

# Phenomenology of Extra Dimensions

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*Frontiers In Physics 2013*  
*University of Hyderabad*  
September 2013

# Talk Outline

- Problems in the Standard Model (SM) of particle physics
  - Gauge hierarchy problem
- Extra Dimensional Proposal for solving this
  - Large Extra Dimensions (LED) (aka ADD)
  - Universal Extra Dimensions (UED)
  - Warped Extra Dimensions (WED)
- LHC Signatures



# Standard Model (SM) problems

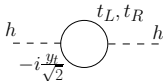
- Gauge hierarchy problem ( $M_{EW} \ll M_{Pl}$ )  
Electroweak scale :  $M_{EW} = 10^3$  GeV    Gravity scale :  $M_{Pl} = 10^{19}$  GeV
  - Higgs sector unstable    (quadratic divergence)
- Fermion mass hierarchy problem ( $m_e \ll m_t$ )
  - Flavor symmetry?
- What is the dark matter
- Inadequate source of CP violation for observed baryon asymmetry
- Cosmological constant problem



# Gauge hierarchy problem in detail

$$\mathcal{L}_{SM} \supset -\frac{1}{2}m_h^2 h^2 + \left(-\frac{y_t}{\sqrt{2}} h \bar{t}_R t_L + h.c.\right) + \dots$$

Higgs mass is not protected by any symmetry!



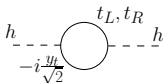
$$\frac{\delta m_h^2}{2} = -\frac{3y_t^2}{8\pi^2} \Lambda^2 \quad (\Lambda \text{ is momentum cut-off})$$

Quadratic divergence!  $\implies$  unnatural (fine-tuning)  
 $m_h = 125 \text{ GeV} \quad ; \quad \Lambda \sim M_{pl} = 10^{19} \text{ GeV}$

# Gauge hierarchy problem in detail

$$\mathcal{L}_{SM} \supset -\frac{1}{2} m_h^2 h^2 + \left( -\frac{y_t}{\sqrt{2}} h t_R \bar{t}_L + h.c. \right) + \dots$$

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 $m_h = 125 \text{ GeV} \quad ; \quad \Lambda \sim M_{pl} = 10^{19} \text{ GeV}$

New physics (BSM) restores naturalness?

Below what scale ( $\Lambda$ ) should it appear?

Fine-tuning measure:  $f_T \equiv \frac{m_h^2}{\delta m_h^2}$

$f_T > 0.1 \implies \Lambda < 2 \text{ TeV}$  (for  $m_h = 120 \text{ GeV}$ )

So expect new physics below 2 TeV scale



# SM problems cured by Physics Beyond SM (BSM) ?

## Some BSM proposals

- Supersymmetry
- Strong dynamics (Technicolor, Composite Higgs)
- **Extra dimensions**
  - Flat extra dims
  - Warped (AdS space) extra dim

5-D gravity theory in AdS  $\overset{\leftarrow}{\text{DUAL}} \overset{\rightarrow}{}$  4-D conformal field theory (CFT)  
AdS/CFT correspondence [Maldacena 97]

- Little Higgs



# Supersymmetry (SUSY)

Transforms Fermions  $\leftrightarrow$  Bosons

Reviews: [Martin] [Dress]

- Minimal Supersymmetric Standard Model (**MSSM**)
  - To every SM particle, add **superpartner** (spin differs by 1/2)  
Particle spectrum doubled



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SUSY solves gauge hierarchy problem

$$\begin{array}{c}
 \begin{array}{c}
 \text{---} h \text{---} \\
 | \\
 \text{---} h \text{---} \\
 \text{---} \text{---} \\
 | \\
 \text{---} h \text{---} \\
 | \\
 \text{---} h \text{---} \\
 | \\
 -i \frac{y_t}{\sqrt{2}}
 \end{array}
 + 
 \begin{array}{c}
 \text{---} h \text{---} \\
 | \\
 \text{---} h \text{---} \\
 \text{---} \text{---} \\
 | \\
 \text{---} h \text{---} \\
 | \\
 \text{---} h \text{---} \\
 | \\
 -i \frac{y_{\tilde{t}}}{2}
 \end{array}
 = 0
 \end{array}$$

