



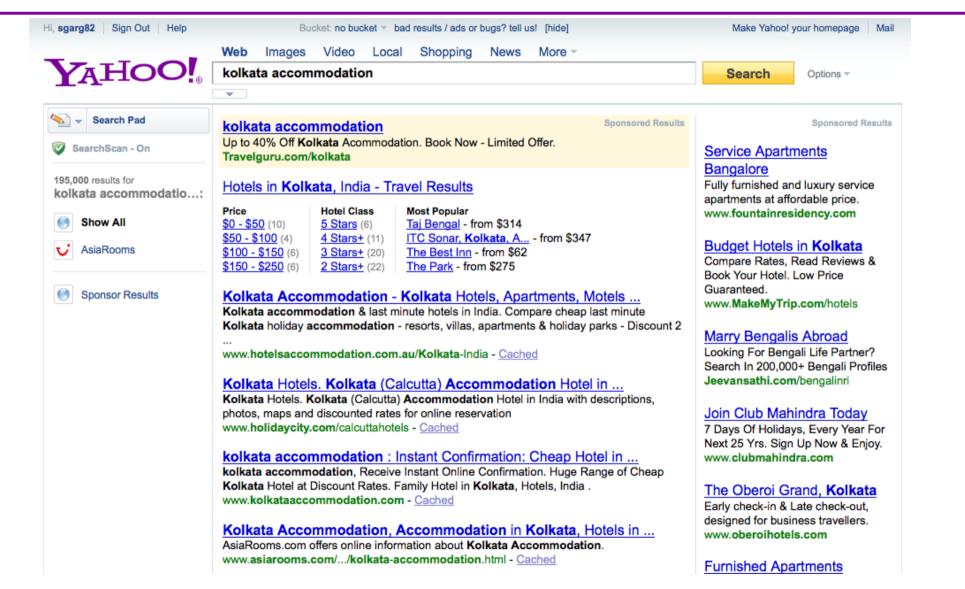
- Introduce Web monetization
 - Search and Display Advertisement
- Auctions
 - Participation in Auctions
 - Pricing
- Exchanges
 - Ranking, response prediction
- "Next gen" monetization
 - Social Targeting
 - Chunked-rewards



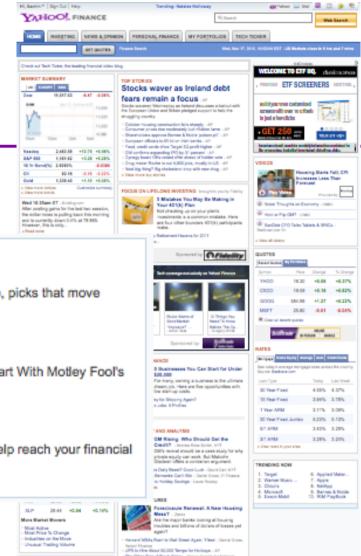
- The WWW comes free for users
 - Browse, search, communicate, chat, socialize, all free!
- Web is funded by advertisers!
 - To a large extent (Yahoo!, Google, Facebook, Bing)

How does online advertising work?





Contextual Ads



SPONSORED LINKS

1.25-1.45% Apply Online! With AA+ Rated GE Capital Corp. Not An Offer Of Securities For Sale. GEinterestplus.com

Foreign Exchange Trading Free \$50,000 Practice Account With Real-Time Charts. News & Research. www.Forex.com

Crown Capital Securities Professional Wealth Management http://RothConverter.com

3 Stocks Set to Surge

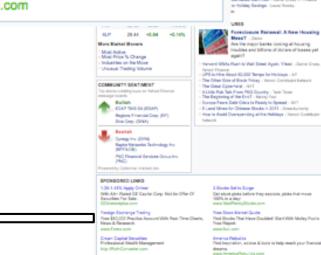
Get stock picks before they explode, picks that move 100% in a day! www.MadPennyStocks.com

Free Stock Market Quote

Find Stocks That Have Doubled! Start With Motley Fool's Free Report. www.fool.com

America Rebuilds

Find inspiration, advice & tools to help reach your financial dreams. www.AmericaRebuilds.com



portunities and	30 Year Fixed	4.00% 4.37%
	10 Year Fixed	3365 3785
	1 Year ARM	3.11% 3.09%
	30 Year Fixed Junito	8.20% 8.10%
	BT ARM	3.43% 3.29%
Cel Re	3/1 ARM	3.28% 3.20%
on, NYT asse study for why	a Vine nine is your area.	
of Malcolm		
n argument.	TRENDING NOW	
Gauld Carr, KYT Gross, YT Finance	1. Target	6. Applied Mater
trainy	2. Warner Music	T. Apple
	3. Chiefs	8. Nethop
	4. Marcaill 5. Easter Meld	 Barres & Noble 10. RM PayBook
A New Housing		
ng all housing lans of losses yet		
as a complete		
her - David Group,		
- A2		
moutor Kativo N		
lainer .		
TWO IS		
Inst Autority		
Yahari Coshibuter		
interine the line of the line		

Display Ad: Impression

HOME L	U.S.	BUSINESS	WORLD	ENTERTAINMENT	SPORTS	TECH	POLITICS	SCIENC	E HEALTH	OPINION	MOST POPULAR
Tech Video	Blog	Internet	Gadgets	Cell Phones	Apple/Macintos	sh So	cial Media	Video Gam	es Security		
Q. Search	All News		New	vs Search TF	RENDING NOW:	rima fakih	sandra d	liaz-twine	ronnie james dio	survivor	miss usa

Technology



Study on cell phone link to cancer inconclusive

AP – 2 hrs 11 mins ago

GENEVA - If there's one lifestyle

tool that's ubiquitous, from American cities to remote villages of the developing world, it's the mobile phone. Full Story »

Technology Slideshows









Microsoft



Most Popular - Technology

· Death of 2 boys prompts toy dart gun set recall

Japan's Astellas to buy US drug co. OSI for \$4B

ADVERTISEMENT

Most Recommended

(iiconnect-

More Most Emailed - Technology »

Most Emailed Most Viewed

Featured

More Technology Slideshows »

Heart group backs video

Supreme Court rejects appeal of "must-carry"

games in obesity

AP - Mon May 17, 1:03 pm ET

AP - Mon May 17, 10:57 am ET

campaign

rule

Technology Photos

Apple iPad

Apple Inc.



Display Ad: Conversion



A minister had asked for

Mon, Nov 15 04:25 PM

Dehradun: When asked to reveal his mai compromising with ethics and values, Tai said he did not have a methodology in thi to tell the audience.

"Several years ago, Tatas were trying to a collaboration with Singapore Airlines. Ever airline industry, we had enormous proble reports in the media.

"We approached three Prime Ministers a our efforts to form the airlines." he said.

Later, Tata said a fellow industrialist commented, "You are stupid people. The Minister was asking for Rs 15 crore. Why didn't he pay?"

Last Name *	
First Name *	
Email *	
Phone *	
Company *	
DHL Express is my preferred service partner because*	
	Yes, it's ok to send me email
G	ET STARTED

No one knows express shipping like we do

Spend less time shipping and more time growing your business, worldwide. As a new DHL customer, here are the key benefits that you can look forward to.

online.

