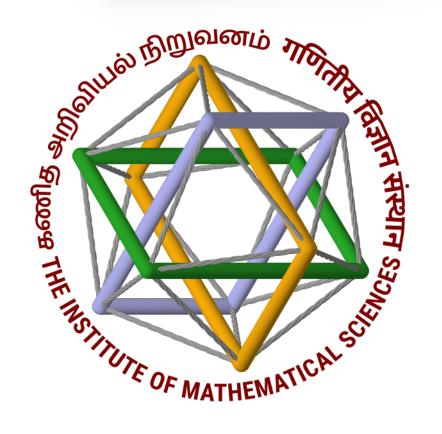
Lattice QCD Study of Doubly Heavy Tetraquarks

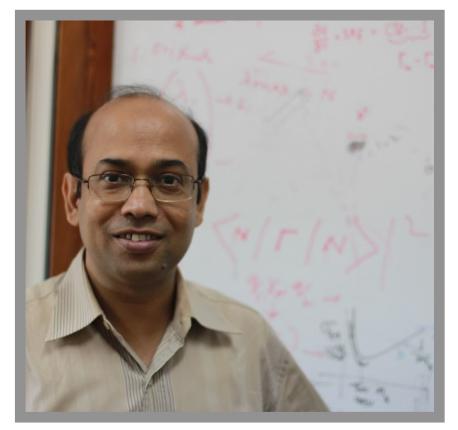


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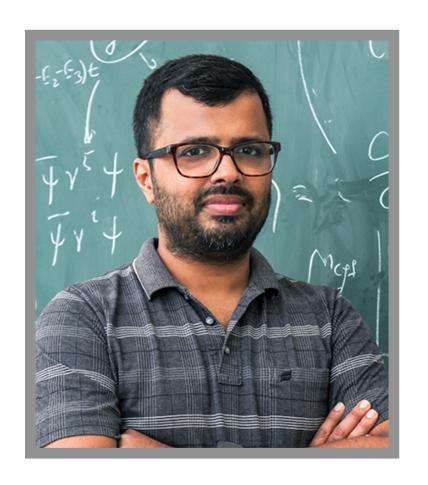




31 Jan 2025



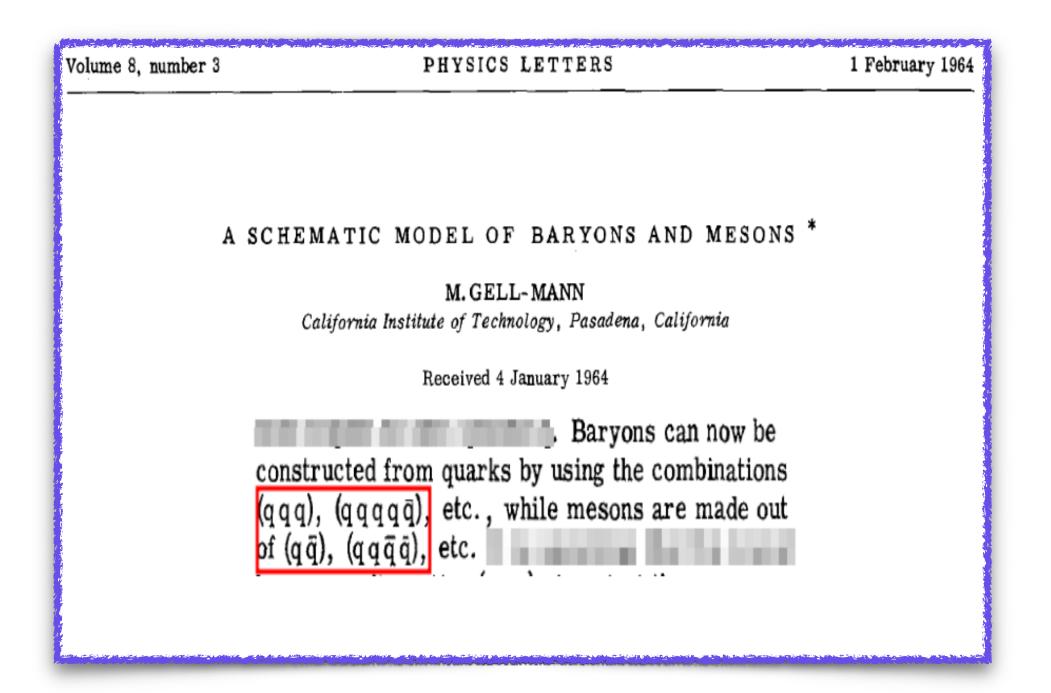




M. Padmanath(IMSc)



Introduction and Motivation



PHYSICAL REVIEW D

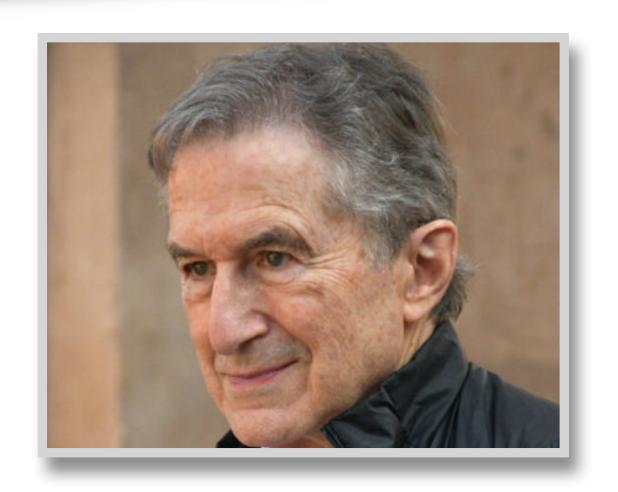
VOLUME 15, NUMBER 1

1 JANUARY 1977

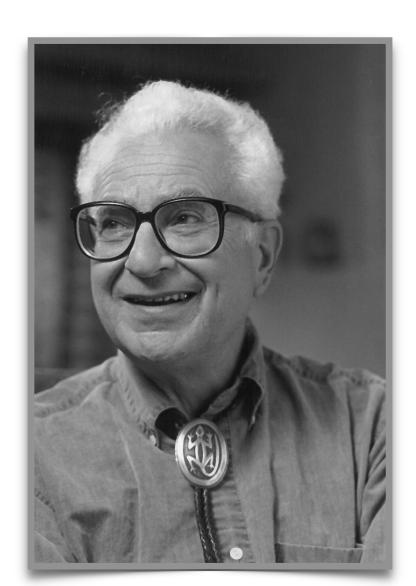
Multiquark hadrons. I. Phenomenology of $Q^2\bar{Q}^2$ mesons*

R. J. Jaffe[†]

Stanford Linear Accelerator Center, Stanford University, Stanford, California 94305 and Laboratory for Nuclear Science and Department of Physics, Massachusetts Institute of Technology, Cambridge, Massachusetts 02139 (Received 15 July 1976)

