

# Vectorlike Quarks at the LHC

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with T.Mandal, S.Mitra, R.Tibrewala [arXiv:1107.4306, PRD84 (2011) 055001]

with T.Mandal, S.Mitra, G.Moreau [arXiv:1306.2656]

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# Talk Outline

- Vector-like fermions we study
  - $b'_{(-1/3)}$ ,  $t'_{(2/3)}$ ,  $\chi(5/3)$       ( $t' \equiv T$ )
    - Warped-space (Randall-Sundrum) model
    - Model independent whenever possible
- LHC Double and Single Resonant channels
  - Identify promising channels
  - Find luminosity required for discovery

# Vectorlike $\psi$

- Vectorlike fermions:

- both  $\chi$  and  $\chi^c$  present in the theory
- can write vectorlike mass term  $\mathcal{L} \supset M \chi \chi^c + h.c.$

Vectorlike fermions	Chiral (4-gen) fermions
$M$ ok with Gauge Symmetry	$M$ only after EWSB i.e. $\langle H \rangle$
can be arbitrarily heavy	Landau pole in Yukawa coupling
CC + NC tree-level decays	only CC tree-level decays
loops decoupling	some loops nondecoupling

# EWSB induced mixing $\implies$ Tree-level NC Couplings

Consider  $t' \equiv T$  and  $b'$

- $T_L b_L W^\pm$  and  $b'_L t_L W^\pm$  CC couplings
- In Yukawa coupling  $\langle \Sigma \rangle = v \implies t \leftrightarrow T, b \leftrightarrow b'$  mixing

- $\mathcal{L}_{\text{mass}} \supset \begin{pmatrix} t_L & t'_L \end{pmatrix} \begin{pmatrix} m_t & 0 \\ \tilde{m} & M_T \end{pmatrix} \begin{pmatrix} t_R \\ t'_R \end{pmatrix} + \begin{pmatrix} b_L & b'_L \end{pmatrix} \begin{pmatrix} m_b & 0 \\ \tilde{m}_b & M_{b'} \end{pmatrix} \begin{pmatrix} b_R \\ b'_R \end{pmatrix} + h.c.$

- leads to NC couplings  $t'tZ, t'th$  and  $b'bZ, b'bh$  also

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    - leads to NC couplings  $t'tZ, t'th$  and  $b'bZ, b'bh$  also
- VL Tree-level Decays
  - $b' \rightarrow tW, b' \rightarrow bZ, b' \rightarrow bh$
  - $T \rightarrow bW, T \rightarrow tZ, T \rightarrow th$
  - $\chi \rightarrow tW$

# Warped Model

SM in background 5D warped AdS space

[Randall, Sundrum '99]

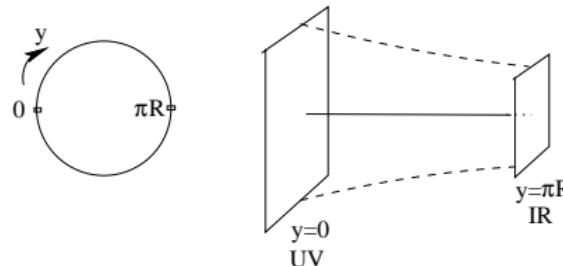
$$ds^2 = e^{-2k|y|}(\eta_{\mu\nu}dx^\mu dx^\nu) + dy^2$$

$Z_2$  orbifold fixed points:

- Planck (UV) Brane
- TeV (IR) Brane

$R$  : radius of Ex. Dim.

$k$  : AdS curvature scale ( $k \lesssim M_{Pl}$ )



Hierarchy prob soln:

- IR localized Higgs :  $M_{EW} \sim k e^{-k\pi R}$  : Choose  $k\pi R \sim 34$ 
  - Gauge-theory dual is a composite Higgs model

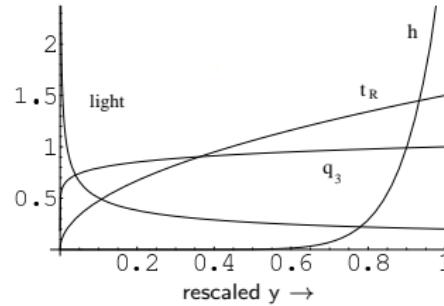
# Explaining SM mass hierarchy

Bulk Fermions explain SM mass hierarchy

[Gherghetta, Pomarol 00][Grossman, Neubert '00]

$$\mathcal{L}_{Yuk}^{(5)} \supset \sqrt{|g|} \left\{ \textcolor{red}{c_L} k \bar{\psi}_L \psi_L + \textcolor{red}{c_R} k \bar{\psi}_R \psi_R + (\lambda_5 \bar{\psi}_R \psi_L H + h.c.) \right\}$$

$$\Psi_L(x, y) = \frac{e^{(2-c)ky}}{\sqrt{2\pi R N_0}} \Psi_L^{(0)}(x) + \dots$$



# AdS/CFT Correspondence

## AdS/CFT Correspondence

[Maldacena, 1997]

- A classical supergravity theory in  $AdS_5 \times S_5$  at weak coupling is **dual** to a 4D large-N CFT at strong coupling
- The CFT is at the boundary of  $AdS$  [Witten 1998; Gubser, Klebanov, Polyakov 1998]

$$Z_{CFT}[\phi_0] = e^{-\Gamma_{AdS}[\phi_0]}$$

$$\mathcal{L} \supset \int d^4x \mathcal{O}_{CFT}(x) \phi_0(x)$$

Eg:  $\langle \mathcal{O}(x_1) \mathcal{O}(x_2) \rangle = \frac{\delta^2 Z_{CFT}[\phi_0]}{\delta \phi_0(x_1) \delta \phi_0(x_2)}$   
with  $Z_{CFT}$  given by the RHS