Fast and reliable Customs expertise We are faster and more reliable than ever. Reach over 220 countries and territories at affordable rates. Relax. DHL collects, clears through customs and delivers millions of shipments every day. Late pick-up times Online tracking Get the latest possible pick-up so you have more time and can respond Enjoy full visibility with real-time check point and delivery details

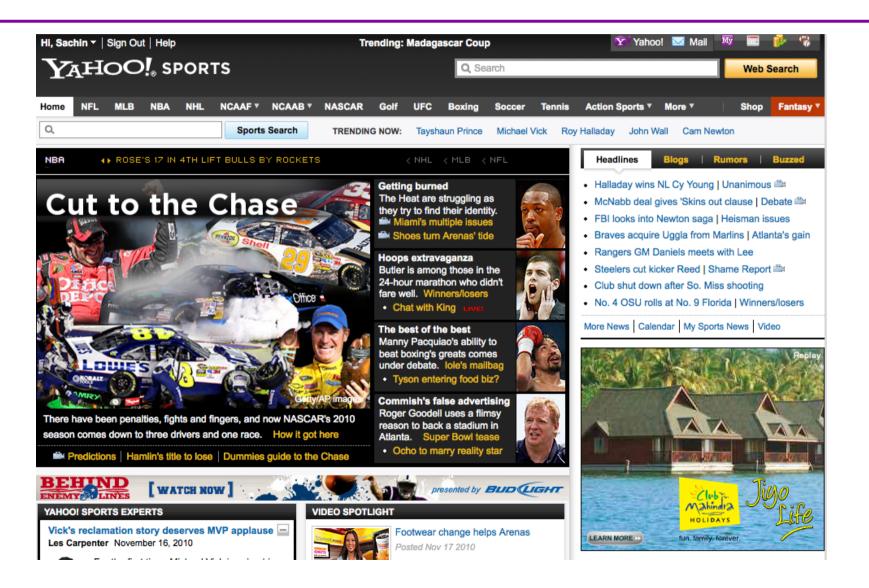
TRY THE NEW NEWS EXPERIENCE

to last minute requests.

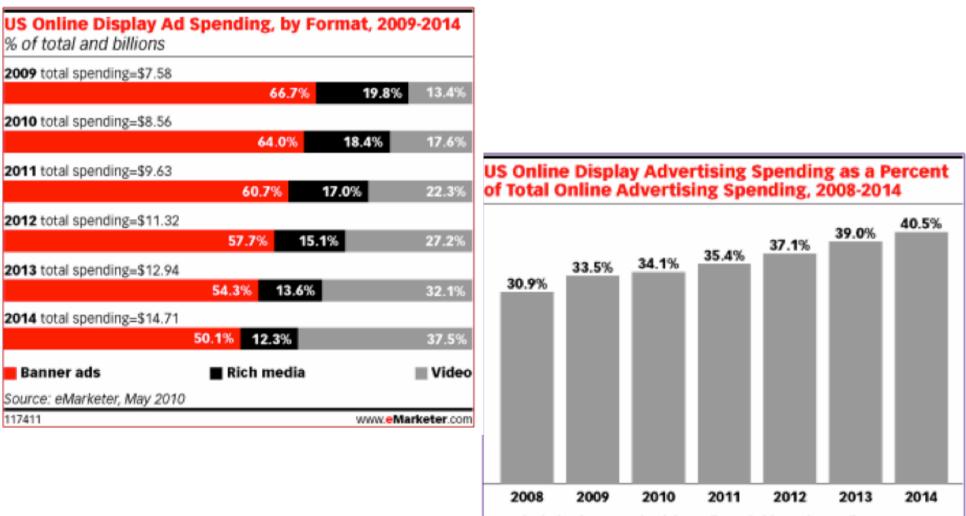
Display Ad: Publisher targeting

	Hi, Sachin	Sign Out He	lp		Trending:	Jennifer Grey		😵! Yahoo! 🔛 I	lai 🔯 📼 🥬	-
	VAL	100!, I	INANC	E		Q. Search			Web Search	
				_						
									oices ()	
			PRICIN	GSTR	UCTURE ONLY	5 405 45	124	TRADEKIN	IG ·	
					COULD HATE.	495 659 10 10 10 10 10 10 10 10 10 10 10 10 10 1		SEE FOR YOURSELF.		
		יין יי		UNER	COULD HATE.	MARKET OR LINIT		SWITCH TO TRADEKING TOD MEMOER FINRA, ISE & SIP		
								PERSEN FIRMA, IZE & SIF	-	
	HOME	INVESTING	NEWS 8	OPINION	PERSONAL FINANCE	MY PORTFOLIOS	TECH T	ICKER		
	HOME	INVESTING	NEWS G	OPINION	PERSONAL FINANCE	MTPORTFOLIOS	TECHT	IGRER		
			GET QUOT	'ES Finar	nce Search	We	ed, Nov 17, 20	10, 7:38AM EST - US Marke	ts open in 1 hr and 51 mi	ins
	Today	s Markets					Scottrad	le: \$7 Online Stock Trade	s & Powerful Trading	Tools
	rouay a	5 Markets								
	Market Summ	ıary	(Edil)	Market Coverage			Market Statistics			
	streaming qu	otes: ON 🔞		Market Overview, Market Update, In Play, Story Stocks, Short			Mkt Digest, Most Actives, U.S. Indices, World Indices,			
	NASDAQ	Nov 16, 4:00pm	EST	Stories, Tech Stocks			Exchange Rates, Unusual Volume, Commodities			
	2,520			Today's Events			Financial News			
	~		2,480	-	Conf. Calls, Economic, IPOs	Splits, Up/Downgrades	Top Stories	s, U.S Markets, Most View	ed Articles, Full Covera	ge,
	2,480						Real-time Quotes, Research Reports			
	10am 12pm 2pm 4pm			Premium Services			Investing Tools			
	SYMBOL	LAST	CHANGE	Real-time Quotes, Research Reports			Stock Alerts, News Alerts			
	Dow		78.47 (1.59%)							
	Nasdaq S&P 500	2,469.84	0.00 (0.00%)	Market	Undate				MY YAROOT go Set.	Alert
	10-Yr Bond	2.8470%	0.00 (0.00 %)	mannet	opullo					
	NYSE Volume		0		: S&P futures vs fair value:	+2.10. Nasdaq futures	vs fair	ADVERT	SEMENT	_
	Nasdaq Volun	ne	0	value: +6.					vesting mistakes yo	bu
	Indices:	US - World Mos	Actives		: Nikkei9811.66+14.60 214.46478.602.00%.	+0.20%. Hang		N/10 11	uld avoid in 2010	
				06:41 am					have a \$500,000 blio, download the guide	
	Advances &	Declines		90.41 dm				W by Fi	orbes columnist and	
		NYSE	NASDAQ				more		ey manager Ken Fisher. alled "The Eight Biggest	
	Advances	574 (15%)	563 (20%)					Mist	akes Investors Make and	d
	Declines	3,226 (82%)							to Avoid Them." Even if ave something else in	
Yahoo! Labs,	Unchanged	132 (3%)	112 (4%)					place	right now, it still makes	
	Up Vol*	442 (447%)	208 (11%)					sens	e to request your guide!	
	Down Vol*	3,938 (3977%)	1,617 (88%)					A Real Property lies	Click here to download	d

Display Ad: Location targeting







Note: includes banner ads, rich media and video ad spending Source: eMarketer, May 2010

www.eMarketer.com

. .