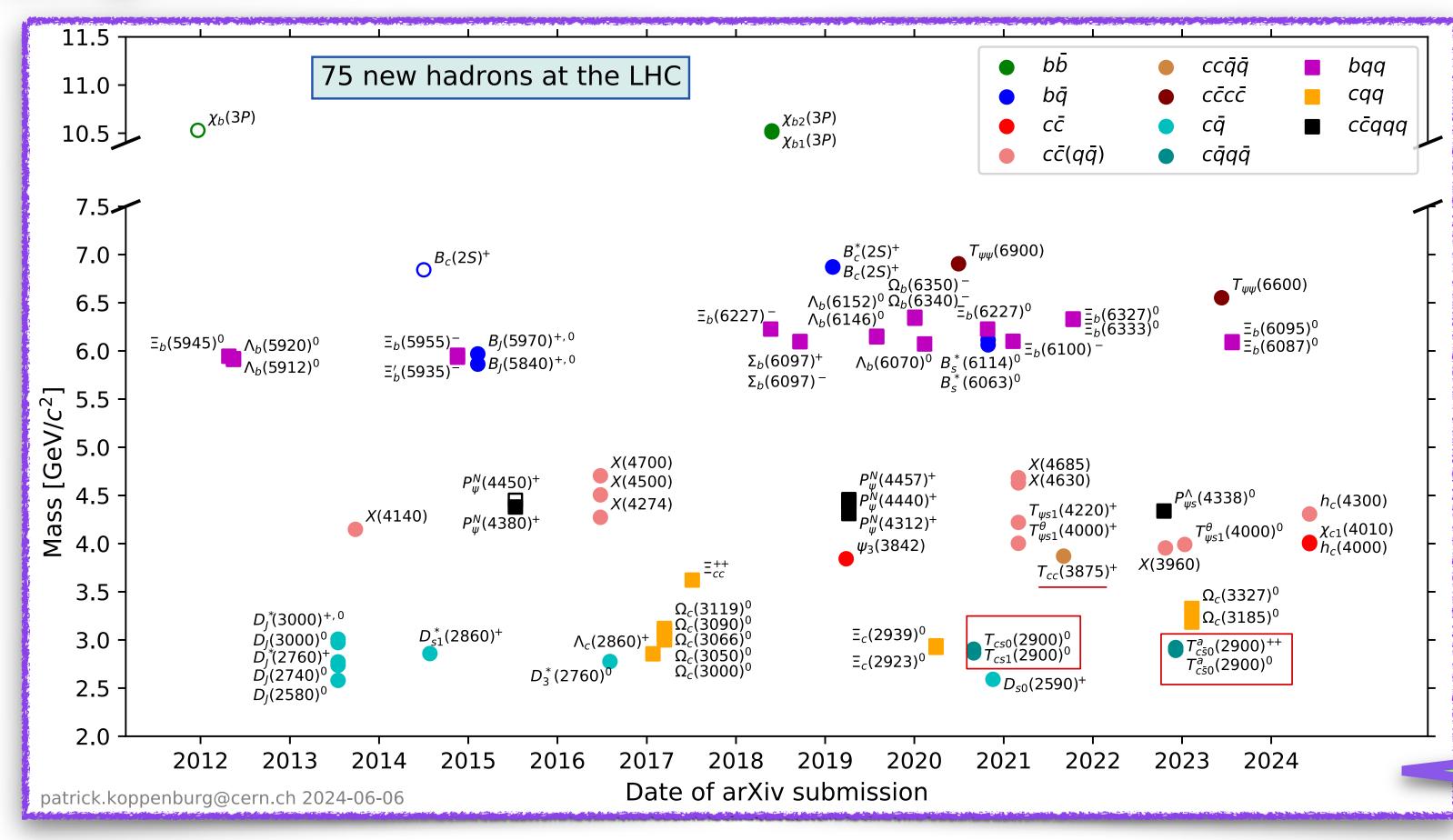


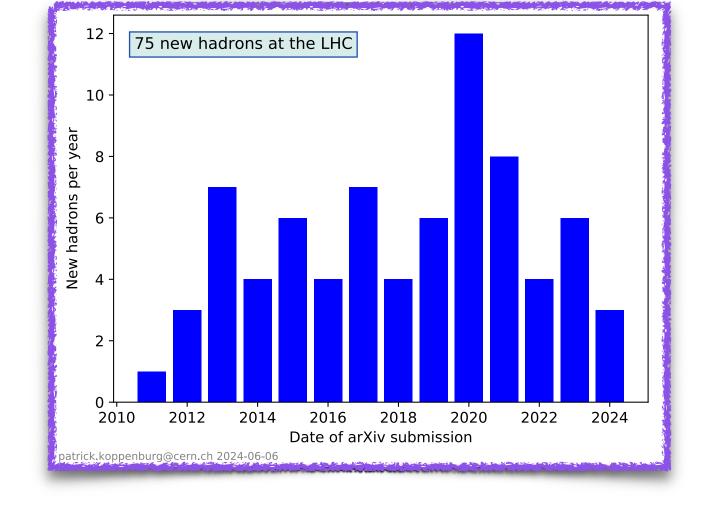
- Murray Gellmann indicated the possibility of multiquark systems.
- Jaffe described it as color neutral states of diquark and antidiquark.
- Currently known as Tetraquarks and Pentaquarks.



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Experimental Results in LHC





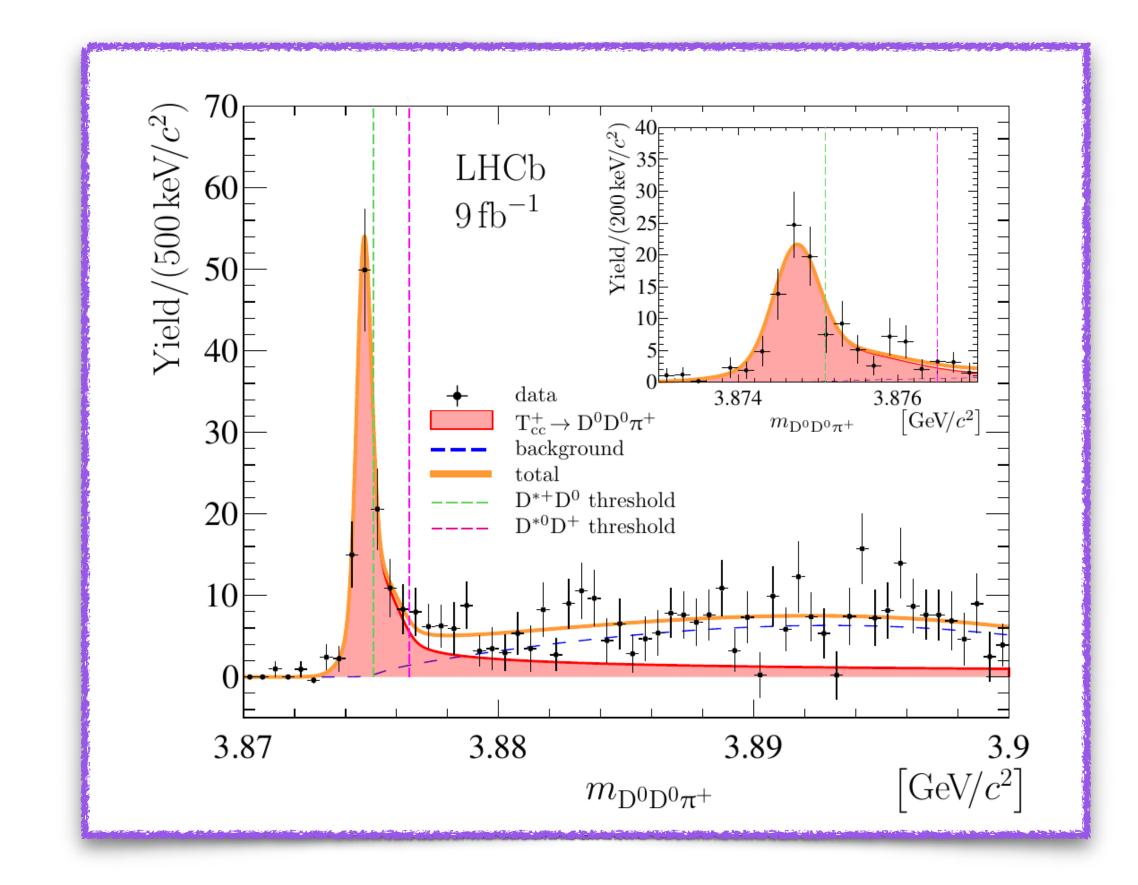
Patrick's Webpage:hhtps://www.nikhef.nl/pkoppenb/

