



***Lecture delivered during the Teachers Enrichment Workshop held at IMSC
between 26th November to 1st December 2018.***

Good noon friends



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1. A cricketer mathematician leading out his cricket team: "The Mathematical", to play against "The Rest of the World".



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2. He wrote a book entitled "Mathematicians apology" in 1940. It is one of the most vivid descriptions of how a mathematician thinks and the pleasure of mathematics.



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1. A cricketer mathematician leading out his cricket team: "The Mathematical", to play against "The Rest of the World".
2. He wrote a book entitled "**Mathematicians apology**" in 1940. It is one of the most vivid descriptions of how a mathematician thinks and the pleasure of mathematics.
3. His interests covered many topics of pure mathematics:- Diophantine analysis, summation of divergent series, Fourier series, the Riemann zeta function and the distribution of primes.



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Godfrey Harold Hardy

**Born: 7 February 1877 in Cranleigh,
Surrey, England**

**Died: 1 December 1947 in
Cambridge, England**

1. **A cricketer mathematician leading out his cricket team: "The Mathematical", to play against "The Rest of the World".**
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Discrete Fourier Transforms



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Discrete Fourier Transforms

- **Continuous signals are digitised using digital computers**
- **When we sample, we calculate the value of the continuous signal at discrete points**
 - **How fast do we sample**
 - **What is the value of each point**
- **Quantization determines the value of each samples value**



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Finite Fourier Sine and Cosine Transforms



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Finite Fourier Sine and Cosine Transforms

Suppose we have a function $f(x)$ defined in an interval $(-c, c)$
which is Fourier expandable



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Finite Fourier Sine and Cosine Transforms

Suppose we have a function $f(x)$ defined in an interval $(-c, c)$ which is Fourier expandable

$$\text{Then, } f(x) = \frac{a_0}{2} + \sum_1^{\infty} a_n \cos\left(\frac{n\pi x}{c}\right) + \sum_1^{\infty} b_n \sin\left(\frac{n\pi x}{c}\right)$$



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$$F_c(n) = \sqrt{\frac{2}{c}} \int_0^c f(t) \cos\left(\frac{n\pi t}{c}\right) dt$$



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$$F_c(n) = \sqrt{\frac{2}{c}} \int_0^c f(t) \cos\left(\frac{n\pi t}{c}\right) dt \text{ is the Finite Fourier cosine Transform of } f(x)$$



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Inverse Finite Fourier Sine and Cosine Transforms



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Inverse Finite Fourier Sine and Cosine Transforms

$$f(x) = \sqrt{\frac{2}{c}} \left\{ \sum_1^{\infty} F_s(n) \sin \left(\frac{n\pi x}{c} \right) \right\}$$



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Inverse Finite Fourier Sine and Cosine Transforms

$$f(x) = \sqrt{\frac{2}{c}} \left\{ \sum_1^{\infty} F_s(n) \sin \left(\frac{n\pi x}{c} \right) \right\}$$

is the inverse Finite Fourier sine Transform of $f(x)$ is



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$$f(x) = \sqrt{\frac{2}{c}} \left\{ \sum_1^{\infty} F_s(n) \sin \left(\frac{n\pi x}{c} \right) \right\}$$

is the inverse Finite Fourier sine Transform of $f(x)$ is

The Inverse Finite Fourier cosine Transform of $f(x)$ is



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Inverse Finite Fourier Sine and Cosine Transforms

$$f(x) = \sqrt{\frac{2}{c}} \left\{ \sum_1^{\infty} F_s(n) \sin \left(\frac{n\pi x}{c} \right) \right\}$$

is the inverse Finite Fourier sine Transform of $f(x)$ is

The Inverse Finite Fourier cosine Transform of $f(x)$ is

$$f(x) = \sqrt{\frac{1}{c}} F_c(0) + \sqrt{\frac{2}{c}} \left\{ \sum_1^{\infty} F_c(n) \cos \left(\frac{n\pi x}{c} \right) \right\}$$