Yahoo! Labs, Bangalore

Massive scale

US Online Display Advertising Metrics, 2001-2011

viewed per user per day	pages viewed (bil- lions)	sions per page	impres- sions (bil- lions)		nue per 1,000 pages	Total reve- nues ⊠(bil- lions)
35	1,980	0.41	812	\$6.35	\$2.60	\$5.16
37	2,238	0.36	806	\$4.67	\$1.68	\$3.76
38	2,484	0.34	844	\$3.65	\$1.24	\$3.08
40	2,707	0.36	975	\$4.03	\$1.45	\$3.93
42	3,024	0.37	1,119	\$4.25	\$1.57	\$4.76
45	3,341	0.50	1,671	\$3.50	\$1.75	\$5.85
47	3,608	0.60	2,165	\$3.31	\$1.99	\$7.17
49	3,868	0.62	2,398	\$3.32	\$2.06	\$7.95
51	4,120	0.61	2,492	\$3.39	\$2.05	\$8.45
52	4,338	0.62	2,689	\$3.50	\$2.17	\$9.41
54	4,563	0.63	2,875	\$3.62	\$2.28	\$10.41
	per user jer day 35 37 38 40 42 42 45 47 49 51 52	viewed per user per daypages viewed (bil- lions)351,980351,980372,238382,484402,707423,024453,341473,608493,868514,120524,338	viewed per user per daypages viewed (bil- lions)sions per page351,9800.41372,2380.36382,4840.34402,7070.36423,0240.37453,3410.50473,6080.60493,8680.62514,1200.61524,3380.62	viewed per user per daypages viewed (bil- lions)sions per pageimpres- sions (bil- lions)351,9800.41812372,2380.36806382,4840.34844402,7070.36975423,0240.371,119453,3410.501,671473,6080.602,165493,8680.622,398514,1200.612,492524,3380.622,689	viewed per user per daypages viewed (bil- lions)sions per pageimpres- sions (bil- lions)351,9800.41812\$6.35372,2380.36806\$4.67382,4840.34844\$3.65402,7070.36975\$4.03423,0240.371,119\$4.25453,3410.501,671\$3.50473,6080.602,165\$3.31493,8680.622,398\$3.32514,1200.612,492\$3.39524,3380.622,689\$3.50	viewed per per daypages viewed (bil- lions)sions per pageimpres- sions (bil- lions)nue per 1,000 pages351,9800.41812\$6.35\$2.60372,2380.36806\$4.67\$1.68382,4840.34844\$3.65\$1.24402,7070.36975\$4.03\$1.45423,0240.371,119\$4.25\$1.57453,3410.501,671\$3.50\$1.75473,6080.622,398\$3.32\$2.06514,1200.612,492\$3.39\$2.05524,3380.622,689\$3.50\$2.17

www.eMarketer.com

Quick Recap: Types of ads

- Textual (3 4 lines of text)
 - Paid Search (e.g.,
 - Appear on Search results page
 - · Selected based on search keywords
 - Advertiser pays per click
 - Contextual Ads
 - Appear on web-pages
 - Keywords constitute content of the page
 - Advertiser pays per click
- Graphical (image, video, animation)
 - Appear on web-pages
 - Targeting criteria specified by the advertiser and optimized by the Adnetwork
 - Advertiser chooses between paying per impression, per-click or perconversion

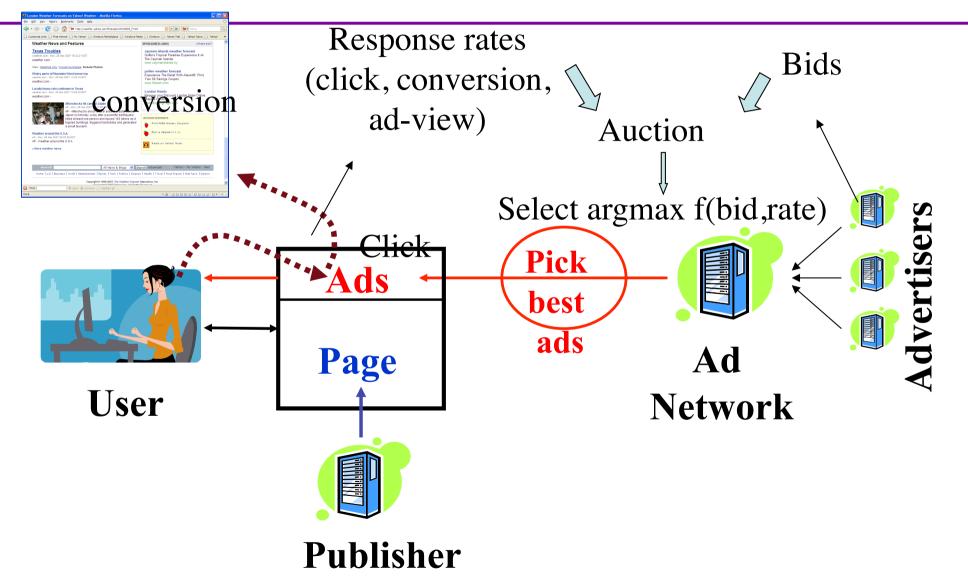
4 Players in Display Ads

- Advertiser: Wants high Rol (e.g. cost per lead or conversion)
 - Demand: Buyer of "ad impressions" from publishers
 - Targets users (e.g. Males, from California) and pages (e.g. sports)
 - May require guaranteed impressions (e.g. 10 Million in 30 days)
 - Or competes in an on-line auction to win impressions
 - Might specify frequency caps (e.g. < 10/user/day)
 - Might specify budget caps (e.g. < \$200 daily)
 - Bidding Examples
 - Lipstick maker: \$2 CPM on 30-40 year old females, who visit fashion pages
 - Insurance seller: \$2 CPA on 40-50 year old males, who visit finance pages
- Publisher: Wants revenue to be maximized, but not at the cost of user dissatisfaction
 - Supply: Seller of "ad impressions" to advertisers
 - Specify types of ads that can be placed (e.g. only travel related ads)
 - Might specify desired payment type of the ads



- User: Wants useful ads
 - Browses
 - Can specify interests / hobbies / likes
 - Views, clicks, converts, buys
- Ad-Network / Exchange (e.g. Y!, Google, MSN): Wants to maximize revenue
 - The "matchmaker"
 - Operates infrastructure for match-making
 - Takes a cut for each payment from advertiser to publisher
 - In many cases, dual role as publisher (like Yahoo!)





