Systems Biology Across Scales: A Personal View XXVI. Waves in Biology: From cells & tissue to populations

> Sitabhra Sinha IMSc Chennai

Spiral Waves in Biological Excitable Media



Aggregation of Dictyostelium Discoidium amoebae by cAMP signalling Ca⁺⁺ waves in cytoplasm of *Xenopus* oocytes

Electrical activity in heart





Spiral Waves in Slime Mold

Normally slime mold exist as individual singlecelled amoeba – but when starvation conditions arise they suddenly aggregate into a multicellular body.

Dictyostelium cells aggregate by moving towards the propagating waves of chemoattractant cyclic AMP (cAMP)





Claviez et al. (1986)

Normal cell aggregation patterns in experiments

Dallon and Othmer (1997)

Streaming cell density patterns in model (cAMP wave shown in blue)

Nakajima and Sawai Nature Communications 5, 5367 (2014)

Anatomical reentry & spiral waves

The earliest understanding of the formation of the spiral was as a 1-dimensional reentrant wave, i.e., the continuous circulation of a single pulse of activity around an inexcitable region resulting in persistent periodic activity of tissue even when individual cells comprising it are not capable of oscillation (Mines, 1913)



G R Mines





if initial position recovers by the time the wave comes back, reentrant activity becomes persistent

Schematic diagram of a ring of cardiac excitable tissue created by Mines from a tortoise heart

A self-sustaining wave of excitation circulation around the system, resulting in successive contractions of V_1, V_2, A_1, A_2 respectively was observed.

Spiral wave from a broken excitation front



Sinha and Sridhar, 2014

Spiral wave from T1-T2 stimulation protocol

First stimulus applied at time T1 in center of domain Second stimulus given at time T2 in a region that is not fully recovered









Formation of a double spiral





Sinha and Sridhar, 2014

Spatiotemporal chaos from spiral breakup



wavefront colliding with inexcitable region



rise of new spiral wave fragments





Sinha and Sridhar, 2014

From excitable to oscillatory media

A close cousin of excitable media models are... Oscillatory media...

obtained by making both the resting and excited states <u>unstable</u>

Also exhibit spiral waves !



Many biological systems that show regular, periodic oscillations are modeled by oscillatory media

Some switch between excitable & oscillatory

Coherent excitation in pregnant uterus



Lammers Lab

The Pregnant Uterus: an excitable media

Increase in excitability with developing pregnancy Increased spatial synchronization in excitation leads to coherent contractions \rightarrow onset of labor (childbirth)

Spreading Waves in Epidemics

Contagion spreading can be represented in an excitable media context

Susceptible, S : resting state Infected, I : excited state Recovered or Removed, R : refractory state



Red : new cases

Ferguson et al, Nature, 2005

Green : areas where the epidemic has finished

Snapshots (30 - 240 days) after first case of an uncontrolled outbreak of transmissible avian flu in people living in Thailand.

Fisher Waves: Wave of advance of advantageous genes in spatially dispersed population

R A Fisher, Annals of Human Genetics (1937)

Let p be the frequency of the mutant gene, and q that of its parent allelomorph, which we shall suppose to be the only allelomorph present. Let m be the intensity of selection in favour of the mutant gene, supposed independent of p. Suppose that the rate of diffusion per generation across any boundary may be equated to

$$-krac{\partial p}{\partial x}$$

at that boundary, x being the co-ordinate measuring position in the linear habitat. Then p must satisfy the differential equation

where t stands for time in generations.

The Mutation Traveling Phenomenon



C.A. Edmonds, A.S. Lillie, and L.L. Cavalli-Sforza, PNAS USA 97 (2004) 975 Expansion of population and subsequent dispersion of a mutant subpopulation - within it shown at three time points (measured in terms of generations)



legend

- # of individuals in deme
- empty deme
- saturated deme (N=10)

- deme contains only non-mutant individuals
- mutation origin
- mutant centroid



End-result of different simulations with mutations seeded at random locations (* indicates place of origin of mutation, x indicates mutant centroid)



The Neolithic Transition Wave



Neolithic revolution:

Cultural Diffusion: Wave of advance for 'polis' (city)



Pounds 1996

Dynamical patterns in excitable/ oscillatory media at all scales

- Intracellular: Ca⁺⁺ waves
- Cellular: signal propagation between neurons
- Groups of cells: synchronization of beta cell activity in pancreas
- Tissue: coordination of muscle activity in ventricles
- Organ: coherent contractions in pregnant uterus
- Populations: population dispersal (Fisher waves); spreading waves of epidemics