Other research facilities like Belle, BES-III etc. have active spectroscopy programs.

Particles discovered in the last decade including conventional heavy hadrons, open flavor mesons, exotic particles

T_{cc} discovery at LHC

- In 2021, LHCb made headlines by discovering the longest-lived exotic state ever observed.
- Many more exotic tetraquark discovered recently e.g. T_{cs} , $T_{c\bar{s}}$, Z_c and so on. Scope for T_{bc} , T_{bs} in near future.



Nature phys: https://rdcu.be/dNMRV
Arxiv:2109.01038

$$\delta M = M_{T_{cc^{+}}} - (M_{D^{*+}} + M_{D^{0}})$$

$$\delta M_{pole} = -360 \pm 40 \binom{+4}{-0} keV/c^{2}$$

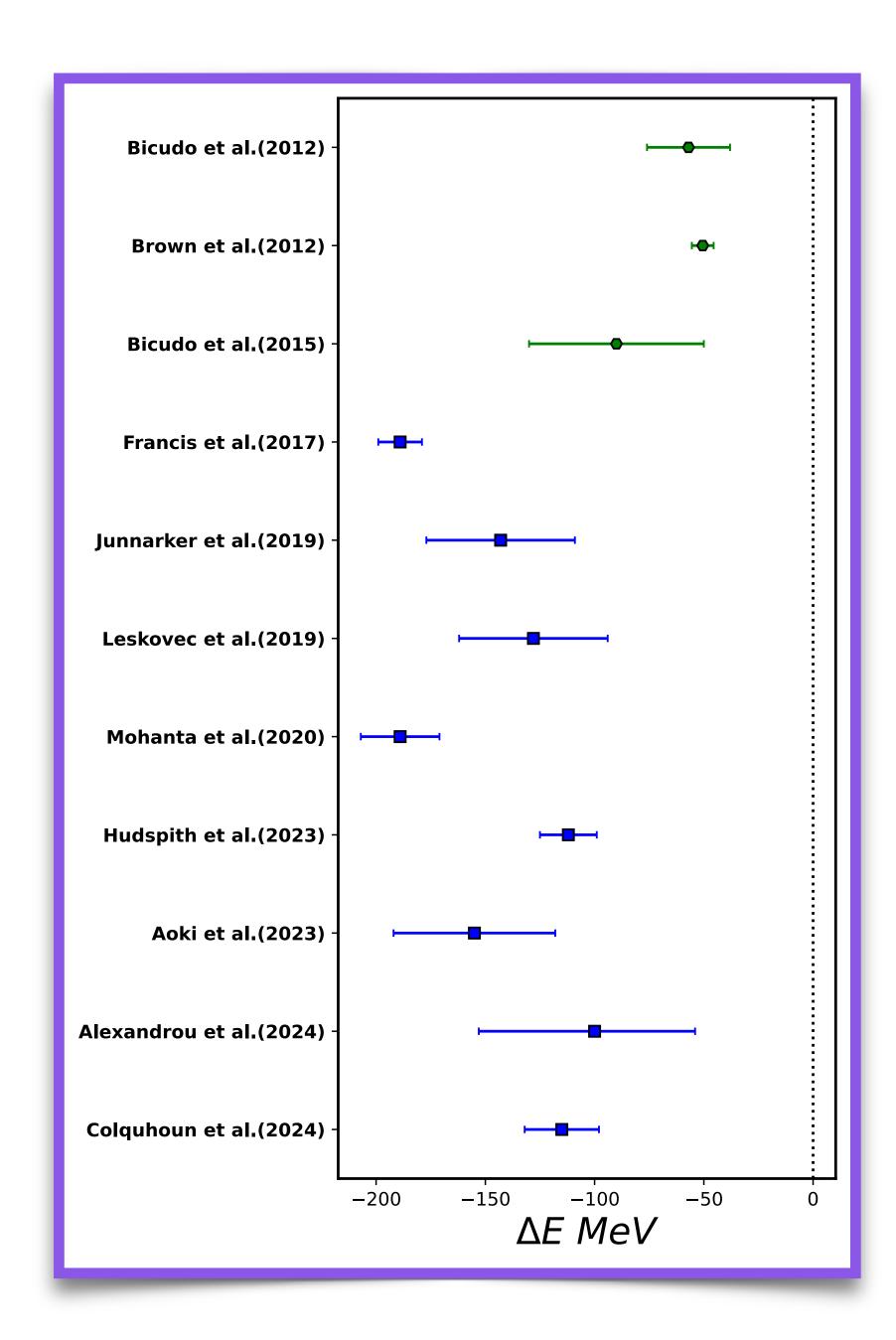
$$\Gamma_{pole} = 48 \pm 2 \binom{+00}{-14} KeV$$