$\Gamma_{AdS}[\phi]$  supergravity eff. action

$\phi(y, x)$  is a solution of the EOM ( $\delta \Gamma = 0$ )  
for given bndry value  $\phi_0(x) = \phi(y = y_0, x)$

# 4D Duals of Warped Models

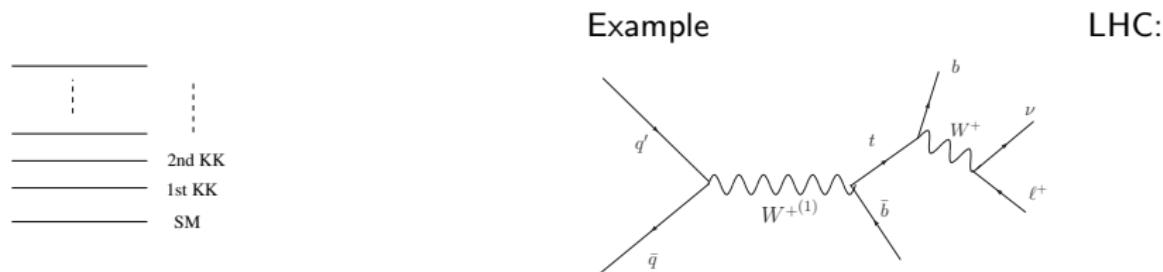
[Arkani-Hamed, Porrati, Randall, 2000; Rattazzi, Zaffaroni, 2001]

- Dual of Randall-Sundrum model **RS1 (SM on IR Brane)**
  - Planck (UV) brane  $\implies$  UV Cutoff; Dynamical gravity in 4D CFT
  - TeV (IR) brane  $\implies$  IR Cutoff; Conformal inv broken  $\lesssim$  TeV
    - All SM fields are composites of the CFT
- Dual of Warped Models with **Bulk SM**
  - UV localized fields are elementary
  - IR localized fields (Higgs) are composite
    - 4D dual is Composite Higgs model [Georgi, Kaplan 1984]
    - Shares many features with Walking Extended Technicolor
  - Partial Compositeness
    - AdS dual is weakly coupled and hence calculable!
  - KK states are dual to composite resonances

# Kaluza-Klein (KK) tower

## Kaluza-Klein (KK) decomposition

- 5D (compact) field  $\leftrightarrow$  Infinite tower of 4D fields
- Look for this tower
  - at the LHC
  - in FCNCs



Look for heavy Kaluza-Klein (KK) states : KK  $h_{\mu\nu}^{(1)}$ ,  $g_\mu^{(1)}$ ,  $W_\mu^{(1)}$ ,  $Z_\mu^{(1)}$ ,  $b_\alpha^{(1)}$ , ...  
 LEP precision electroweak constraints  $\Rightarrow W_\mu^{(1)}, Z_\mu^{(1)} \gtrsim 2$  TeV

# Precision ElectroWeak Constraints



## Precision Electroweak Constraints ( $S$ , $T$ , $Zb\bar{b}$ )

- Bulk gauge symm -  $SU(2)_L \times U(1)$  (SM  $\psi$ , H on TeV Brane)
  - T parameter  $\sim (\frac{v}{M_{KK}})^2 (k\pi R)$  [Csaki, Erlich, Terning 02]
  - S parameter also  $(k\pi R)$  enhanced
- AdS bulk gauge symm  $SU(2)_R \Leftrightarrow$  CFT Custodial Symm [Agashe, Delgado, May, Sundrum 03]
  - T parameter - Protected
  - S parameter -  $\frac{1}{k\pi R}$  for light bulk fermions
  - Problem:  $Zb\bar{b}$  shifted
- 3rd gen quarks (2,2) [Agashe, Contino, DaRold, Pomarol 06]
  - $Zb\bar{b}$  coupling - Protected
  - Precision EW constraints  $\Rightarrow M_{KK} \gtrsim 2 - 3$  TeV

[Carena, Ponton, Santiago, Wagner 06,07] [Bouchart, Moreau-08] [Djouadi, Moreau, Richard 06]

# Warped Bulk Gauge Group

[Agashe, Delgado, May, Sundrum '03]

Bulk gauge group :  $SU(3)_{QCD} \otimes SU(2)_L \otimes SU(2)_R \otimes U(1)_X$

- Gauge Symmetry breaking:

- By Boundary Condition (BC):  $A(x, y) : (-, +)$  BC:  $A|_{(y=0)} = 0 ; \partial_y A|_{(y=\pi R)} = 0$

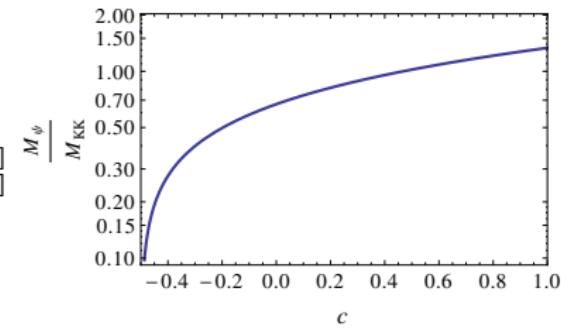
- $SU(2)_R \times U(1)_X \rightarrow U(1)_Y$

- By VEV of IR localized Higgs  $\text{Higgs } \Sigma = (2, 2)_0$

- $SU(2)_L \times U(1)_Y \rightarrow U(1)_{EM}$

# Warped Fermions

- SM fermions :  $(+, +)$  BC  $\rightarrow$  zero-mode
- “Exotic” fermions :  $(-, +)$  BC  $\rightarrow$  No zero-mode
  - 1<sup>st</sup> KK vectorlike fermion
- Typical  $c_{t_R}, c_{t_L} : (-, +)$  top-partners “light”
  - $c$  : Fermion bulk mass parameter
  - [Choi, Kim, 2002] [Agashe, Delgado, May, Sundrum, 03]  
 [Agashe, Perez, Soni, 04] [Agashe, Servant 04]
  - Look for it at the LHC