Ad Selection: Simple example

- Advertiser 1: Bids \$2 CPM on 30-40 year, males, from Karnataka
- Advertiser 2: Bids \$30 CPC on 25-35 year old males from India
- Advertiser 3: Bids \$90 CPA on males
- Advertiser 4: Bids \$3 CPM on females from Karnataka
- A 30 year old male from Karnataka (user u) browses (page p), causing an opportunity
- Which ad will he end up viewing?
 - Match based on targeting (Ads 1, 2 and 3 are eligible)
 - Compute expected revenue from each
 - Ad 1 = \$0.002_
 - Ad 2 = 30 * P(Click|u, p) = 0.003, (if P(Click|u, p) = 0.001)
 - Ad 3 = \$90 * P(Conv|u, p) = \$0.0009, (if P(Conv|u, p) = 0.0001)
 - Auction conducted on expected revenue: highest one wins
 - Ad 2 wins and gets shown to the user

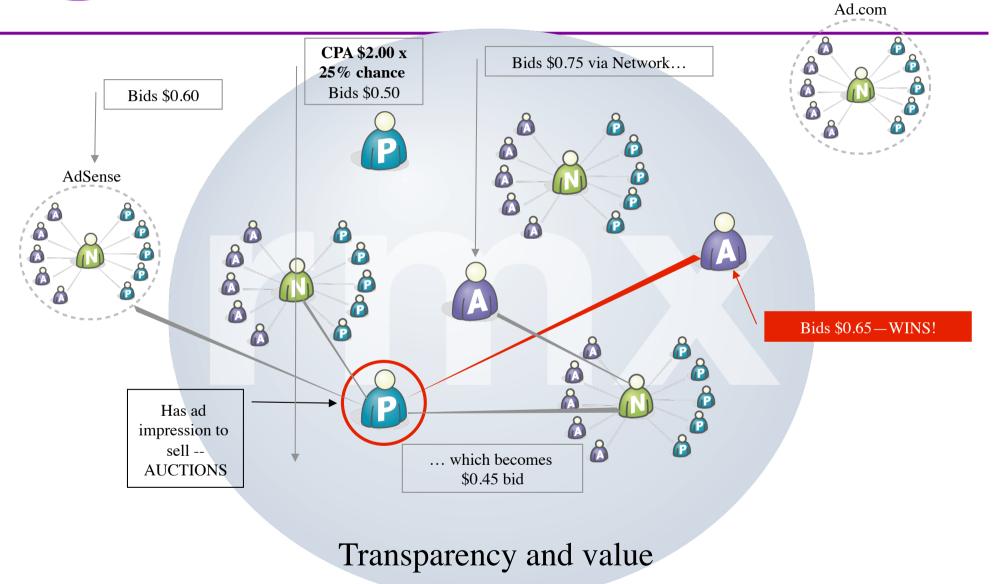
Ad Selection: Prediction

- True P(Click|u, p), P(Conv|u, p) are unknown
- Need to predict
 - Say $\hat{P}(Click|u, p)$ for Ad 2 = 0.0006 (true = 0.001), then Ad 1 wins \implies Loss of \$0.001
 - Say $\hat{P}(Conv|u, p)$ for Ad 3 = 0.0004 (true = 0.0001), then Ad 3 wins \implies loss of \$0.0021
- In-accurate prediction causes 'wrong' ad to be shown
- Accurate prediction is crucial to revenue
- Ranking problem versus absolute prediction



- Determine eligible ads "Matching Problem"
 - Satisfy targeting criteria
 - Other constrains
 - Budget remaining
 - Frequency caps per user / day
- Auction rules
 - Allocation rule
 - Payment rule
- All this needs to happen in tens of milliseconds







- Users ~ tens of millions
- Pages ~ hundreds of millions
- Ads ~ hundreds of thousands
- Responses are of three types
 - Click, Post-click conversion, Post-view conversion
 - Each needs a separate model
- Billions of <user, page, ad> records per day along with response observed
- Privacy policy limits amount of historical data to be used in prediction
- Response rates are non-stationary
 - Trust recent history more

Response Prediction Problem

- Notation:
 - -Page: (i, X_p) X_p = page features
 - -Ad: (j, X_a) X_a = Ad features
 - -User: (k, X_u) X_u = user features
 - -Response: Tries = N_{ijk} , Success = S_{ijk}
- Goal is to predict response rates for each cell P(j|i,k)

• MLE:
$$\hat{P}(j|i,k) = \frac{S_{ijk}}{N_{ijk}}$$



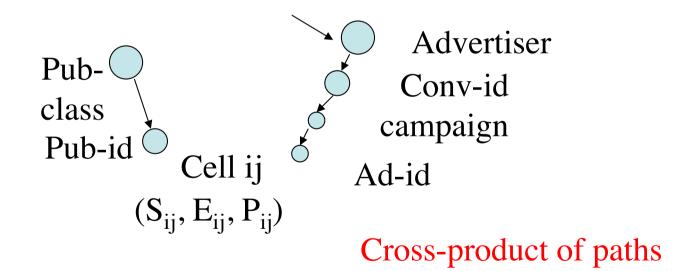
- Sparsity:
 - Too many combinations, most cells have $N_{ijk}=0$
 - High dimensional categorical variables, e.g. In CLICK data, 100M cells
 - 'cold-start' problem
 - If not zero, most cells have small tries
- Rare response:
 - Response rates are extremely rare
 - 0 in 100 is not the same as 0 in 100,000
- Imbalanced sample size
 - N_{ijk} in cells have huge variation
- Smoothing to perform small sample corrections is important
- How do we perform such corrections in a scalable way?



- When N_{ijk} is 'sufficiently' large, trust MLE
- For small N_{ijk} ,
 - Collapse cells based on features and predict from the aggregates
 - Use hierarchical information for aggregation and predict by "falling back"
 - Use smoothing
 - Other statistical corrections



 Assuming two hierarchies (Publisher and advertiser)





- Baseline
 - Logistic Regression
- Decision Tree
 - Learnt hierarchy based on predictive-ness of attributes, then smoothing / corrections
- LMMH [D. Agarwal et. al., ACM SIGKDD 2010]
 - Natural hierarchy of ads and pages
- Collaborative filtering with hierarchies



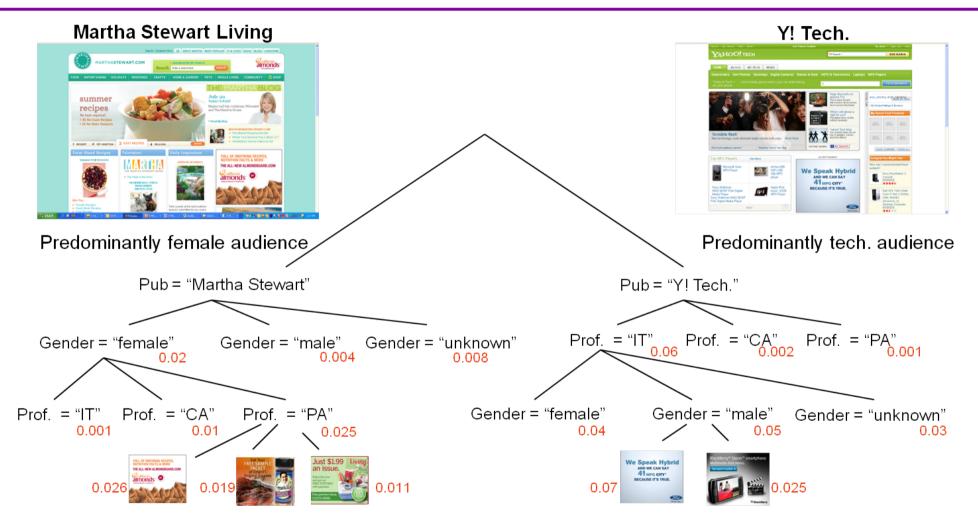
$$\log \frac{p}{1-p} = \sum_{i,j,k} w X_{u,p,a}$$