Long History of T_{bb}

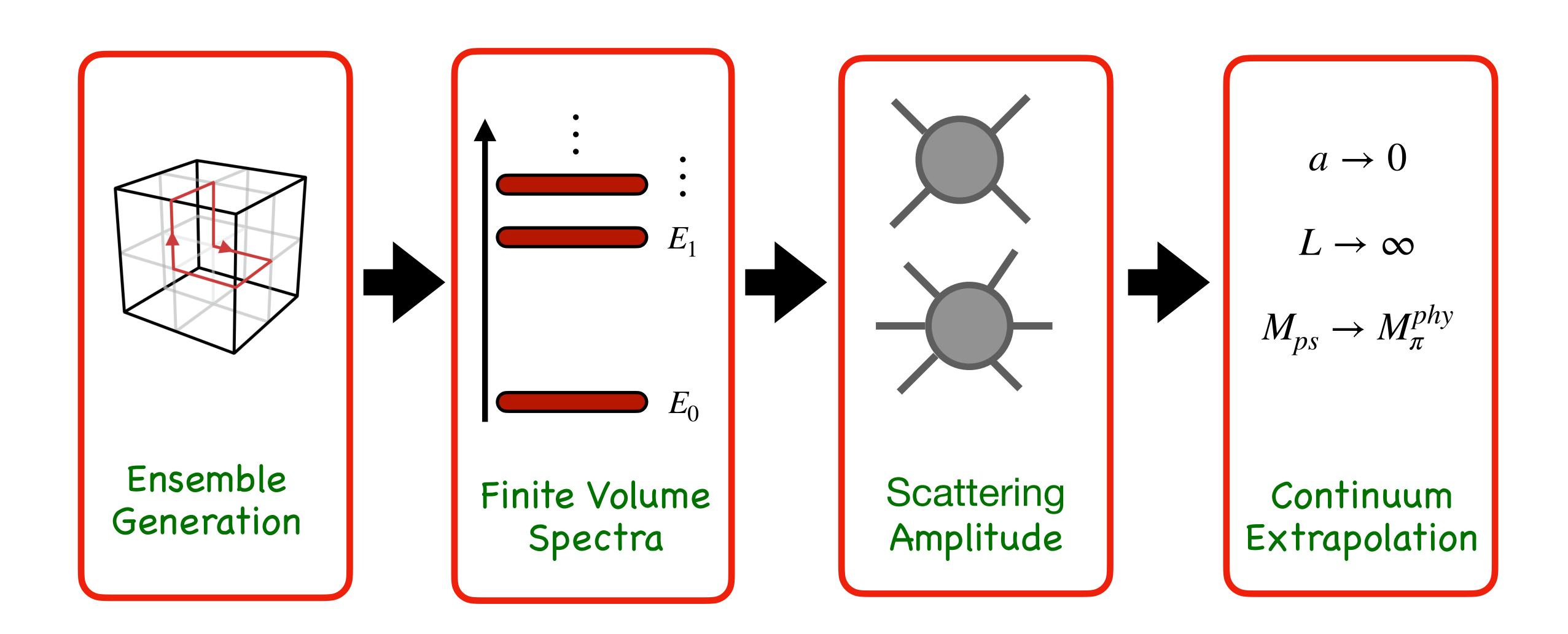
- ullet Phenomenological calculation of T_{bb} can be trace back to the early 80's.
- Prediction of deeply bound state in the heavy quark limit.

Nucl.Phys.B 399 (1993)

- Results from various phenomenological studies suggest possibility of deeply bound state.
- ullet Previous lattice calculations on $bb\bar{u}d\ I=0$ shows deep bound state upto systematics.
- \bullet T_{cc} lattice results matches with that of the experimental results as pion mass decreases.



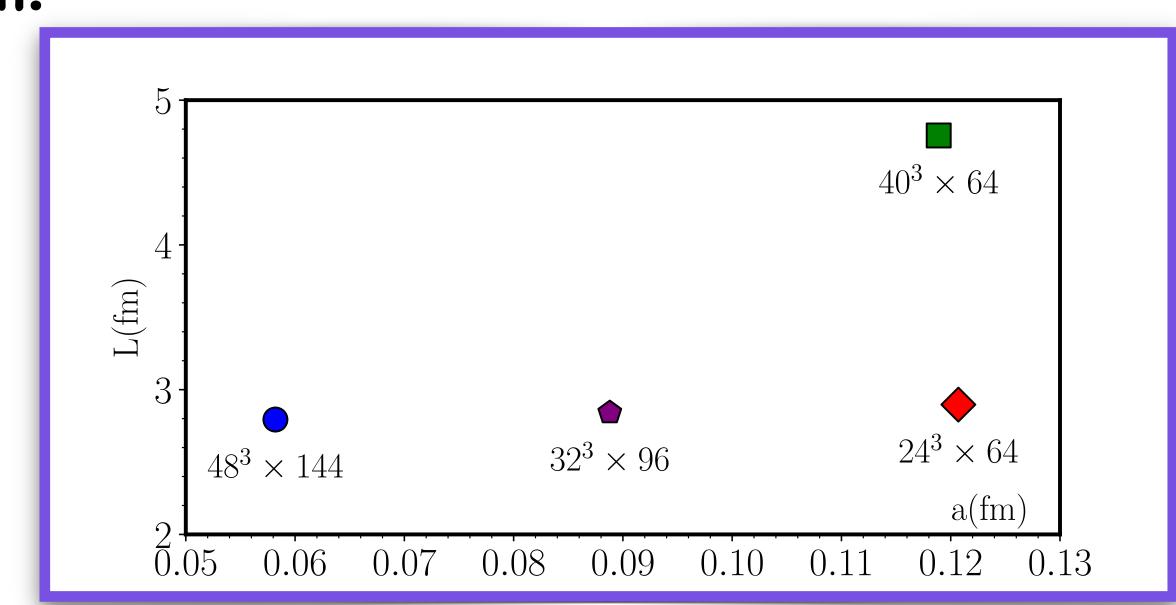
Hadron Spectroscopy in a Nutshell



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Lattice Setup

- ullet We are interested in doubly bottom tetra quarks $bb\bar{u}\bar{d}$ with $I(J^P)=0(1^+)$.
- ullet Worked with 4 MILC ensembles with $N_{\!f}=2+1+1$ using HISQ action.
- Ensembles were generated at unphysical light quarks and physical charm and strange quarks.
- Light quark propagators were constructed using Overlap action. For heavy(bottom) quark, we used NRQCD action.
- Wall-source smearing setup.
- Used multiple volumes, box-sink correlators to reduce systematic effects.



Extracting Finite Volume Spectrum

- To extract spectrum we need good interpolating operators.
- Here we are using two types of operators.

Meson-Meson:

$$\Phi_{\mathcal{M}_{RR}^*}(x) = [\bar{u}(x)\gamma_i b(x)][\bar{d}(x)\gamma_5 b(x)] - [\bar{u}(x)\gamma_5 b(x)][\bar{d}(x)\gamma_i b(x)]$$

Diquark-antidiquark:

$$\Phi_{\mathcal{D}}(x) = \left[(\bar{u}(x)^T C \gamma_5 \bar{d}(x)) - (\bar{d}(x)^T C \gamma_5 \bar{u}(x)) \times (b^T(x) C \gamma_i b(x)) \right]$$

ullet Finite volume spectrum can be calculated using Euclidean $\mathscr{C}_{ij}(t)$, between $\Phi's$

$$\mathscr{C}_{ij}(t) = \left\langle \Phi_i(\mathbf{x}, t) \tilde{\Phi}_j^{\dagger}(0) \right\rangle$$

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Finite Volume Spectrum cont.