[Dennis et al, '07] [Carena et al, '07] [Contino, Servant, '08]  
 [Atre et al, '09, '11] [Aguilar-Saavedra, '09] [Mrazek, Wulzer, '09]  
 [SG, Moreau, Singh, '10] [SG, Mandal, Mitra, Tibrewala, '11] [SG, Mandal, Mitra, Moreau : '13]

# Fermion rep : $Zb\bar{b}$ not protected (DT model)

[Agashe, Delgado, May, Sundrum '03]

- Complete  $SU(2)_R$  multiplet
  - $Q_L \equiv (\mathbf{2}, \mathbf{1})_{1/6} = (t_L, b_L)$
  - $\psi_{t_R} \equiv (\mathbf{1}, \mathbf{2})_{1/6} = (t_R, b')$
  - $\psi_{b_R} \equiv (\mathbf{1}, \mathbf{2})_{1/6} = (T, b_R)$ 
    - "Project-out"  $b'$ ,  $T$  zero-modes by  $(-, +)$  B.C.
    - New  $\psi_{VL} : b', T$
- $b \leftrightarrow b'$  mixing
  - $Zb\bar{b}$  coupling shifted
    - So LEP constraint quite severe

# Fermion rep : $Zb\bar{b}$ protected (ST & TT models)

- $Q_L = (2, 2)_{2/3} = \begin{pmatrix} t_L & \chi \\ b_L & T \end{pmatrix}$  [Agashe, Contino, DaRold, Pomarol '06]
  - $Zb_L\overline{b_L}$  protected by custodial  $SU(2)_{L+R} \otimes P_{LR}$  invariance  
 $Wt_L b_L, Zt_L t_L$  not protected, so shifts

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**Two  $t_R$  possibilities:**

① Singlet  $t_R$  (ST Model) :  $(1, 1)_{2/3} = t_R$  New  $\psi_{VL}$  :  $\chi, T$

② Triplet  $t_R$  (TT Model) :

$$(1, 3)_{2/3} \oplus (3, 1)_{2/3} = \psi'_{t_R} \oplus \psi''_{t_R} = \begin{pmatrix} \frac{t_R}{\sqrt{2}} & \chi' \\ b' & -\frac{t_R}{\sqrt{2}} \end{pmatrix} \oplus \begin{pmatrix} \frac{t''}{\sqrt{2}} & \chi'' \\ b'' & -\frac{t''}{\sqrt{2}} \end{pmatrix}$$

New  $\psi_{VL}$  :  $\chi, T, \chi', b', \chi'', t'', b''$

# Yukawa Couplings

## Yukawa Couplings

- No  $Zb\bar{b}$  protection

$$\mathcal{L}_{\text{Yuk}} \supset \lambda_t \bar{Q}_L \Sigma \psi_{tR} + \lambda_b \bar{Q}_L \Sigma \psi_{bR} + h.c.$$

- With  $Zb\bar{b}$  protection

- ST Model  $\mathcal{L}_{\text{Yuk}} \supset \lambda_t \text{Tr}[\bar{Q}_L \Sigma] t_R + h.c.$

- TT Model  $\mathcal{L}_{\text{Yuk}} \supset \lambda_t \text{Tr}[\bar{Q}_L \Sigma \psi'_{tR}] + \lambda'_t \text{Tr}[\bar{Q}_L \Sigma \psi''_{tR}] + h.c.$

