



# Resolving the $sgn(\Delta m_{31}^2)$ Ambiguity with INO-ICAL



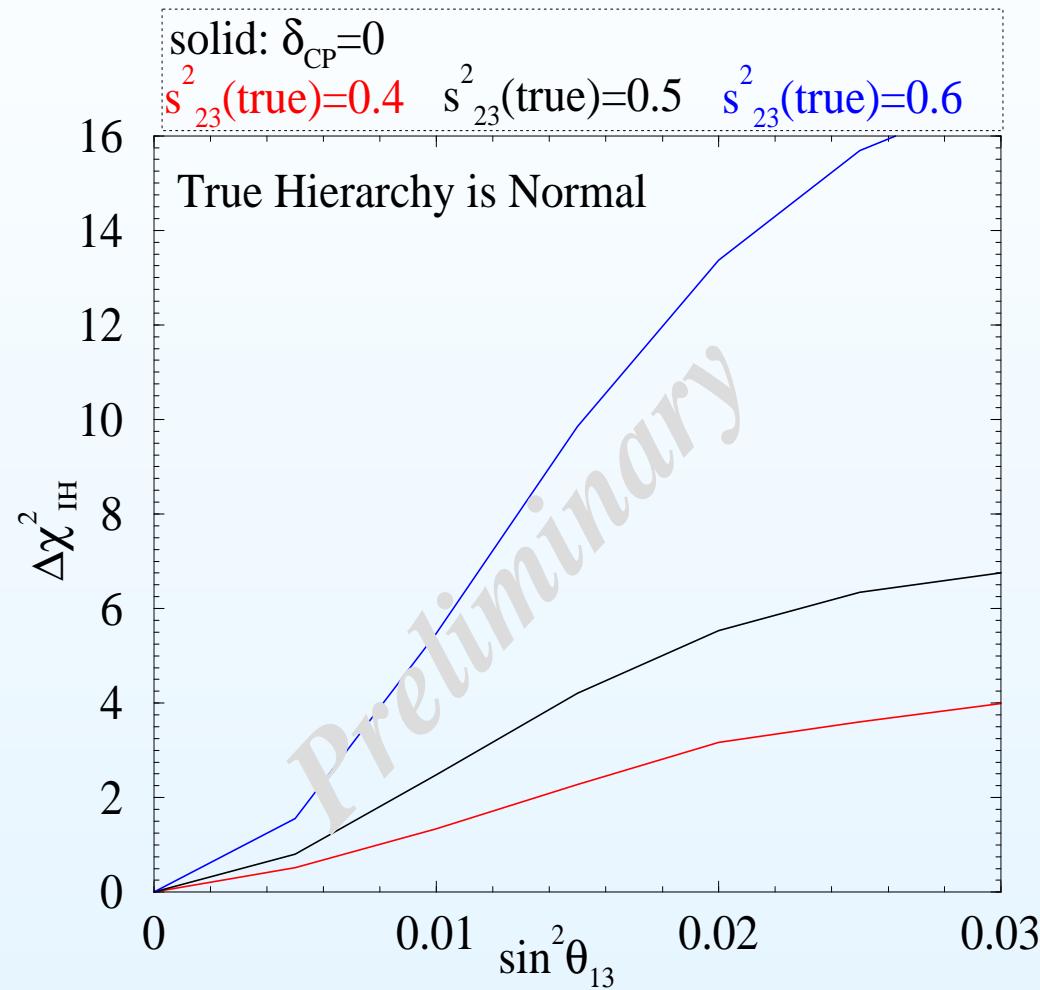
Petcov and Schwetz, hep-ph/0511277

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- Sensitivity increases with  $\sin^2 \theta_{23}$