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Find the Inverse Finite Fourier Sine and Cosine Transforms of the function



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Find the Inverse Finite Fourier Sine and Cosine Transforms of the function

1) $f(t) = 1, 0 < t < 1$

2) $f(t) = t(\pi - t), 0 < t < \pi$



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Find the Inverse Finite Fourier Sine and Cosine Transforms of the function

$$1) f(t) = 1, 0 < t < 1$$

$$2) f(t) = t(\pi - t), 0 < t < \pi$$

These are also called the Discrete Fourier transforms of the function



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Fast Fourier Transformation



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Fast Fourier Transformation

- A fast Fourier transform (FFT) is an algorithm that calculates the discrete Fourier transform (DFT) of some sequence – the discrete Fourier transform is a tool to convert specific types of sequences of functions into other types of representations.



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Fast Fourier Transformation

- A fast Fourier transform (FFT) is an algorithm that calculates the discrete Fourier transform (DFT) of some sequence – the discrete Fourier transform is a tool to convert specific types of sequences of functions into other types of representations.
- Another way to explain discrete Fourier transform is that it transforms the structure of the cycle of a waveform into sine components.



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- Another way to explain discrete Fourier transform is that it transforms the structure of the cycle of a waveform into sine components.
- Cooley - Tukey FFT algorithm



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- **Fast Fourier transformation and the Caller ID in a Mobile phone**



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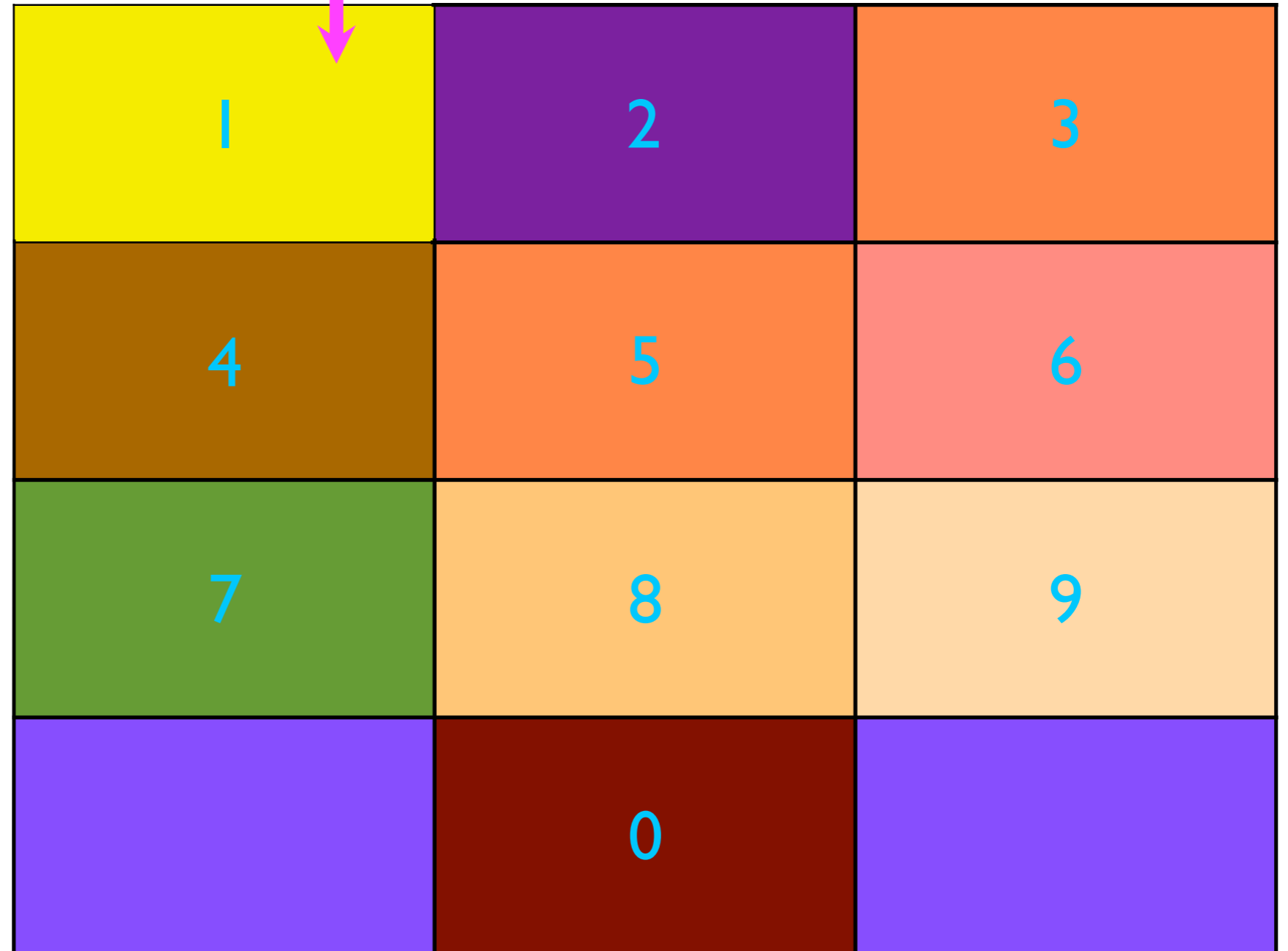
- **Fast Fourier transformation and the Caller ID in a Mobile phone**