- Use singleton features only
- Use conjunction features
 - Need hashing trick to reduce dimensionality [Weinberger et. Al, ICML 2009]
- Performs poorly: Approximating in the non-linear region



- Each record is labeled 'succ' or 'no-succ'
- Tree induction with gain ratio as the splitting criterion
- Shrinkage: Child's estimate is shrunk towards the parent
- Return from the parent for cold-start
- Runs on Grid (Map-Reduce), model refreshed periodically





DT - Learned hierarchy, tree induction on ad, publisher, user attributes

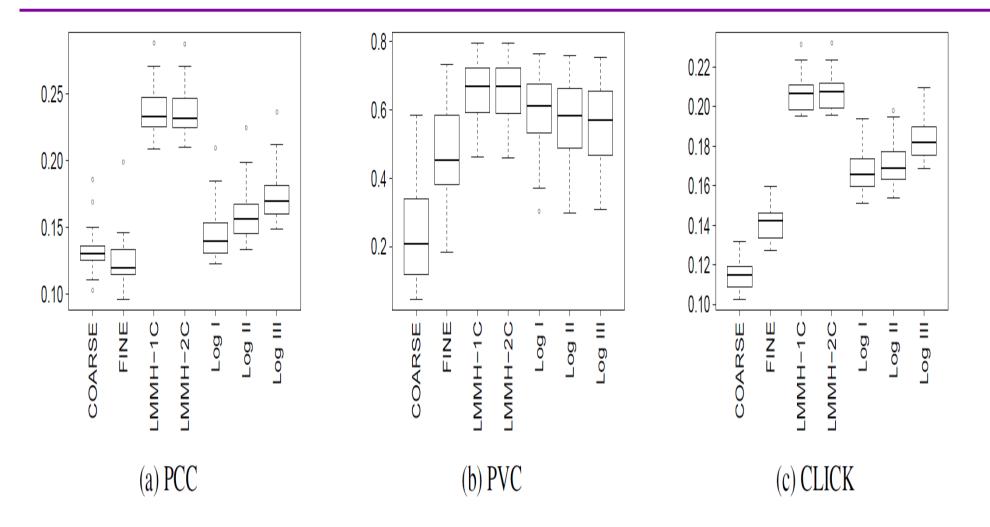
EXAMPLE 1 LMMH (Agarwal et. Al: ACM SIGKDD 2010)

- 3-stage log-linear model
 - Stage 1: Feature based only, uses GLMM
 - e.g. pub category, creative category, daypart,...
 - Stage 2: Clustering data matrix elements
 - through multi-clustering : extension of SIGKDD 07 work
 - E.g. features 1(pub clust =1, creative cluster= 2))
 - Stage 3: corrections using multiple hierarchies
 - Sparse solutions through a new penalty
 - E.g Publisher x Adv hierarchy + daypart x Adv hierarchy



- CLICK [~90B training events]
- PCC (~.5B training events)
 - Conversion only through click
- PVC Post-View conversions (~7B events)
 - Cookie gets augmented with pixel and triggers success
- Features
 - User, pub and ad features
 - 2 hierarchies (publisher and advertiser)

Accuracy: Average test loglikelihood

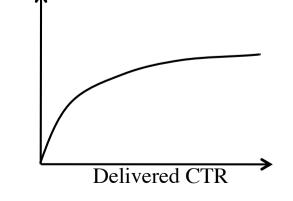


What if prediction still goes wrong?

- Erroneous prediction can cause auction to degenerate
- Risk mitigation is needed
- Allocate a budget proportional to historical number of successes
 - Decrement every time the ad is shown
 - Stop when there is no budget left
 - Refresh budget periodically
- Principle: "Throttle" un-tested ads until they (slowly) prove themselves
- Note: Allocation rule no longer just (max eCPM) in auction



- We talked about
 - -CPM (advertiser bears the risk)
 - -CPC, CPA (Publisher bears the risk)
- Any scheme which can balance this?
 - -dCPM (dynamic CPM)



Things we did not talk about

- Guaranteed delivery display!
- How do advertisers bid?
- Behavioral targeting
- Social targeting
- Layout optimization
- Social sharing of Ads
 - Do influencers affect product buying? {Bhatt et. AI – CIKM 2010}
- Many many others

Wext Gen": Social Targeting, Chunked Rewards



Product Adoption in Large-Scale Social Networks

Rushi Bhatt, Vineet Chaoji, Rajesh Parekh

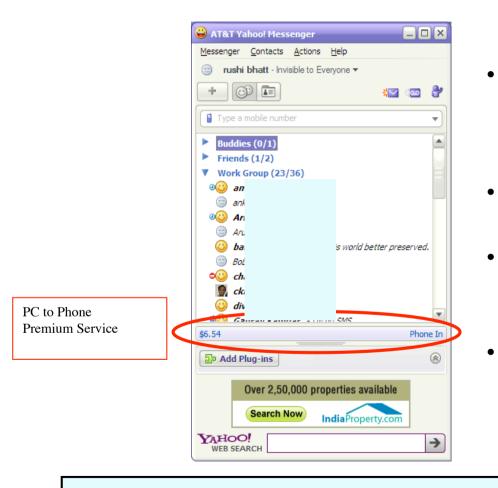


- What are the correlates of adoption spread?
 - –Are high-degree users "different"?
 - -Are neighborhoods predictive?
- How do we improve uptake?
 - Do social attributes provide a lift?
 - -Is neighborhood targeting a good idea?

Spread of Premium Service Adoption Through a Network

Case Study: Adoption Spread in the PC to Phone Premium Service



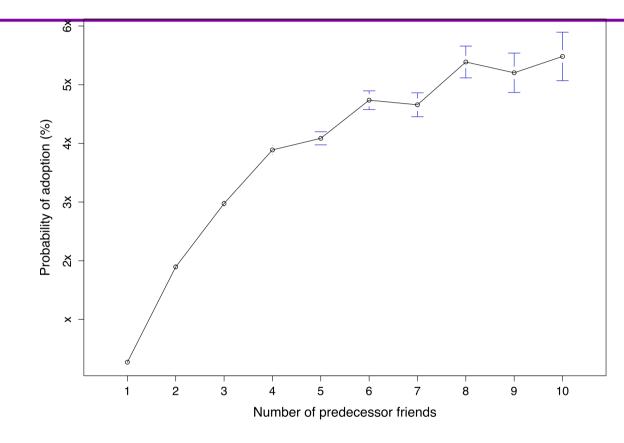


Social Graph

- IM users and their friendship network
- O(100M) nodes, O(1B) edges
- Behavior
 - Granular events: page views, searches, search result clicks, ad views, ad clicks
 - IM usage: messages sent, login days, ...
- Demographic
 - Gender, Age
- Geographic (from IP address)
 - Login country
 - Granular DMA level information
- Premium Service
 - PC 2 Phone subscription