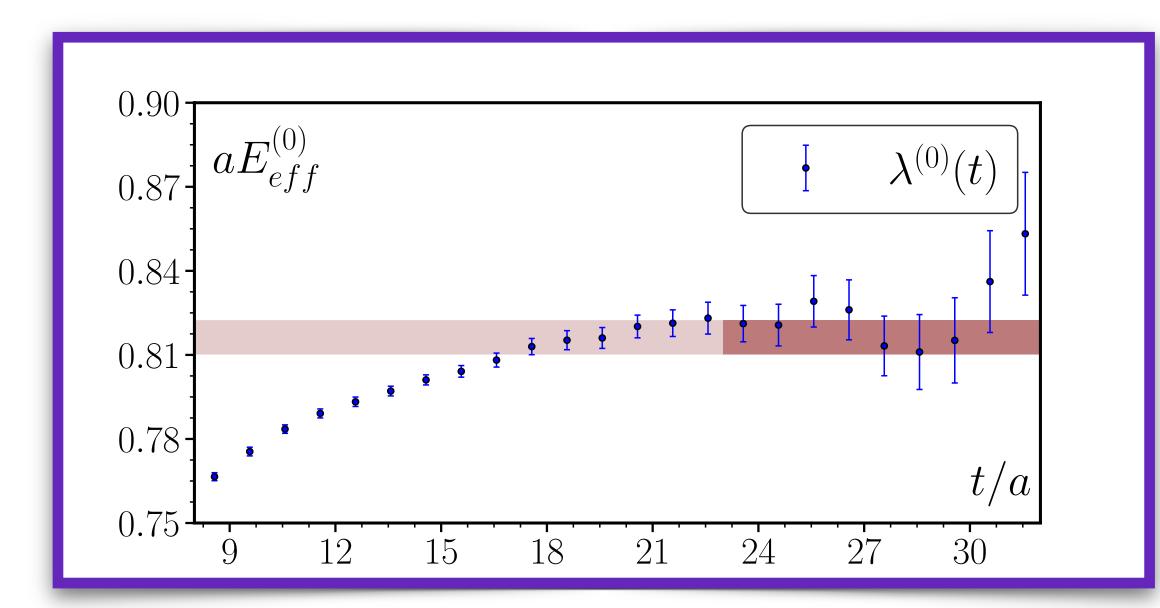
 We use GEVP to extract finite volume spectrum from correlation-matrix variationaly.

$$\mathscr{C}(t)v^{(n)}(t) = \lambda^{(n)}(t, t_0)\mathscr{C}(t_0)v^{(n)}(t)$$

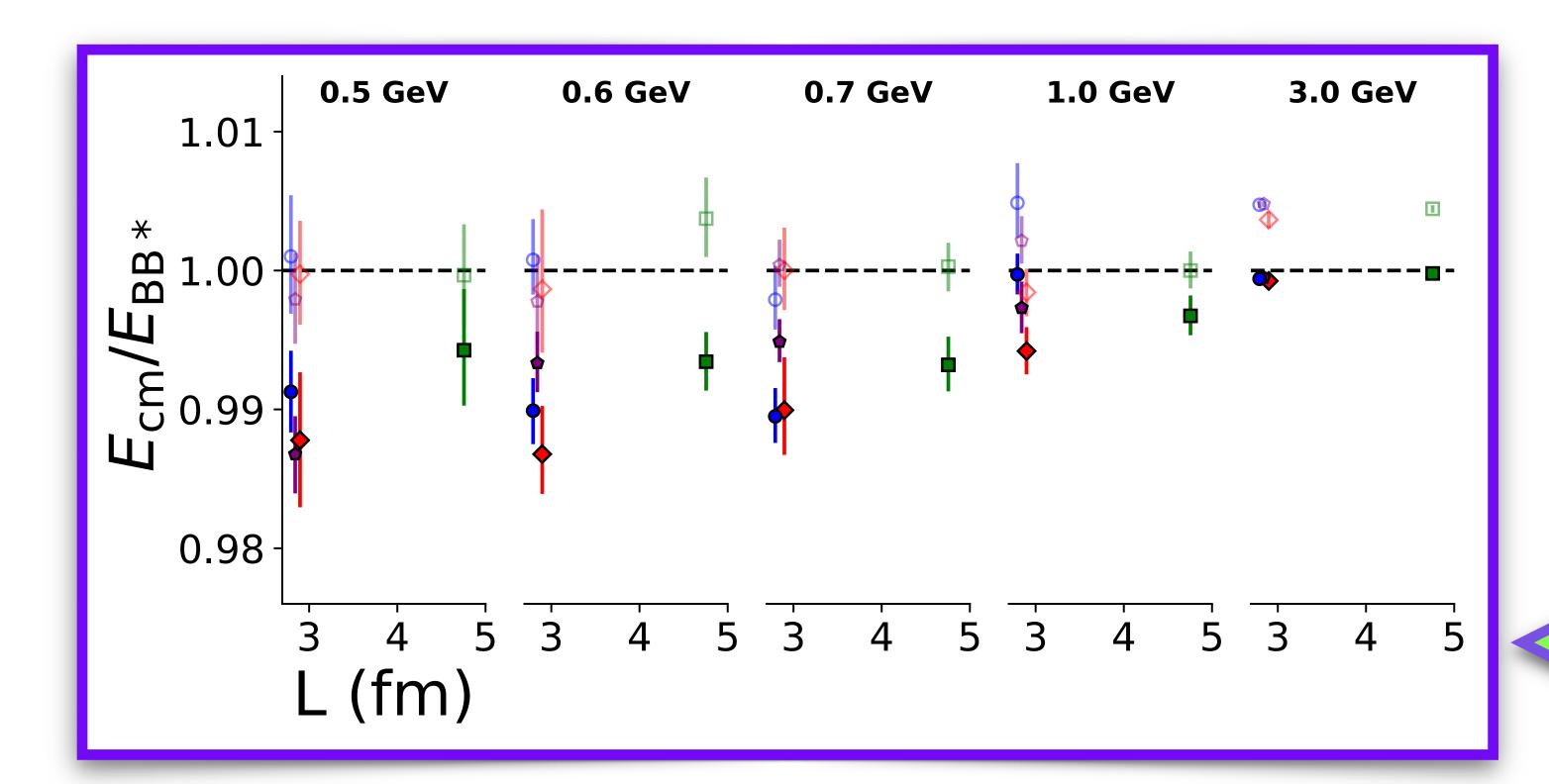
ullet Fitting the leading exponential of $\lambda^n(t)$, yields the energy Eigen state E_n .

$$\lambda^{n}(t, t_{0}) = |A_{n}|^{2} e^{-E_{n}(t-t_{0})} [1 + \mathcal{O}(e^{-\Delta_{n}(t-t_{0})})]$$

- Excited states can be determined with this method.
- ullet Repeated for B and B^* mesons.