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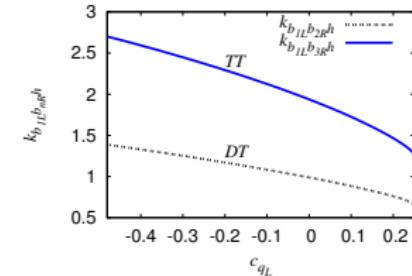
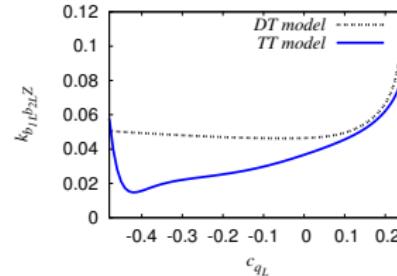
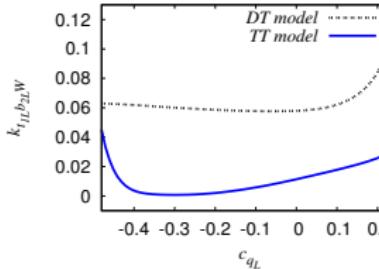
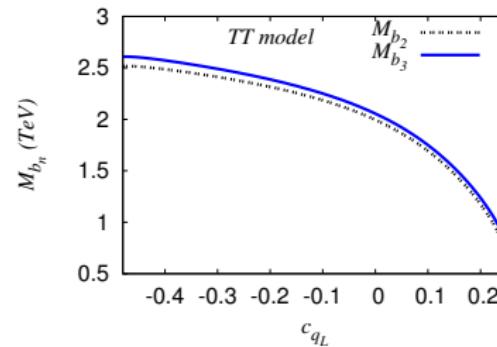
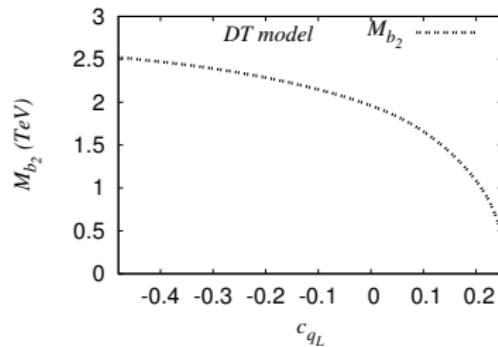
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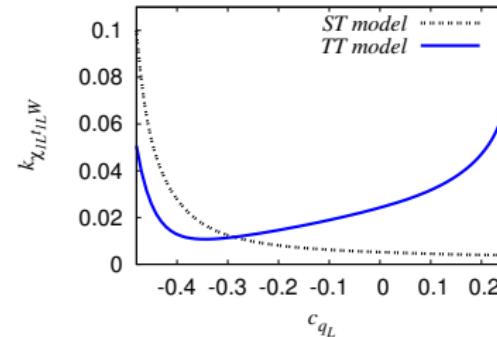
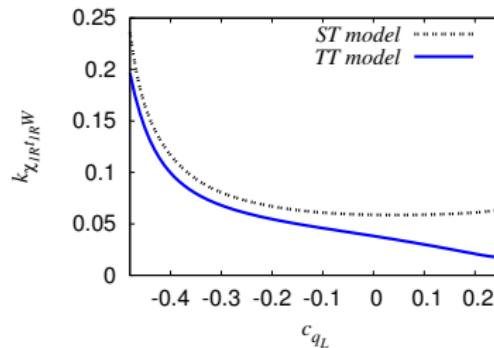
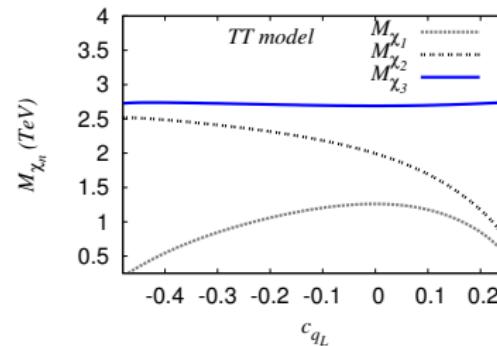
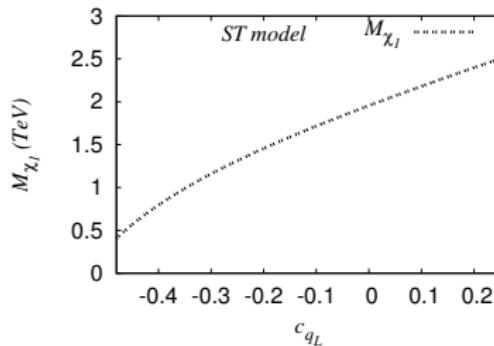
EWSB  $\langle \Sigma \rangle = v$

- Induces  $\psi \leftrightarrow \psi'$  mixing
  - LHC Single production can probe this mixing

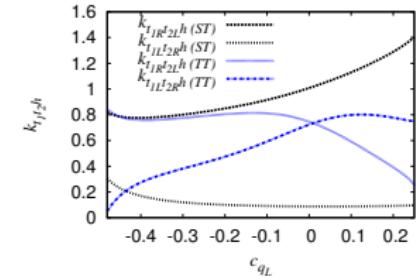
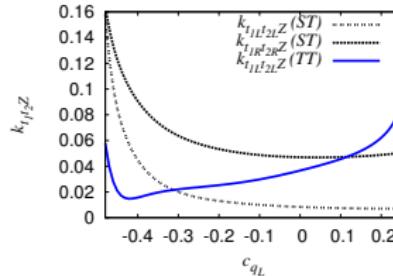
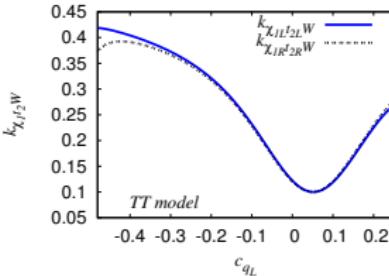
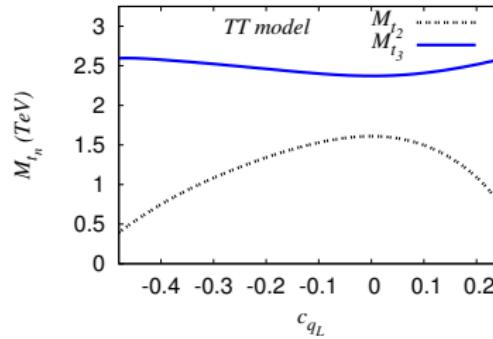
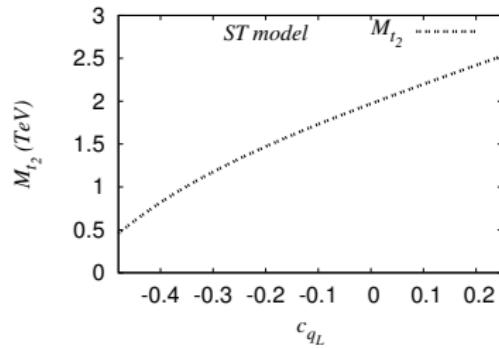
# Warped model $b'$ parameters