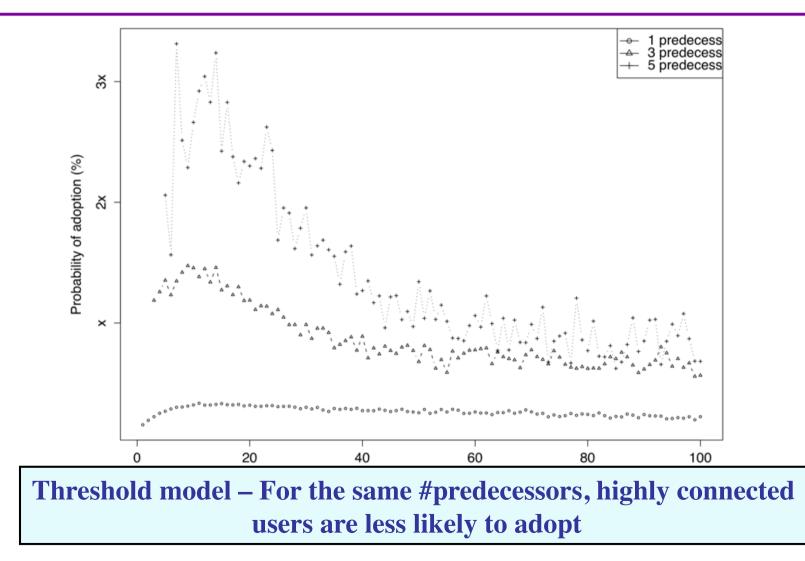
Low baseline adoption rates



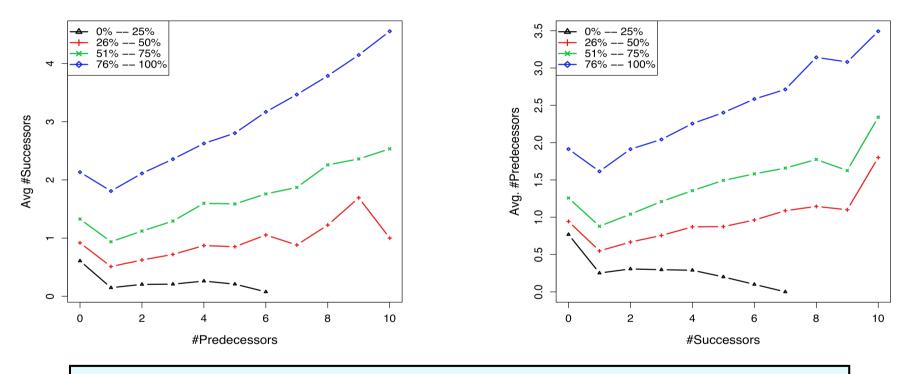


More friends adopting improves chances of adoption

High-degree users are harder to convert



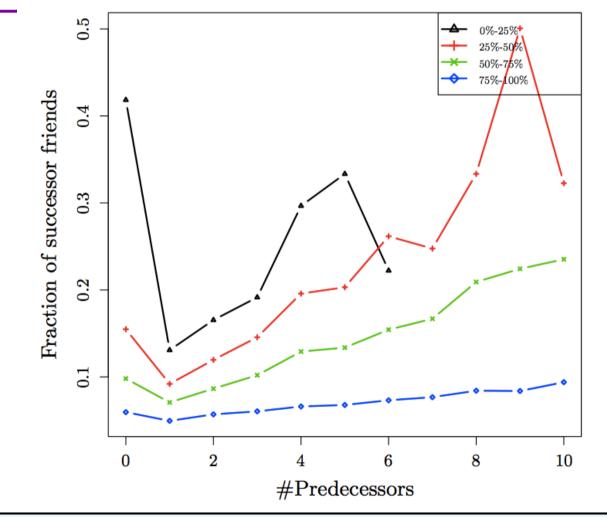
Are High Degree Users Influencers?



If high degree → influencer, then there should be difference in #predecessors & #successors

Also, Anagnostopoulos et al. '08, Dodds & Watts '07

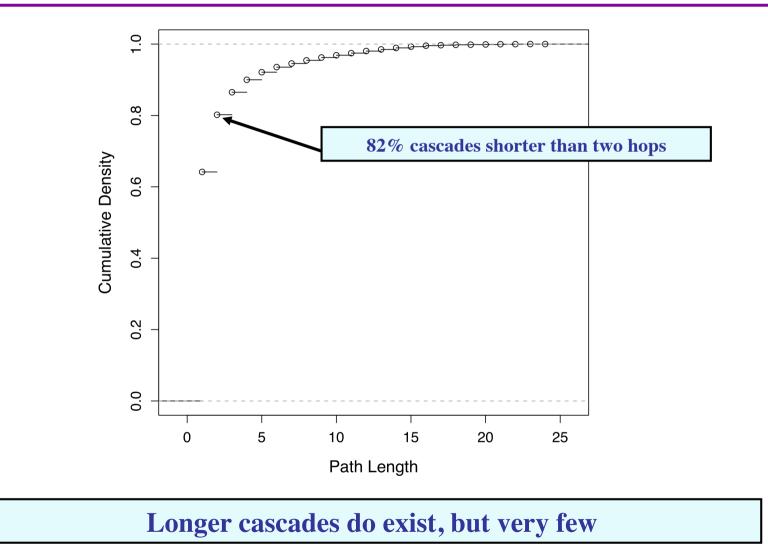




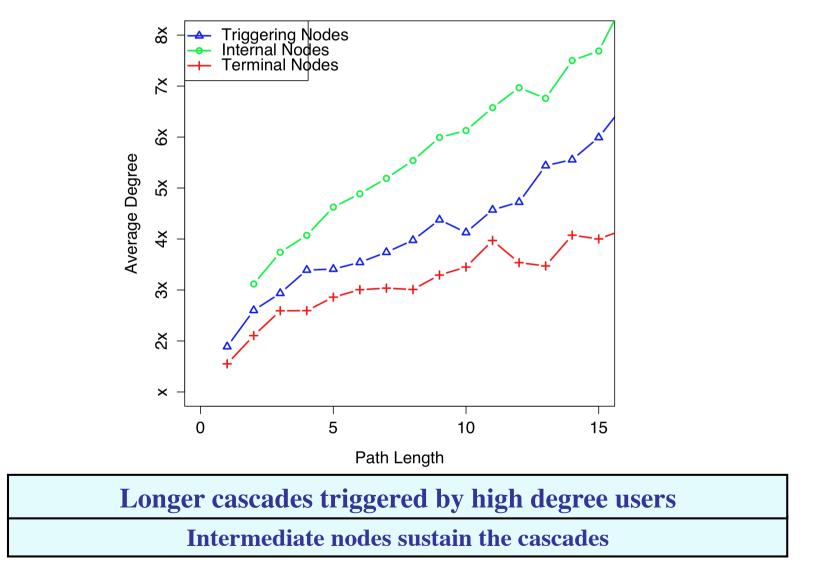
Successors per user reached lower for high degree users [Dodds & Watts '07, also Kitsak et al. '10]