1	2	3
4	5	6
7	8	9
	0	



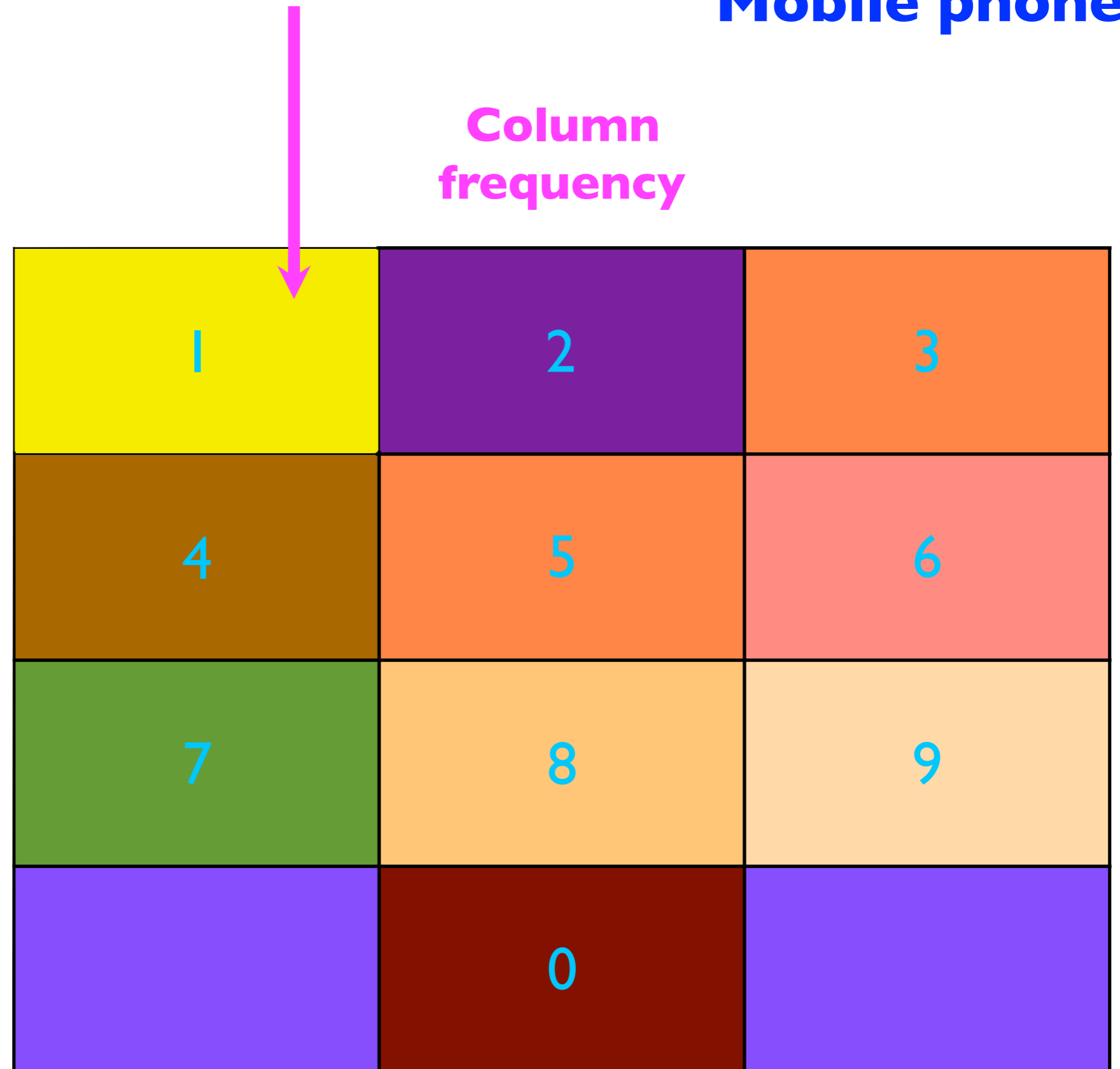
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- **Fast Fourier transformation and the Caller ID in a Mobile phone**