# Warped model $\chi$ parameters



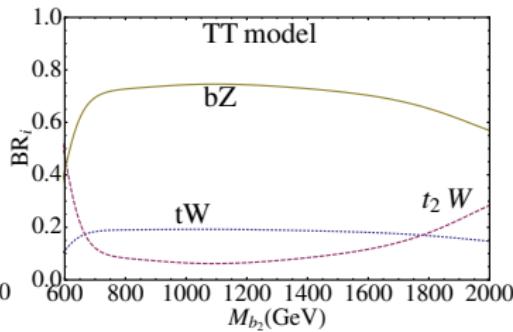
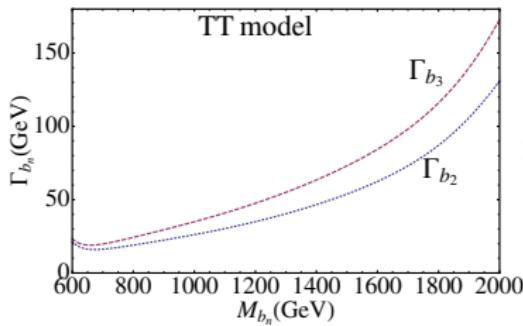
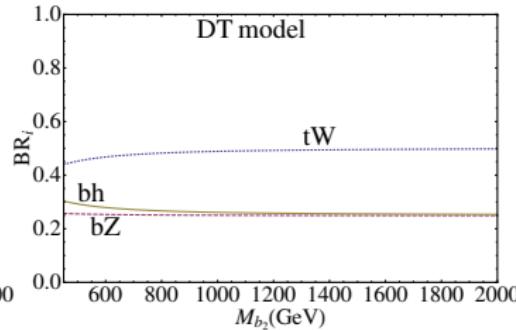
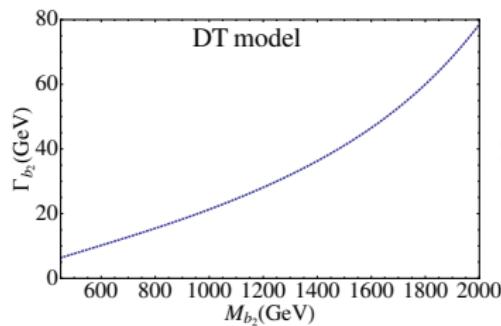
# Warped model $t'$ parameters



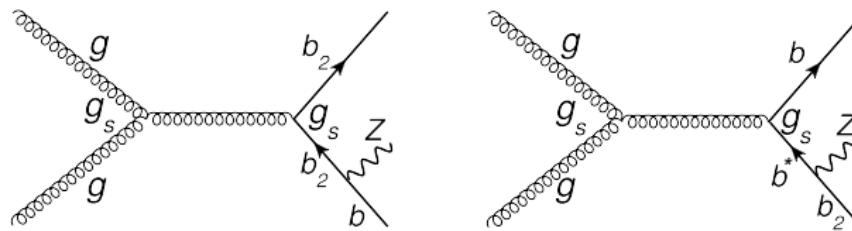
## $b'$ Phenomenology at the LHC

[SG, T.Mandal, S.Mitra, R.Tibrewala, arXiv:1107.4306]  
[SG, T.Mandal, S.Mitra, G.Moreau : arXiv:1306.2656]

# Warped model $b'$ : $\Gamma$ and BR



# $b'$ Single & Double Resonant channels

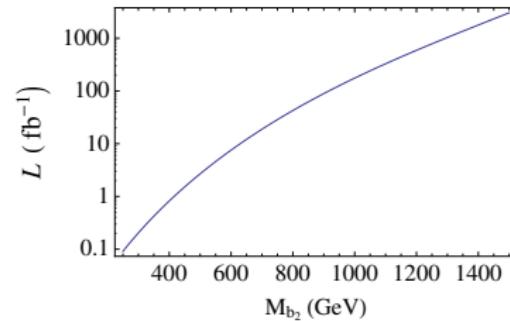
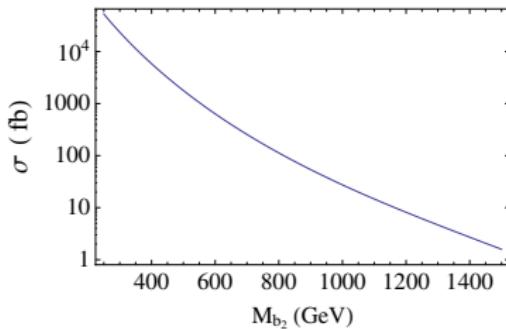


... followed by  $b_2 \rightarrow bZ$

- Both  $b_2$  on-shell : **Double Resonant (DR) channel**
- Only one  $b_2$  on-shell : **Single Resonant (SR) channel**
  - $|M(bZ) - M_{b_2}| \geq \alpha_{cut} M_{b_2}; \quad \alpha_{cut} = 0.05$

# $b'$ Double Resonant

Pair Production :  $pp \rightarrow b'\bar{b}' \rightarrow bZ\bar{b}Z \rightarrow bjj\bar{b}\ell\ell$



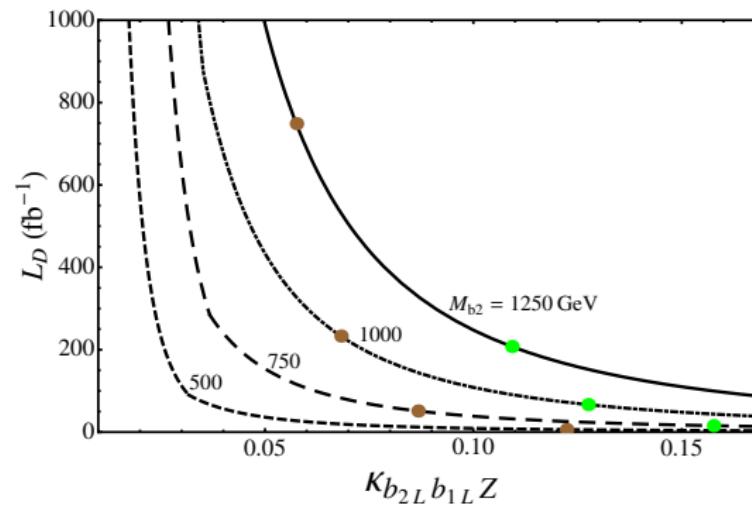
Cuts:

Rapidity:  $-2.5 < y_{b,j,Z} < 2.5$ ,  
Transverse momentum:  $p_{T,b,j,Z} > 25 \text{ GeV}$ ,  
Invariant mass cuts:  
 $M_Z - 10 \text{ GeV} < M_{jj} < M_Z + 10 \text{ GeV}$ ,  
 $0.95M_{b_2} < M_{(bZ)} < 1.05M_{b_2}$ .