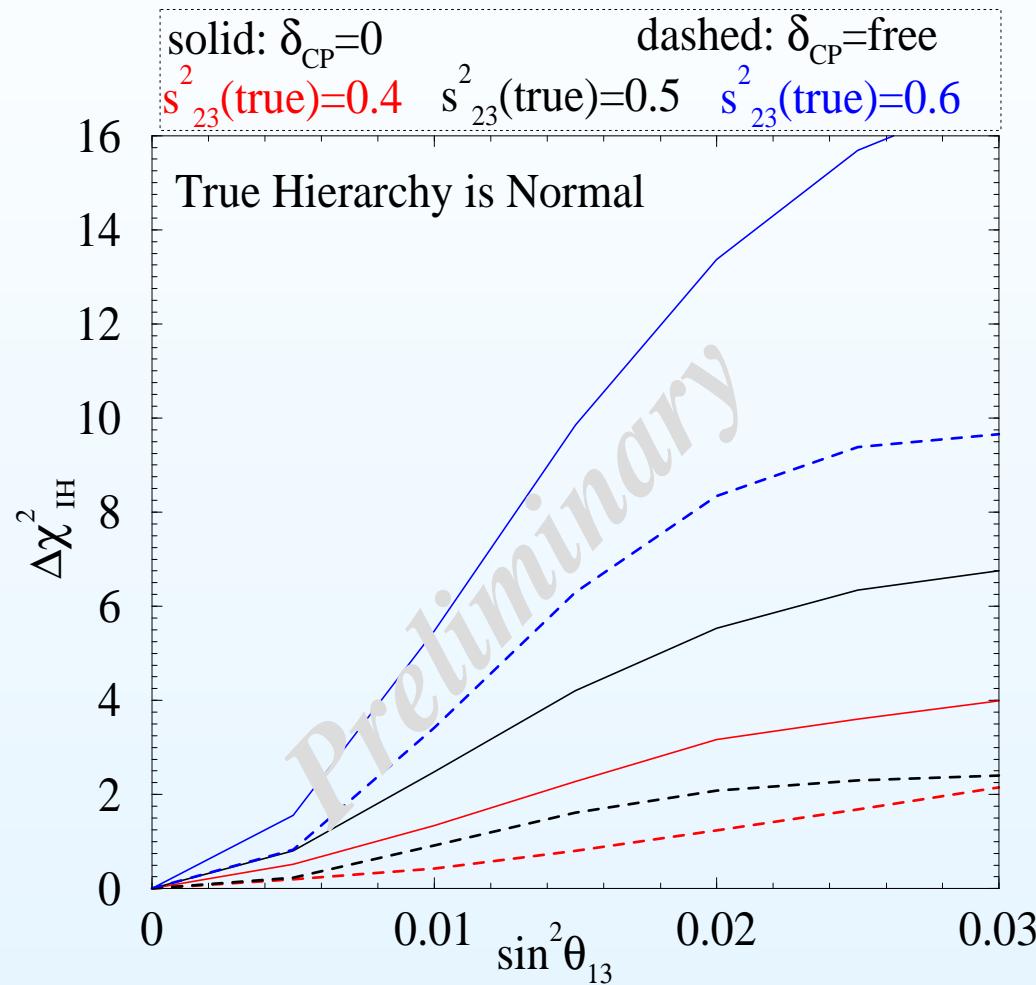


# Resolving the $sgn(\Delta m_{31}^2)$ Ambiguity with SK50





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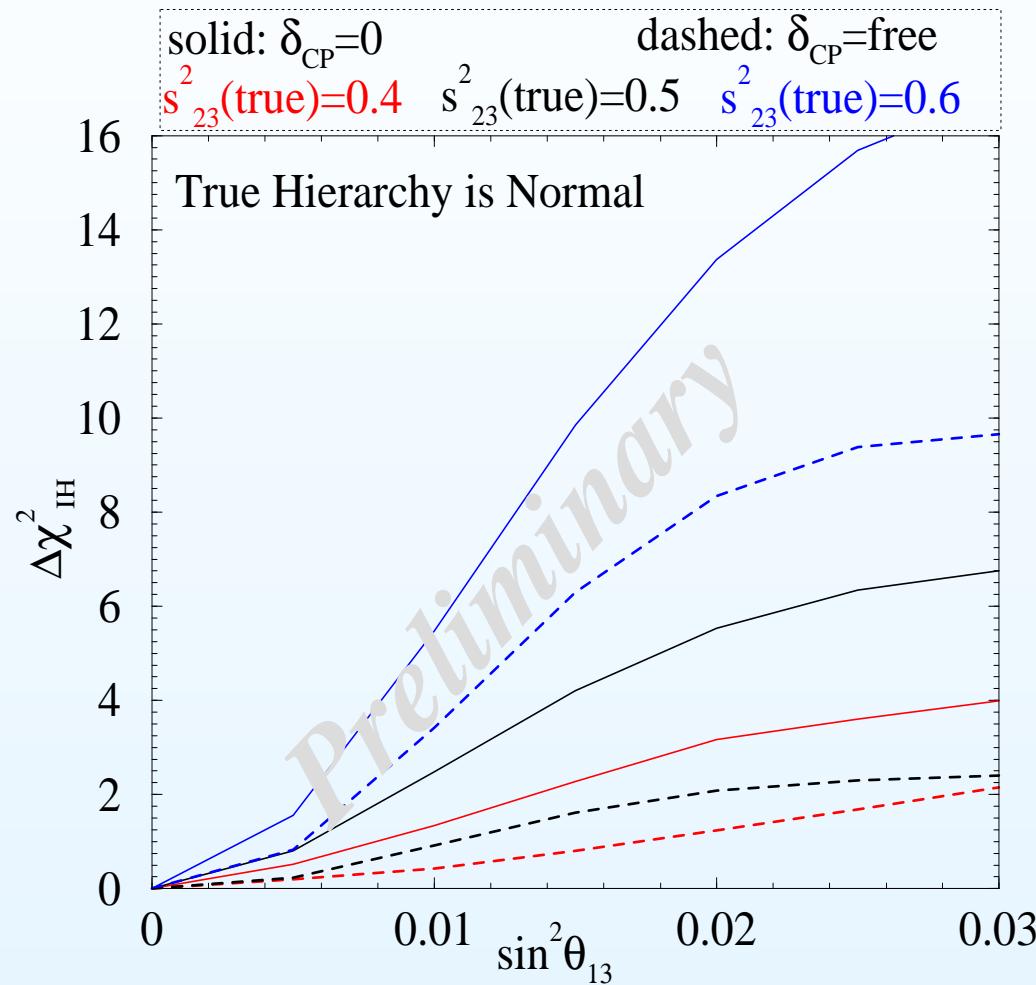


- Sensitivity drops appreciably due to  $\delta_{CP}$





# Resolving the $sgn(\Delta m_{31}^2)$ Ambiguity with SK50



- Resolving param degen:  
T2K+ATM:[hep-ph/0501037](#)
- $\beta$ beams+ATM:[hep-ph/0603172](#)

- Sensitivity drops appreciably due to  $\delta_{CP}$





# Searching for New Physics





# Searching for New Physics

- Non-Standard neutrino-matter Interaction
- Violation of Equivalence Principle
- Lorentz Invariance Violation
- Violation of CPT Symmetry
- Neutrino Decay
- Quantum Decoherence

(This list is not exhaustive.)