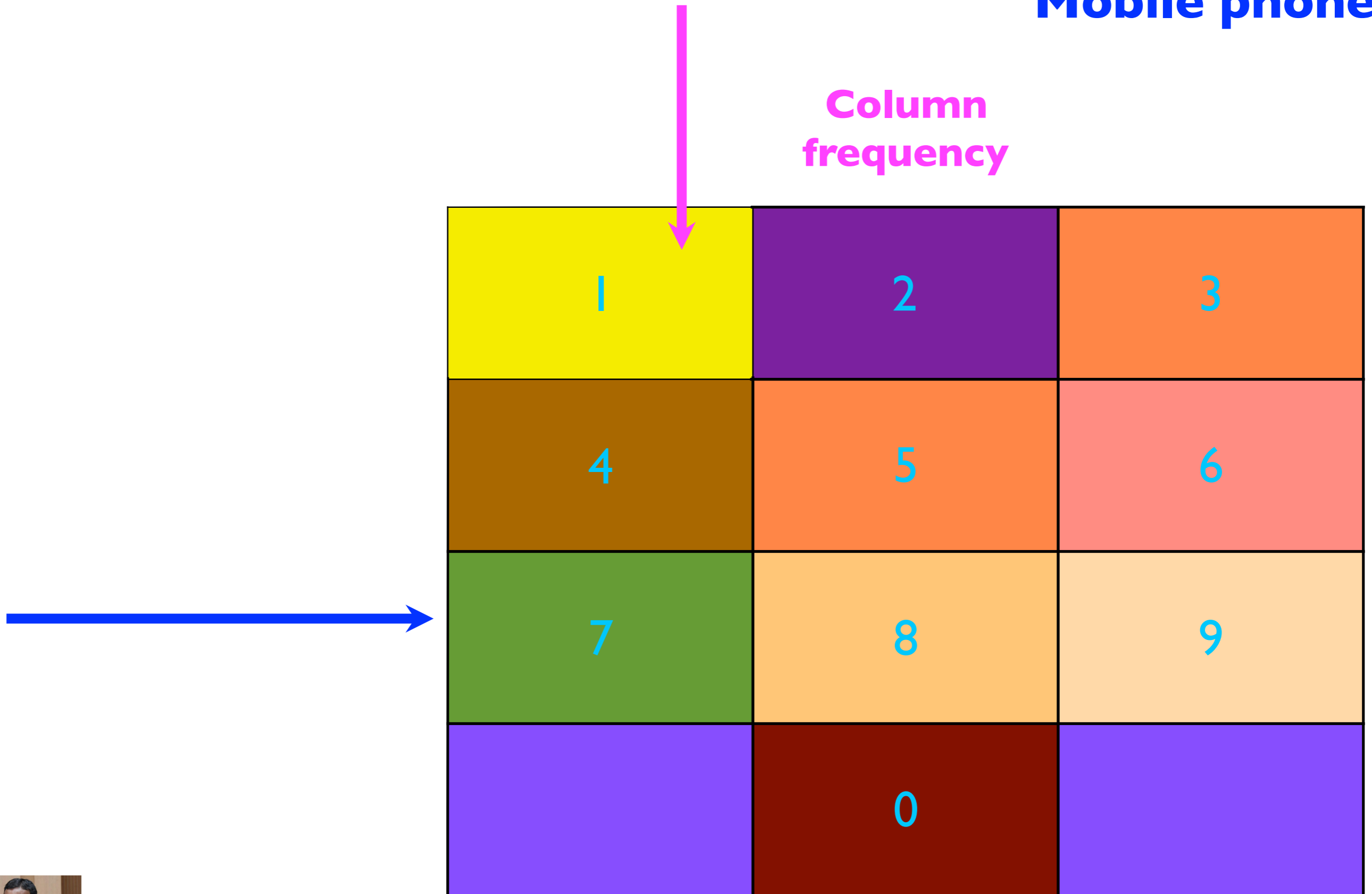
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