Yahoo! Labs, Bangalore

Adoption Spread is Mostly Local Influence is not Far Reaching



Adoption Spread by Internal Nodes



Predicting Future Adoption

Predict future adoptions, target the likely adopters through messaging

• Direct:

- Identify individuals with high probability of adoption
- Message: "Sign-up now to receive 100 free minutes"



Social Neighborhood:

- Identify adopters in *prime* social neighborhoods
- Message: "Refer a friend: Get 100 free minutes per adopting friend"



Yahoo! Labs, Bangalore

Model to Predict Adoption

Social Neighbourhood:

Premium friends
Premium friends that are linked

Total number of friends Number of different countries your friends belong to Activity:

PC-to-PC CallsIMs Sent# Friends added

logins

Demographic Age Gender

Geographic Originating Country

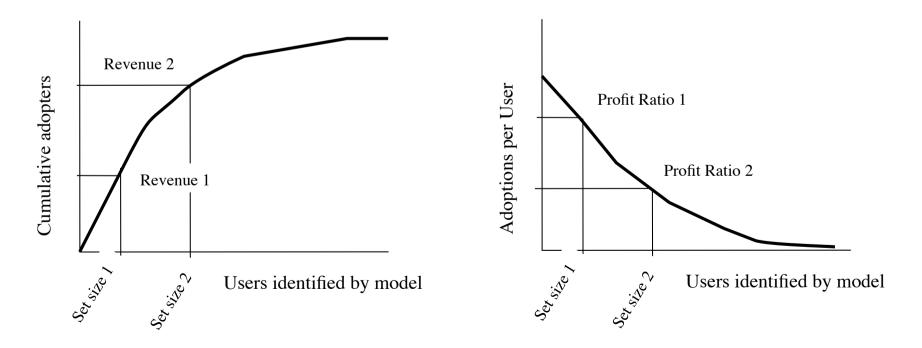
- Target variable:
 - Direct marketing: Binary variable indicating adoption during training period
- Train a Decision Tree

Training Period:Testing Period:User features till M_i User features till M_{i+1} Adoption in M_{i+1} Adoption in M_{i+2} M_i M_{i+1}



- Metric 1: Cumulative coverage
 - Good if there is a large number of adoptions from a small target pool
 - Does not factor in the cost of targeting users

- Metric 2: Adoptions per user
 - Good when we have the highest adoptions per targeted user
 - Factors in the cost of targeting to each user
 - Helps to decide the *right* incentives for each targeted user

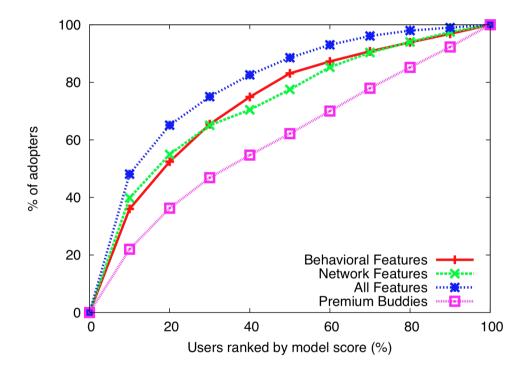


Yahoo! Labs, Bangalore



- # Premium predecessors
- Ego-features: User's own behavior
- Social-features: Behavior of one's friends
- Ego+Social

Direct Targeting

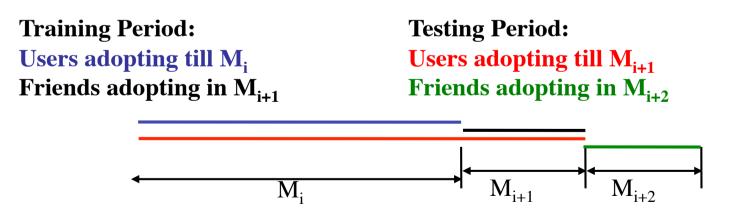


Feature	Relative Importance Score
country	44.76
pc2pc	25.81
prem_bdy	6.32
fringe	6.03
ten_cat	4.51
gender	2.25
age_cat	2.20
n_logins	1.92
n_friends	1.51
buddy_countries	1.27
reach_bdy	1.00

• Combined user and behavioral features best for direct targeting [Also, Hill et al. '06]



- Given a set A of adopters
 - Define $\sigma(A)$ as the cumulative number of future adoptions among friends of A (over a specified time period)
- Target variable: Identify the set A of adopters that maximizes $\sigma(A)$
- Approach
 - Train a regression model (Gradient Boosted Decision Tree) to predict $\sigma(A)$
 - Rank order adopters in descending order of $\sigma(A)$



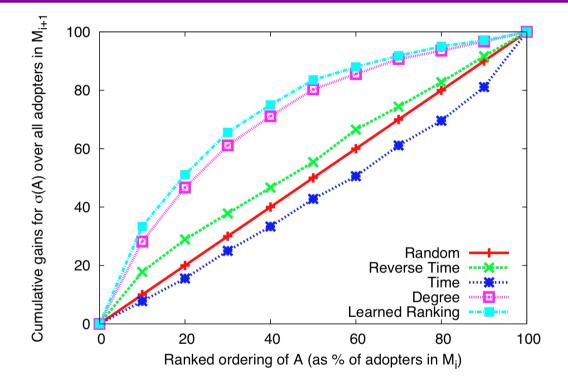


- Earliest-first
- Latest-first
- Most-connected (!)
 - Enjoys advantage: even random adoption around them will yield highest

#successors

Learned estimates





 Learned ranking better than all heuristics

Yahoo! Labs, Bangalore



- Correlation or causation?
 - Strong correlation in adoption of friends observed from data.
 Does it mean adoptions are induced by social neighborhood?
- Response rates (probability of adoption) are assumed to be same for direct vs. social neighborhood targeting
 - Adoptions per targeted user may be different for the two schemes
- Social neighborhood targeting expects users to recruit their friends
 - Target identification is "crowd sourced" to selected users in the neighborhood



- Neighborhoods, not Individuals (!)
 - Most models already allow this (e.g., IC, Threshold)
- Behavior, Demographics, Geography, Social Neighborhood: All matter
- Both targeting methods better than well-established heuristics
 - Social targeting: Assumes that users will select and recruit friends with right incentive
 - Direct targeting: Useful to "start off" neighborhoods that are sparse in adoption





Thank you!