# Searching for New Physics in INO-ICAL/SK50 like Expts

- Non-Standard neutrino-matter Interaction
  - Violation of Equivalence Principle
  - Lorentz Invariance Violation
  - Violation of CPT Symmetry
  - Neutrino Decay
  - Quantum Decoherence
- 
- Each one has a distinctive  $L/E$  behavior
  - Oscillations go linearly as  $L/E$
  - Atmospheric neutrinos have a very wide range of  $L/E$
  - This  $L/E$  data can be used to probe new physics – INO-ICAL
  - Comparison of contained events and upward going muons in water Cerenkov detectors can also be used



# Searching for New Physics with Neutrino Telescopes

- Neutrino Telescopes have atmospheric  $\nu$ 's as background



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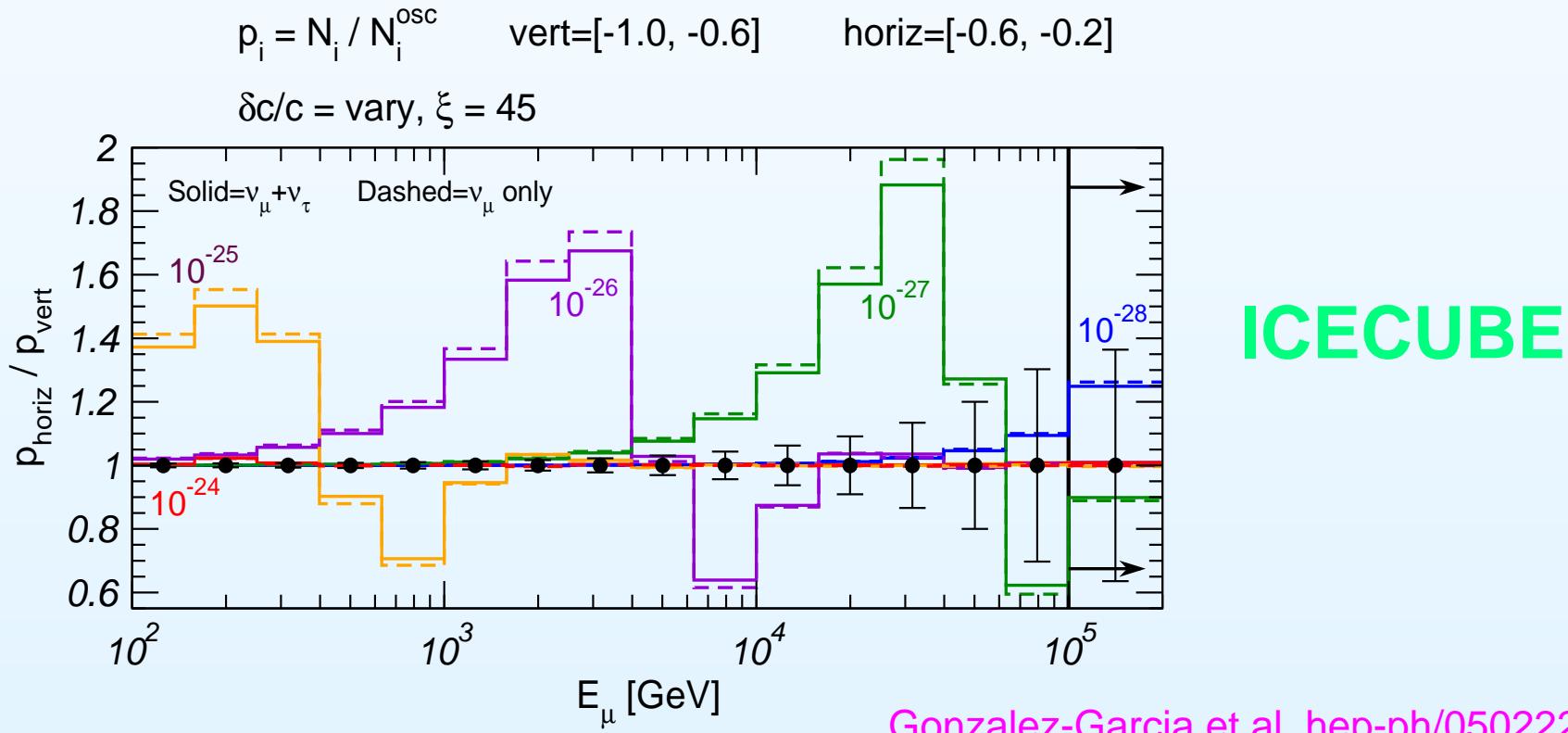
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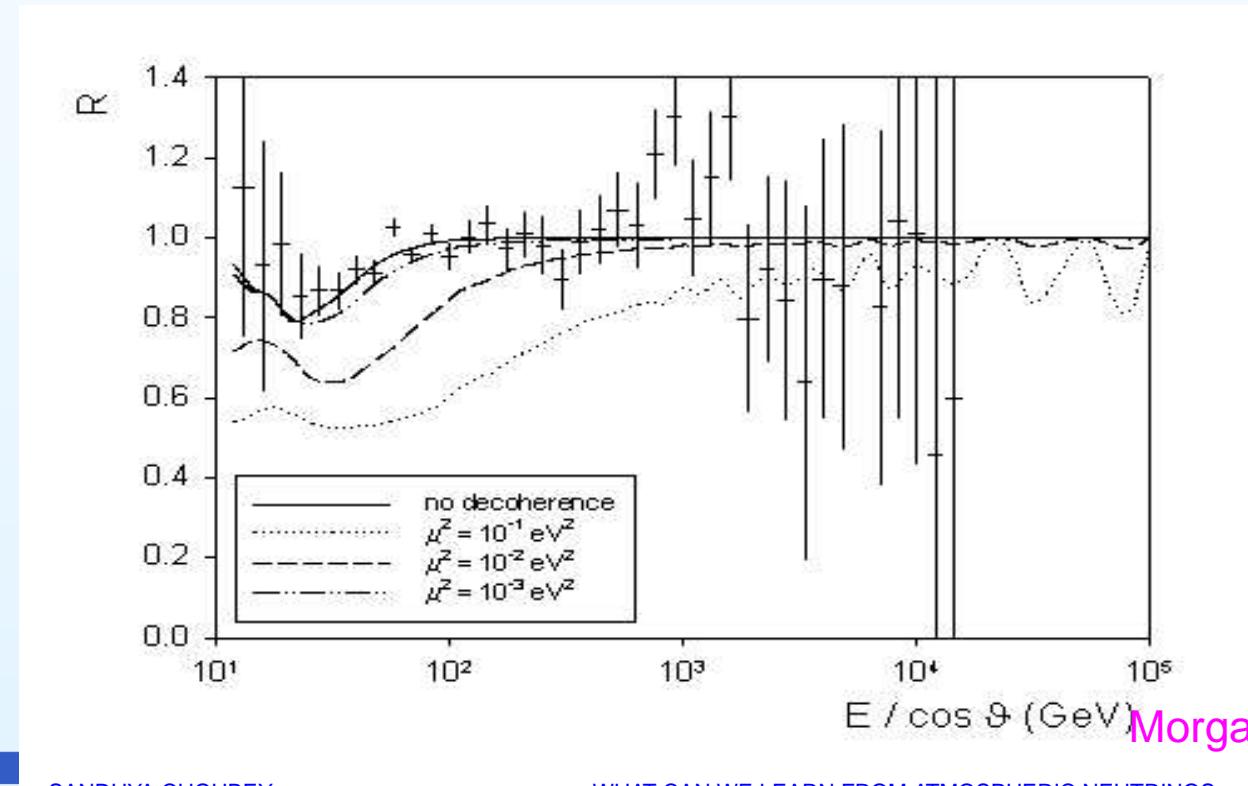
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ANTARES

Morgan et al, astro-ph/0412618





# Conclusions





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# Conclusions

- Neutrino mass hierarchy can be determined at  $2\sigma$  at 4000 upward going events at INO-ICAL if  $\sin^2 \theta_{13}(\text{true}) = 0.026$  and  $\sin^2 \theta_{23}(\text{true}) = 0.5$





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**Thank You!!**