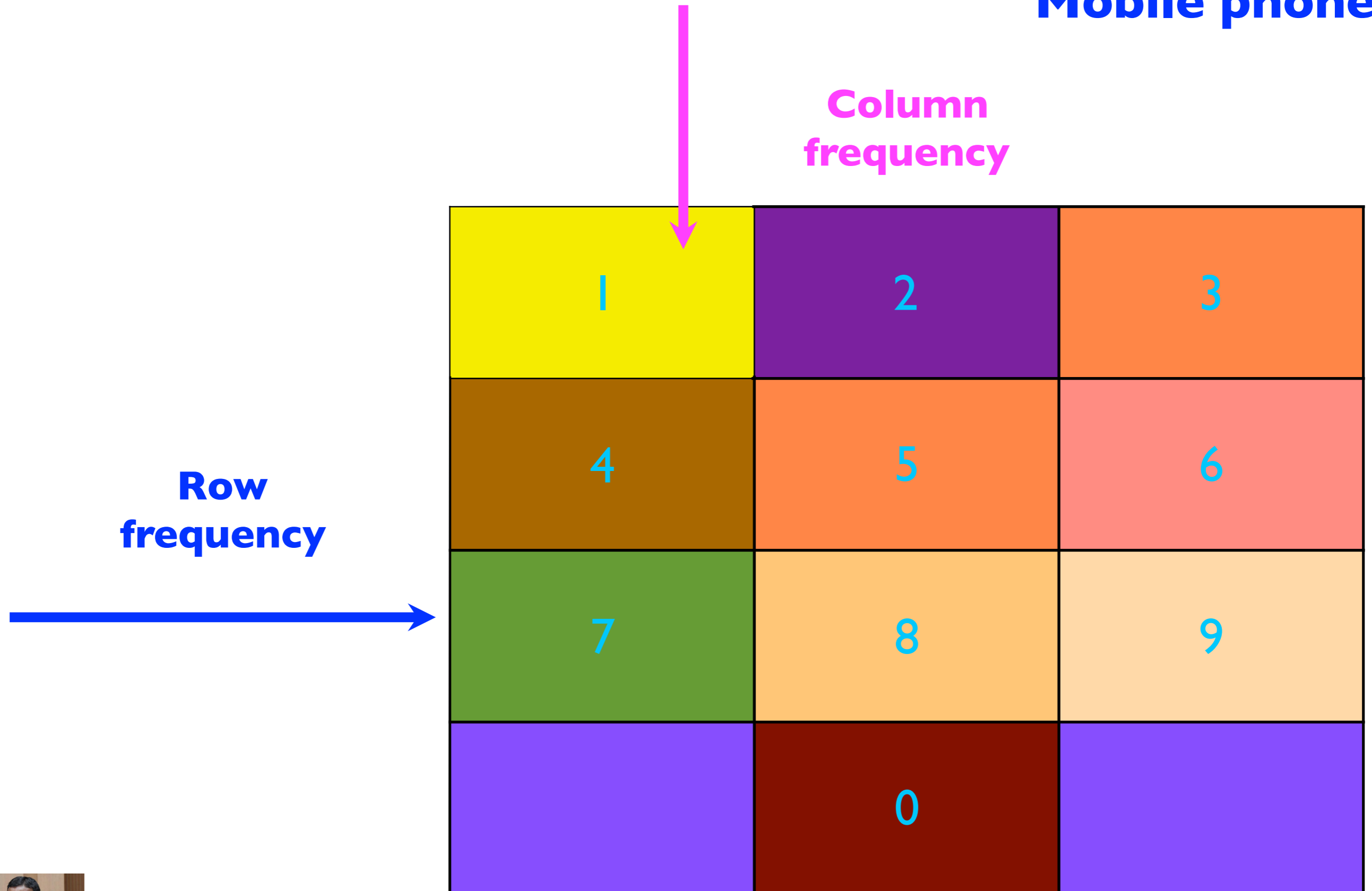
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DTMF Technology