# $b'$ Single Resonant - I

Single Resonant :  $bg \rightarrow b'bZ \rightarrow bZbZ \rightarrow bbJJ\ell\ell$

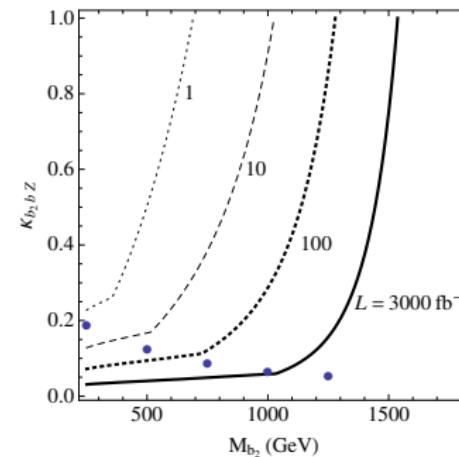
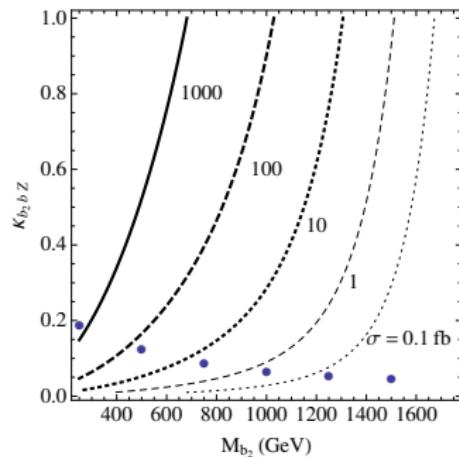
Model Independent LHC-14 reach



Brown dots : DT Model      Green dots : TT Model

# $b'$ Single Production - II

Single Production :  $bg \rightarrow b'Z \rightarrow bZZ \rightarrow bjj\ell\ell$



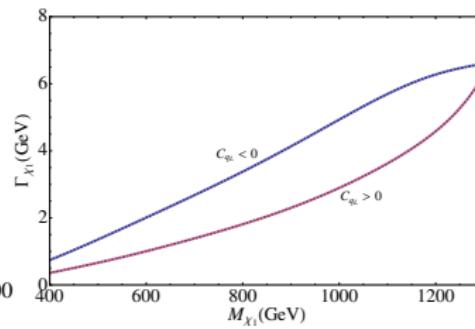
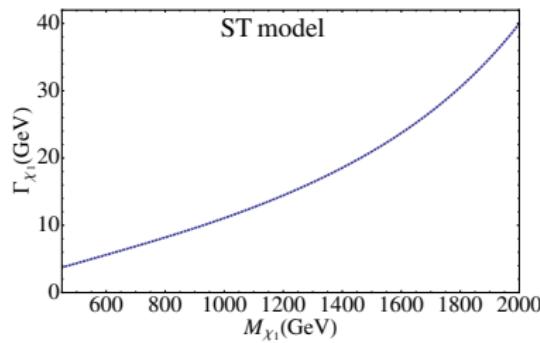
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 Invariant mass cuts:  
 $M_Z - 10 \text{ GeV} < M_{jj} < M_Z + 10 \text{ GeV}$ ,  
 $0.95M_{b_2} < M_{(bZ)} \text{ OR } (bjj) < 1.05M_{b_2}$  .

# $\chi$ Phenomenology at the LHC

[SG, T.Mandal, S.Mitra, G.Moreau : arXiv:1306.2656]

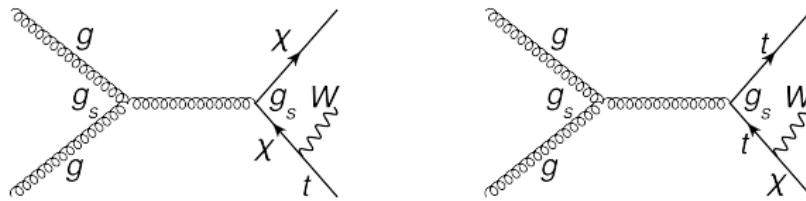
# Warped model $\Gamma_\chi$



ST Model

TT Model

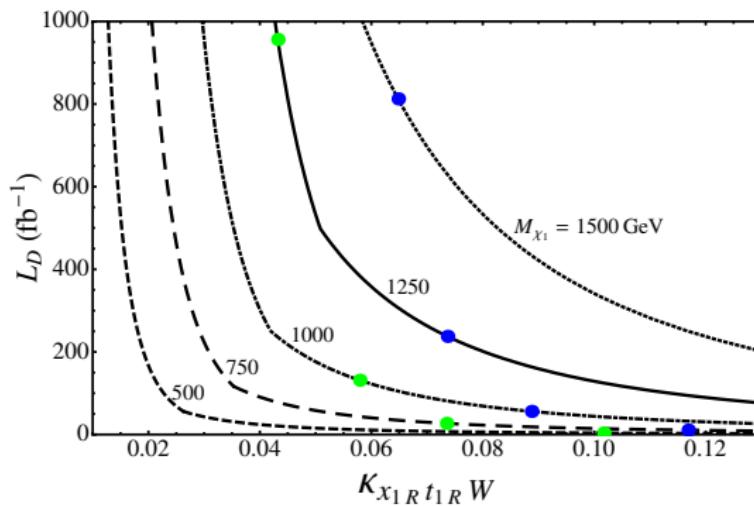
# $\chi$ Double and Single Resonant channels