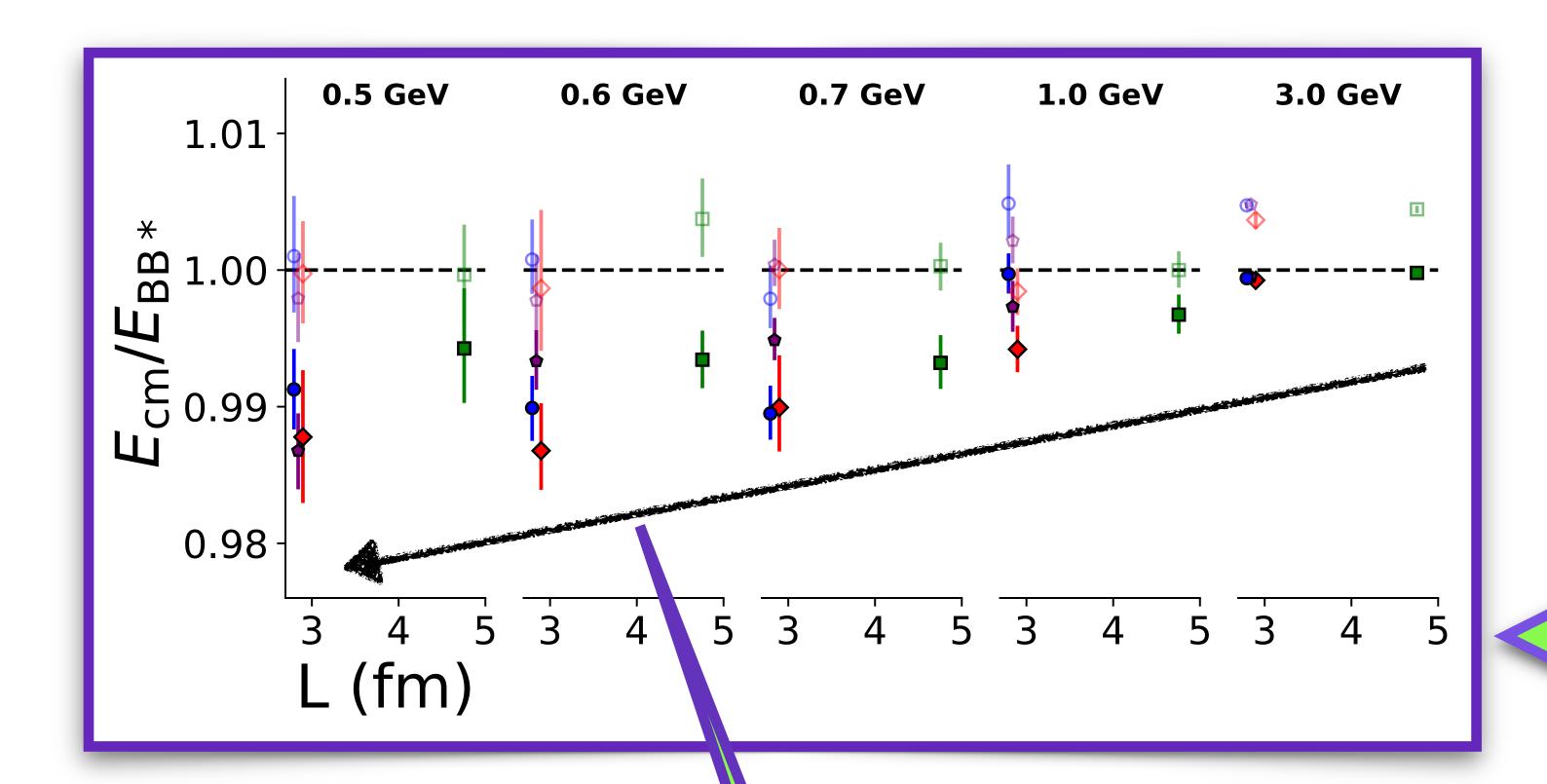
Finite Volume Spectrum cont.



ullet Spectrum extraction repeated for every M_{ps} and every ensemble.

Spectrum were calculated In terms of nearest Two body decay threshold BB^{st} .

Finite Volume Spectrum cont.



Spectrum extraction repeated for every M_{ps} and every ensemble.

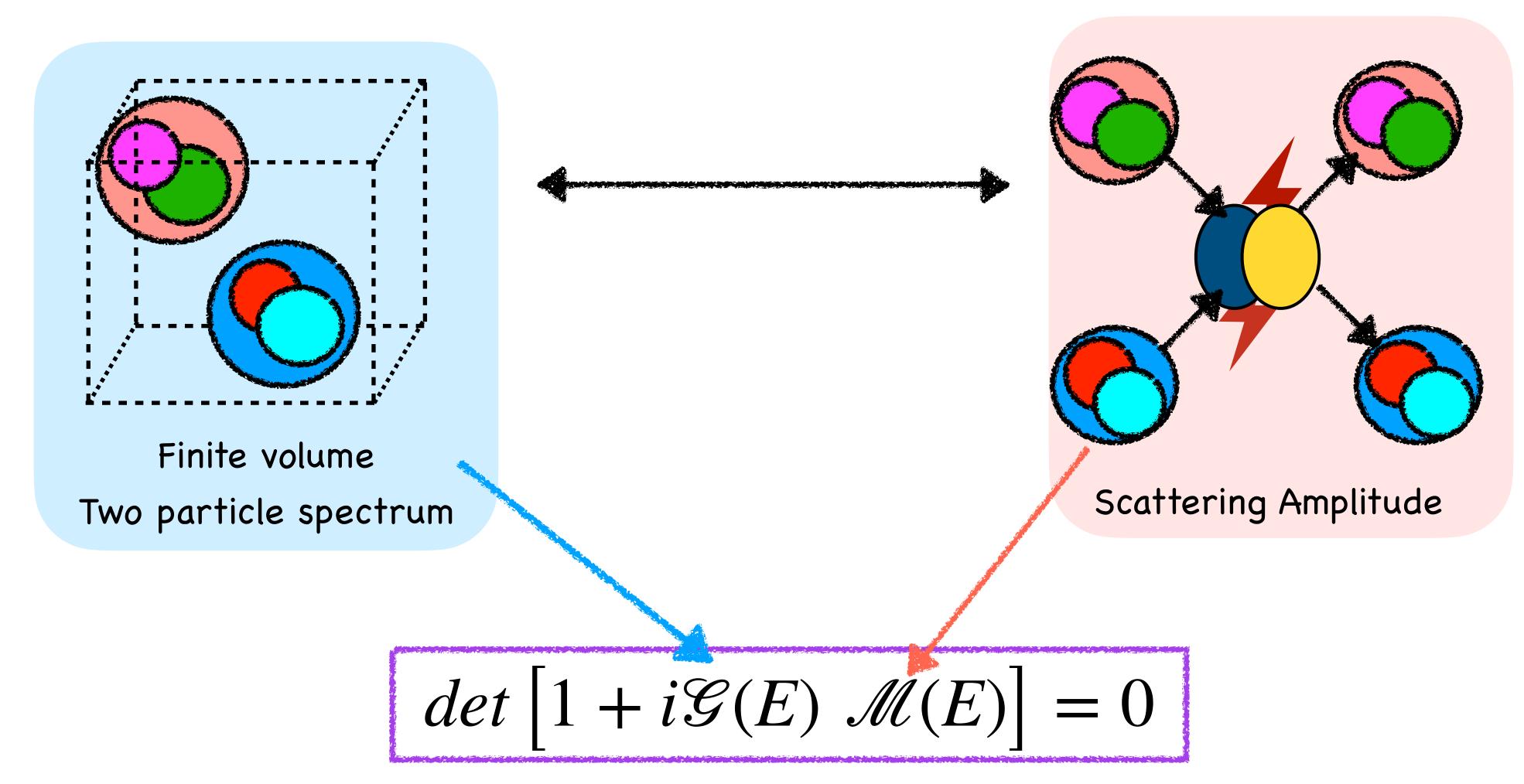
Spectrum were calculated In terms of nearest Two body decay threshold BB^{st} .