Column frequency

Row frequency

1	2	3
4	5	6
7	8	9
	0	



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I. When a number is pressed two frequencies are generated



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- 1. When a number is pressed two frequencies are generated**
- 2. When all the , say, + 10 numbers are pressed a combined time curve is formed**



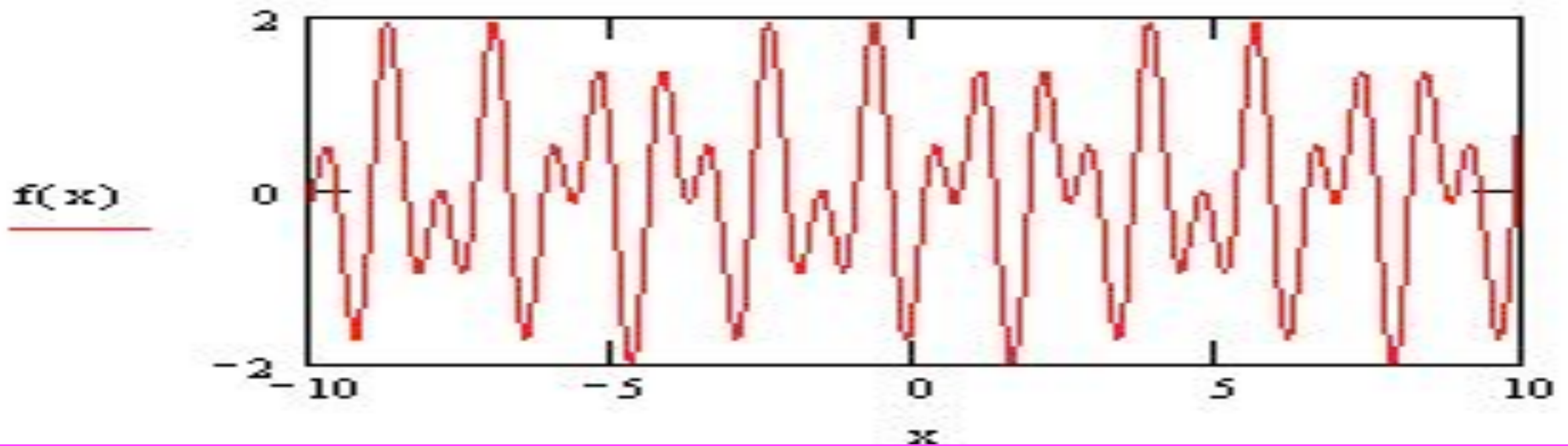
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- 1. When a number is pressed two frequencies are generated**
 - 2. When all the , say, + 10 numbers are pressed a combined time curve is formed**
 - 3. A Fourier transformation ,actually FFT , of that curve is taken.**
- This curve may be of the form**