Ad Selection with a Chunked Price Model

Narayan Bhamidipati, Rushi Bhatt, Michael Grabchak (Cornell)

STRATEGIC DATA SOLUTIONS

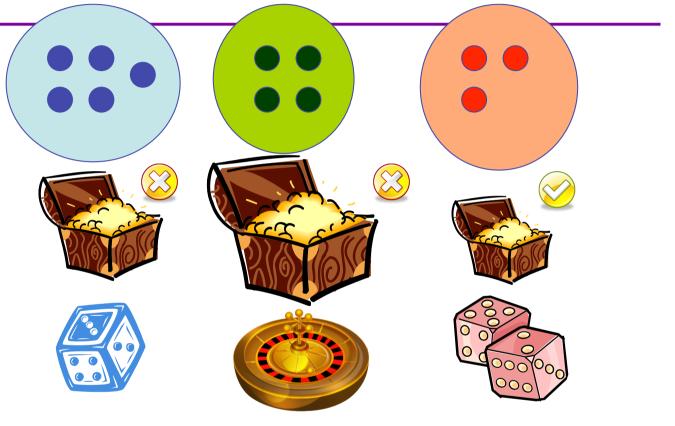
Chunked Price Model: The Setup

Goal: #successes needed

Reward: Payout on achieving goal

Probability:

of success in an attempt



Time: #attempts



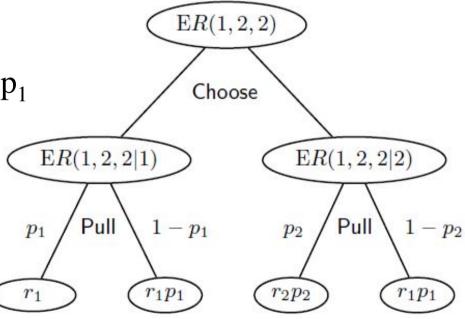
- At each time $1 \le t \le T$
 - decide which ad to show
 - observe the outcome (click or no click)
 - revise the goals
 - repeat
- In such a way that total (expected) revenue is maximized at time T
- Obviously, once a goal for an ad is met, that ad is never shown again



- Let n₁=1, n₂=2, and T=2,
- Also, let $r_1 p_1 < r_2 p_2$
- ER(1,2,2) = max{ ER(1,2,2|1), ER(1,2,2|2)}

> where,

- $ER(1,2,2|1) = p_1r_1 + (1-p_1)r_1p_1$
- $ER(1,2,2|2) = p_2r_2p_2 + (1-p_2)r_1p_1$
- Complexity: O(4^T)





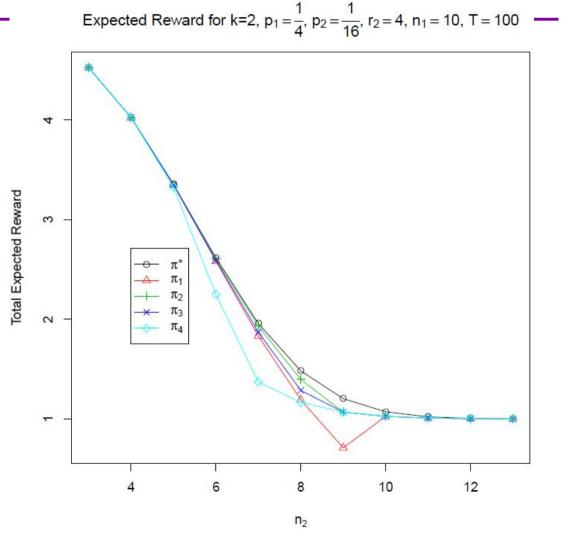
- For each ad, define an index that
 - Considers only ads with unattained but attainable goals
 - Increases with p_i and r_i , decreases with n_i .
 - Is a scalar multiple of r_i .
- Some indices:
 - $r_i p_i / n_i$: continues showing the same ad
 - $r_i p_i / n_i P(n_i \text{ in } T)$: depends on T also
 - $r_i P(n_i \text{ in } T)$: simplified, yet feasible



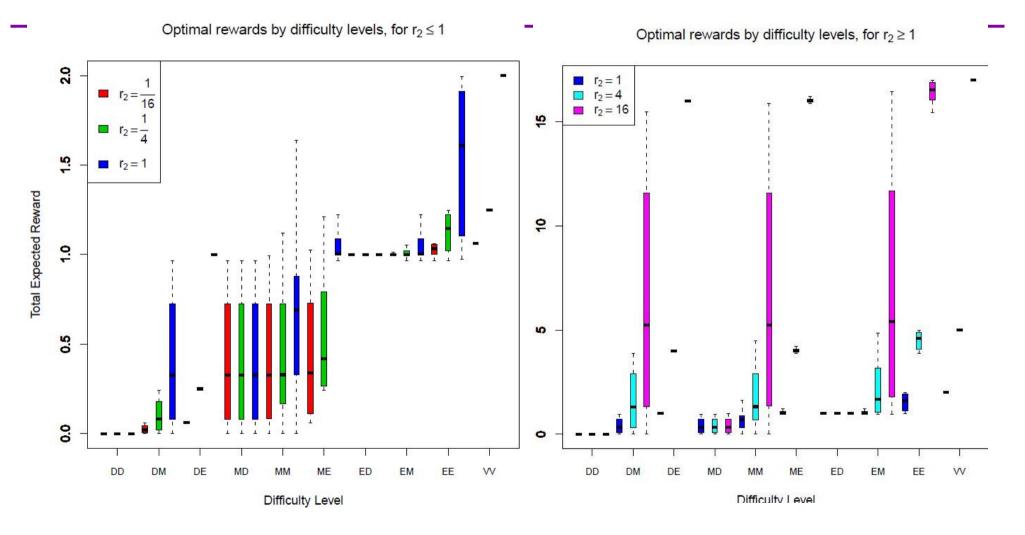
- Make use of the parallels with Stochastic Knapsack Framework
 - Items = ads,
 - random weight W_i = #attempts to attain goal
- Introduce artificial policies like
 - $-\gamma_0$ = always show the ad with max exp reward
 - $-\gamma_7$ = choose the better of γ_0 and $r_i p_i / n_i$.
- Obtain a 3-approximation
 - under mild assumptions: $P(n_i \text{ in } T) \ge \frac{1}{2}$

Optimal vs. Greedy Performance

- Algorithms are much closer to optimal
- Identical to optimal in certain regions
- Significantly lower for some cases

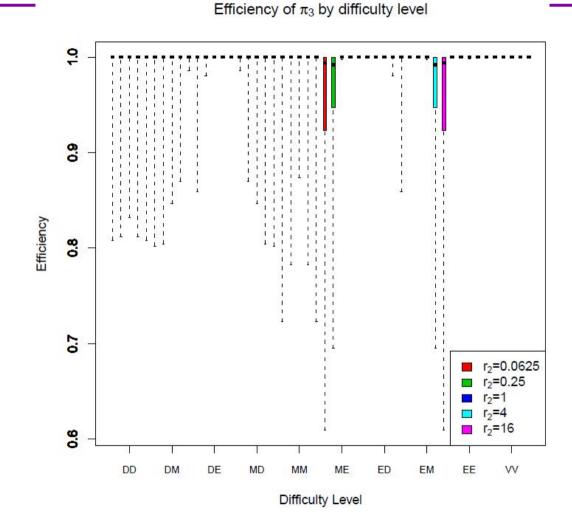


Complete Enumeration: Optimal





- Two ads
- Several combinations of
 - Goals
 - Rewards
 - Probabilities
- Segregated by difficulty levels





- Once the next ad to be shown is determined
 - Need to bid for it in the NGD system
 - Bid should be proportional to the value the ad is supposed to bring
 - A missed opportunity would imply one less attempt available
 - Maximize profits by optimizing bid prices