A decreasing trend can be observed

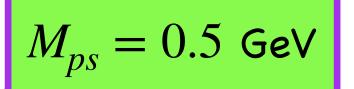
We need continuum extrapolation to have results in physical limit

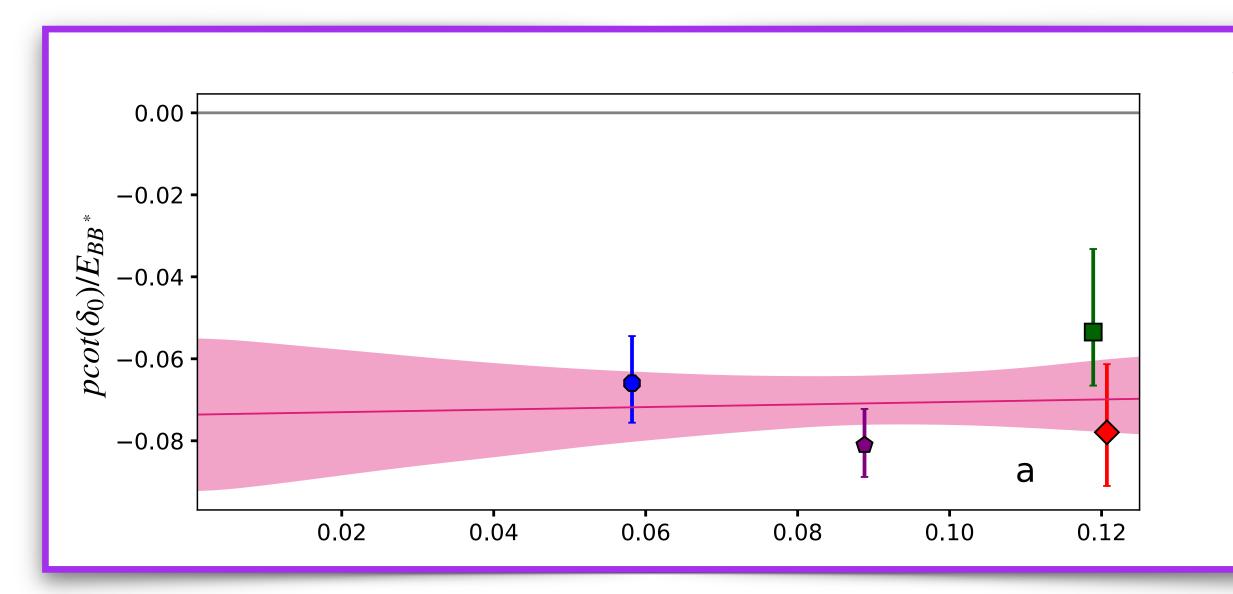
Amplitude Analysis

Lüscher based quantization condition(1991)