$pp \rightarrow \chi tW \rightarrow tWtW \rightarrow tWt\ell\nu$

$X$	$M_\chi$ (GeV)	$\sigma_{tot}$ (fb)	$\sigma_{SR}$ (fb)	cuts	S (fb)	BG (fb)	$\mathcal{L}$ (fb <sup>-1</sup> )
$X_1$	500	2406	261.5	Basic	977.5	3.257	-
				Disc.	146.1	0.115	0.826
$X_2$	750	235.5	29.31	Basic	99.99	3.257	-
				Disc.	42.74	0.115	2.824
$X_3$	1000	39.19	5.198	Basic	17.92	3.257	-
				Disc.	11.36	0.115	10.63
$X_4$	1250	8.576	1.231	Basic	4.305	3.257	-
				Disc.	3.226	0.115	37.42
$X_5$	1500	2.188	0.364	Basic	1.235	3.257	-
				Disc.	1.010	0.115	119.5
$X_6$	1750	0.613	0.121	Basic	0.393	3.257	-
				Disc.	0.339	0.115	355.8

# $\chi$ Single Resonant Channel



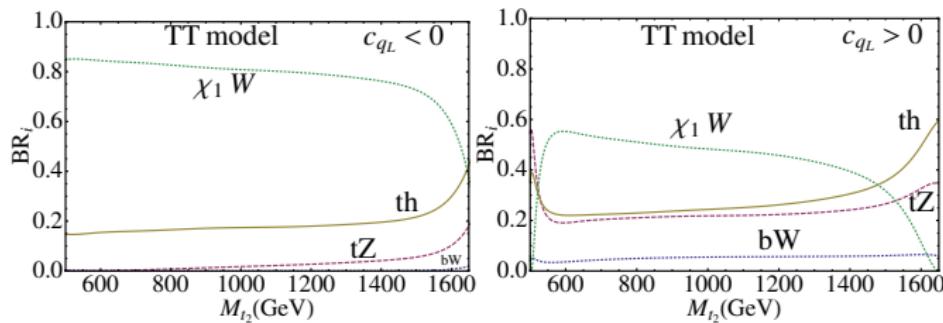
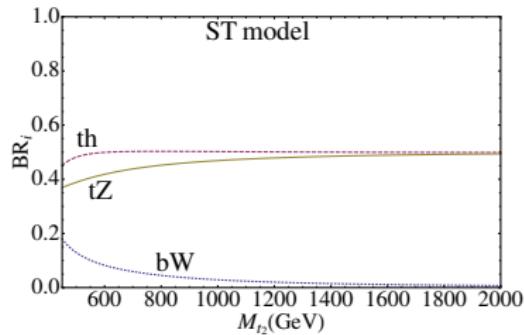
Blue Dots - ST Model    Green Dots - TT Model

## $t'$ Phenomenology at the LHC

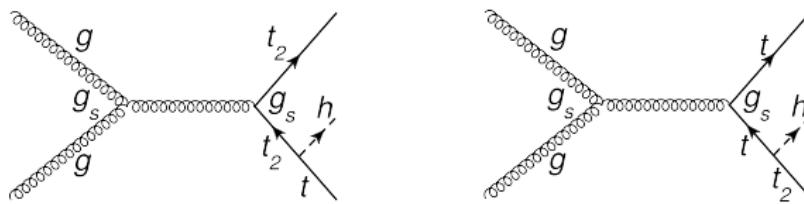
[SG, Tanumoy Mandal, Subhadip Mitra, Gregory Moreau : arXiv:1306.2656]

See also: [Harigaya et al., '12] [Giridhar, Mukhopadhyaya, 2012] [Azatov et al., '12]  
[Berger, Hubisz, Perelstein, '12] [Cacciapaglia et al., '10, '12]

# Warped model $t'$ BR



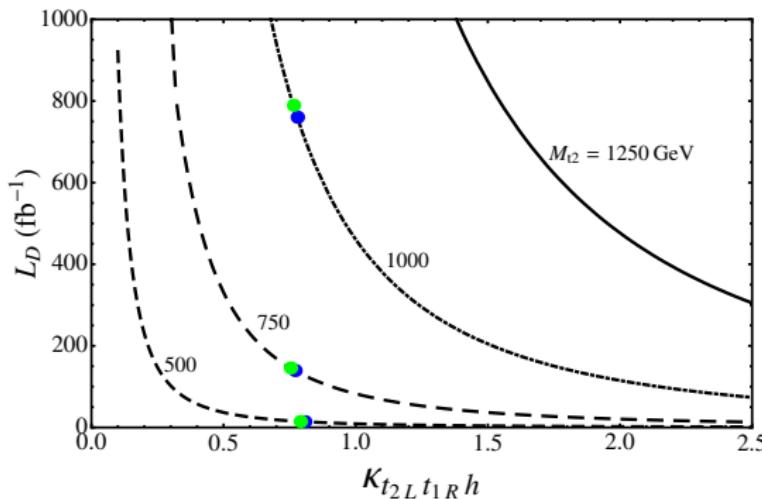
# $t'$ Double and Single Resonant channels



$pp \rightarrow t_2 th \rightarrow thth \rightarrow tb btb b \rightarrow 6~b~4~j$  (4 b-tags)