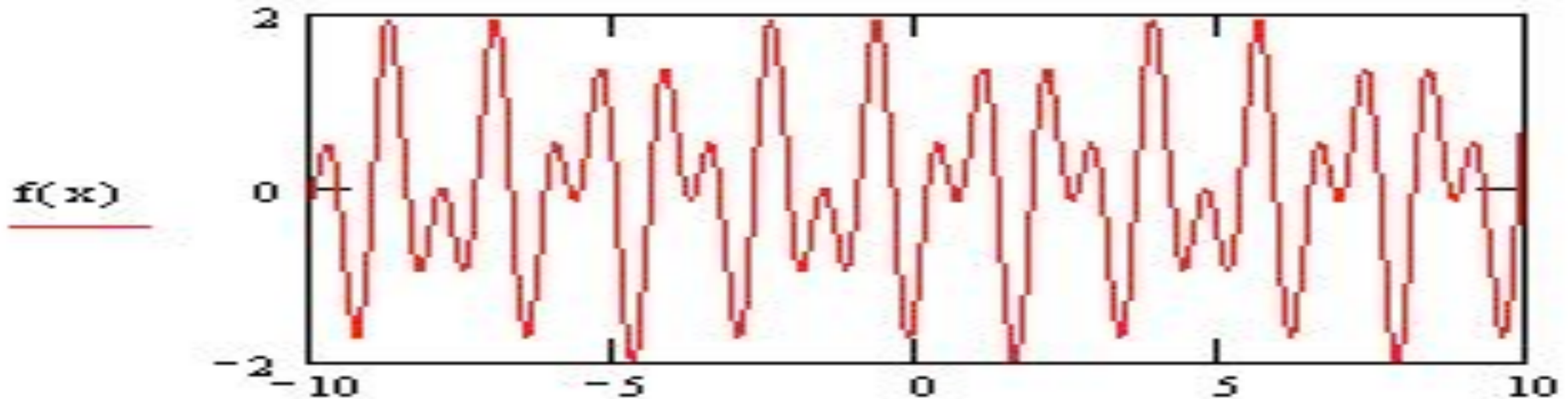
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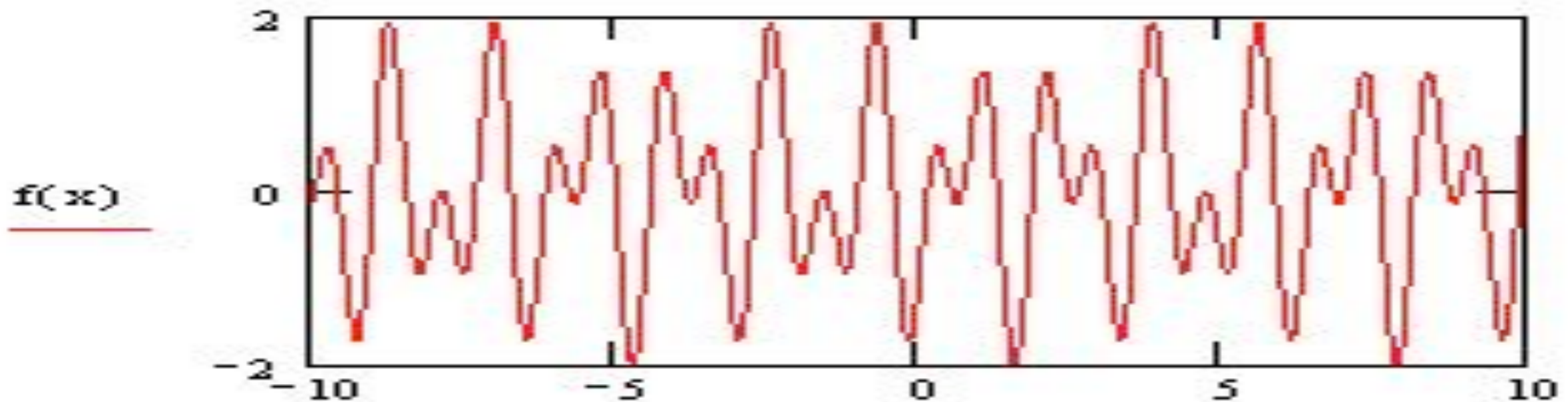