Continuum Extrapolation





• Scattering Amplitude is given as

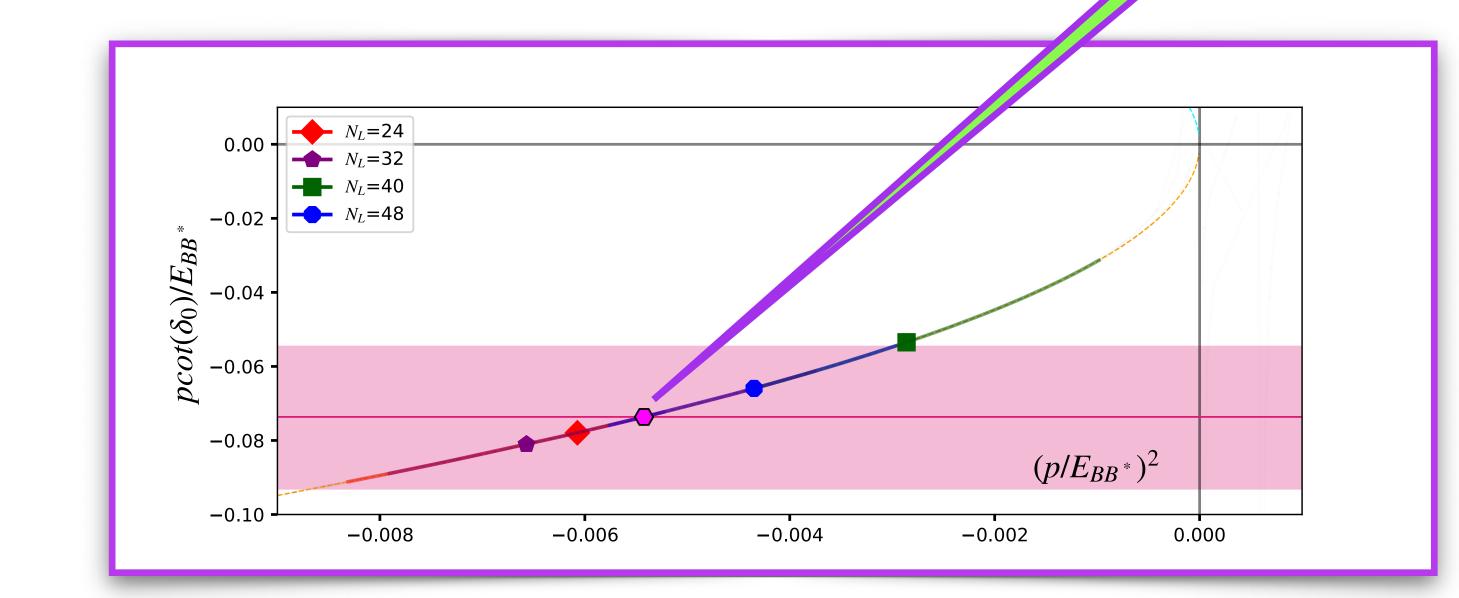
$$T \propto (pcot \ \delta - ip)^{-1}$$

• It is parametrised as

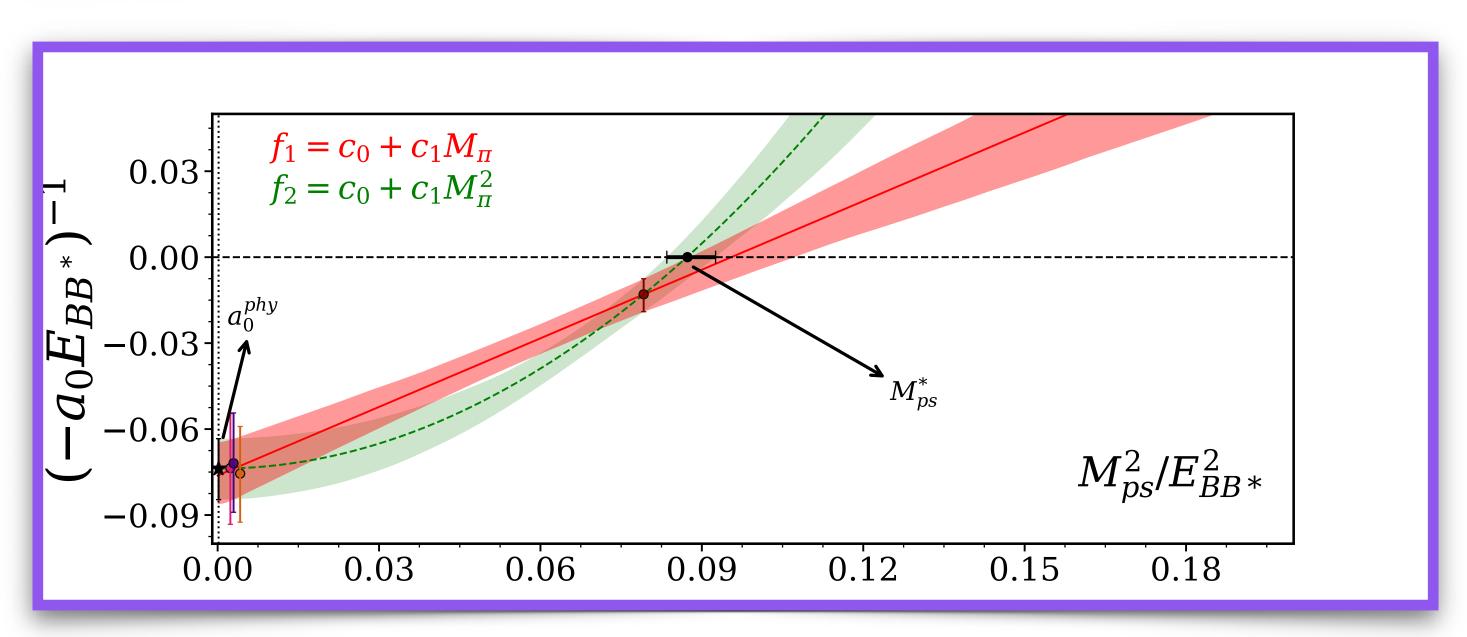
$$pcot \ \delta = -\frac{1}{a_0} + B \cdot a$$

Real Bound State

- ullet Same repeated for other M_{ps} .
- \bullet Consistent Negative values for other M_{ps} as well as real bound state.



Chiral Extrapolation

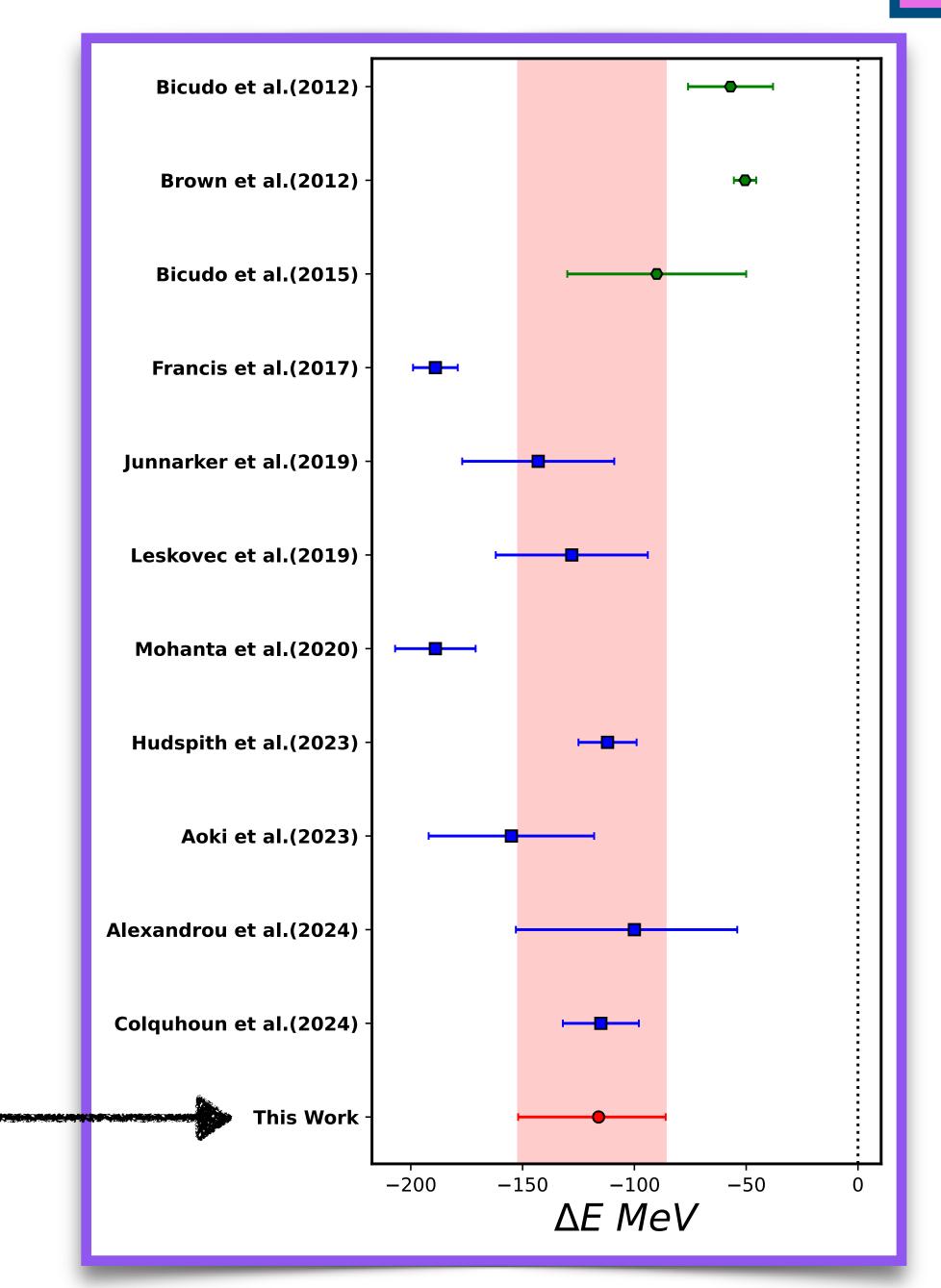


Result:

Scattering length at physical limit

$$a_0^{phy} = 0.25\binom{4}{3} fm$$

Corresponds to binding energy $\Delta E = -\ 116(^{+30}_{-36})$ MeV.



Summary and Outlook

- ullet Various work widely predicted deep binding in isoscalar T_{bb} .
- ullet Rigorous spectrum analysis were done for T_{bb} tetraquark with $I(J^P)=0(1^+)$.
- We worked with multiple lattice spacing, two volumes to control systematics.
- ullet Finite volume spectrum indicates negative energy shift with respect to BB^* threshold.
- Amplitude analysis were carried out with Lüscher Formalism.
- Found a possible deeply bound state.

THANK YOU

More Lattice Talks tomorrow

- Dr. Sanayantan Sharma
- Dr. M. Padmanath
- Dr. Indrakshi R.