$T$	$M_{t_2}$ (GeV)	$\sigma_{tot}$ (fb)	$\sigma_{SR}$ (fb)	cuts	S (fb)	BG (fb)	$\mathcal{L}$ (fb $^{-1}$ )
$T_1$	500	1207	223.0	Basic	237.4	102.7	-
				Disc.	52.38	0.389	6.379
$T_2$	750	115.2	18.30	Basic	22.67	102.7	-
				Disc.	13.25	0.389	25.22
$T_3$	1000	18.38	2.715	Basic	3.088	102.7	-
				Disc.	2.421	0.389	138.0
$T_4$	1250	3.821	0.590	Basic	0.477	102.7	-
				Disc.	0.415	0.389	1889.2

# $t'$ Single Resonant channel



Blue Dots - ST Model    Green Dots - TT Model

# Conclusions

- Vector-like quarks
  - have NC (and CC) tree-level decays
  - could be much lighter than  $V_\mu^{KK}$  in warped models
- Identified promising DR and SR channels
  - SR can probe EW couplings
- 14 TeV LHC with  $\approx 300 \text{ fb}^{-1}$  reach about 1.5 - 2 TeV in DR
- New ATLAS & CMS results
  - limits around  $M_\psi \gtrsim 750 \text{ GeV}$

# BACKUP SLIDES

BACKUP SLIDES

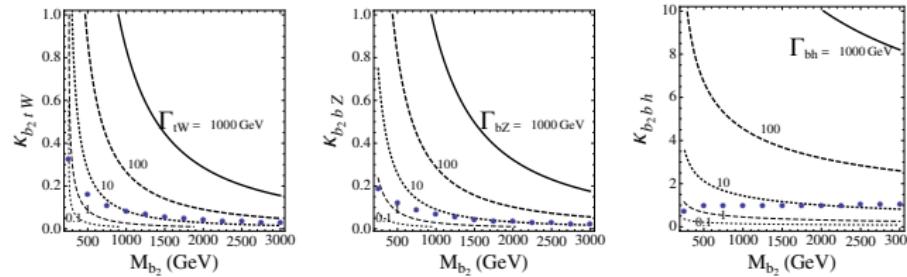
# $b'$ Pair Production Details

$$pp \rightarrow b' \bar{b}' \rightarrow bZ\bar{b}Z \rightarrow bjj\bar{b}\ell\ell$$

$M_{b_2}$ (GeV)	Signal $\sigma_s$ (in fb)		Background $\sigma_b$ (in fb)				$\mathcal{L}$ (fb $^{-1}$ )	
	$bZb\bar{Z}$		$bZb\bar{Z}$		$(bjj\bar{b}Z)_{\text{tot}}$			
	$y, p_T$ cuts	All cuts	$y, p_T$ cuts	All cuts	$y, p_T$ cuts	All cuts		
250	25253	25082	21.804	0.3797	16938	29.52	0.021	
500	171.34	148.69	21.804	0.047	16938	3.74	3.514	
750	14.508	12.221	21.804	0.0097	16938	0.997	42.752	
1000	2.314	1.9214	21.804	0.0027	16938	0.259	271.92	
1250	0.484	0.399	21.804	0.0011	16938	0.048	1310	

$M_{b_2}$ (GeV)	QCD background (in fb)					
	$bj\bar{b}Z$		$bbj\bar{b}Z$		$bbbbZ$	
	$y, p_T$ cuts	All cuts	$y, p_T$ cuts	All cuts	$y, p_T$ cuts	All cuts
250	16790	27.304	255.41	2.7	81.01	1.92
500	16790	3.513	255.41	0.256	81.01	0.194
750	16790	0.958	255.41	0.031	81.01	0.057
1000	16790	0.2514	255.41	0.0052	81.01	0.008

# $b'$ Signature (Model Independent)



Benchmark Points (Model I):

$M_{b_2}$ (GeV)	250	500	750	1000	1250	1500
$\kappa_{b_2 bZ}^L$	0.185	0.121	0.084	0.064	0.051	0.043
$\kappa_{b_2 tW}$	0.322	0.161	0.107	0.080	0.064	0.054
$\kappa_{hb_L b_{2R}}$	0.714	0.937	0.972	0.985	0.990	0.993
$M_{b_2}$ (GeV)	1750	2000	2250	2500	2750	3000
$\kappa_{b_2 bZ}^L$	0.037	0.032	0.029	0.026	0.024	0.022
$\kappa_{b_2 tW}$	0.046	0.040	0.036	0.032	0.029	0.027
$\kappa_{hb_L b_{2R}}$	0.995	0.996	0.997	0.998	0.998	0.998

# $b'$ Single Resonant II Details

$$pp \rightarrow b'Z \rightarrow bZZ \rightarrow bjj\ell^+\ell^-$$

$M_{b'}$ (GeV)	signal $\sigma_s$ (in fb)		background $\sigma_b$ (in fb)				$\mathcal{L}_{\text{SemiLep}}$ (fb $^{-1}$ )	
	$bjjZ$		$(bjjZ)_{EW}$		$(bjjZ)_{QCD}$			
	Primary cuts	all cuts	Primary cuts	all cuts	Primary cuts	all cuts		
250	1017.66	995.86	77.03	10.33	7853.02	867.82	0.66	
500	16.84	15.50	8.81	0.68	419.75	14.11	45.94	
750	1.26	1.14	1.85	0.10	56.26	0.86	551.26	
1000	0.14	0.12	0.47	0.01	12.38	0.05	3399.67	

$M_{b'}$ (GeV)	QCD background (in fb)		
	$bjjZ$	$bjbZ$	$bbbZ$
250	546.36	634.32	17.19
500	10.14	7.76	0.35
750	0.52	0.66	0.03
1000	0.02	0.06	0.002