4. Count the number of peaks which is the number of number dialled



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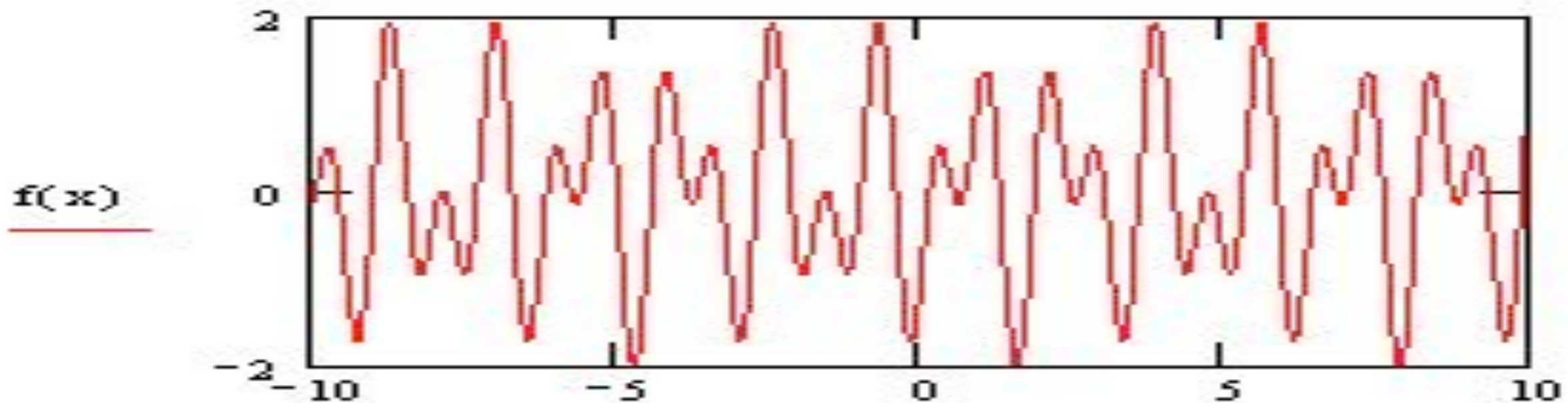


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5. Each peak corresponds to the combined frequency of certain number



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4. Count the number of peaks which is the number of number dialled
5. Each peak corresponds to the combined frequency of certain number
6. A mechanism will catch the number and display them.



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Steganography



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Steganography

By removing all but the last 2 bits of each colour component, an almost completely black image results. Making the resulting image 85 times brighter which results a cat comes from the tree



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References



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References

1. **B.S. Grewal** , **Higher Engineering Mathematics**



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3. http://www-history.mcs.st-and.ac.uk/Day_files/Year.html



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