$\Lambda^2$  divergence cancelled

[Romesh Kaul 1981, 82]

(Similarly  $h, W^\pm, Z$  divergences cancelled by  $\tilde{\lambda}$ )





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$$\begin{array}{c}
 \text{Feynman Diagram 1: } h \text{---} \text{---} \text{---} h \text{ loop with } t_L, t_R \text{ and vertex } -i \frac{y_t}{\sqrt{2}} \\
 + \\
 \text{Feynman Diagram 2: } h \text{---} \text{---} \text{---} h \text{ loop with } \tilde{t}_L, \tilde{t}_R \text{ and vertex } -i \frac{y_t^2}{2} \\
 = 0
 \end{array}$$

$\Lambda^2$  divergence cancelled

[Romesh Kaul 1981, 82]

(Similarly  $h, W^\pm, Z$  divergences cancelled by  $\tilde{\lambda}$ )

- SUSY  $\implies M_\psi = M_\phi$  ; but experiment  $\implies$  **SUSY broken**
- Lightest SUSY Particle (LSP) stable dark matter (if  $R_p$  conserved)
- Gauge Coupling Unification - SUSY SO(10) GUT



# Large Extra Dimensions (LED, ADD)

[Arkani-Hamed, Dimopoulos, Dvali (ADD), 1998]

- $n$  (compact) space extra dims with Radius  $R$   
(in addition to the usual 3+1 dims)

- Only fundamental scale  $M_* \sim 1$  TeV

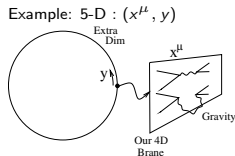
$$M_{pl}^2 = M_*^{2+n} V_n \quad V_n \sim R^n$$

- Gravity in bulk, SM on brane

$$S = \int d^4x d^n y \left[ \mathcal{L}_{\text{Bulk}} + \delta(\underline{y}) \mathcal{L}_{\text{Brane}} \right]$$

- Gravitational potential modified to

$$V(r) \sim 1/r^{n+1}$$



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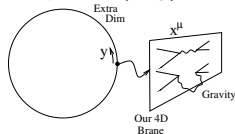
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## Some implications

- for  $n = 1$ ,  $R = 10^{11} m$ 
  - excluded by solar system tests!
- for  $n = 2$ ,  $R \sim 100 \mu m$ 
  - Cavendish type experiments limit  $M_* > 4 \text{ TeV}$

Example: 5-D :  $(x^\mu, y)$



# Universal Extra Dimensions (UED)

[Appelquist, Cheng, Dobrescu] [Cheng, Matchev, Schmaltz] [Datta, Kong, Matchev]

All SM fields propagate in Extra Dimension(s)

- No solution to the hierarchy problem
- KK parity conserved
  - Relaxed constraints since no tree level contribution to EW precision obs
    - $M_{KK} \gtrsim 400 \text{ GeV}$
- LKP stable!
  - Dark Matter
  - Missing energy at Colliders

[Servant, Tait]



# Warped Extra Dimensions (WED, RS)

SM in background 5D warped AdS space

[Randall, Sundrum 99]

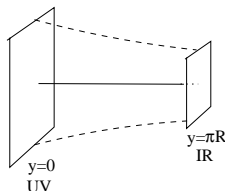
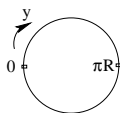
$$ds^2 = e^{-2k|y|} (\eta_{\mu\nu} dx^\mu dx^\nu) + dy^2$$

$Z_2$  orbifold fixed points:

- Planck (UV) Brane
- TeV (IR) Brane

$R$  : radius of Ex. Dim.

$k$  : AdS curvature scale ( $k \lesssim M_{pl}$ )



Hierarchy prob soln:

- IR localized Higgs :  $M_{EW} \sim ke^{-k\pi R}$  : Choose  $k\pi R \sim 34$ 
  - CFT dual is a composite Higgs model

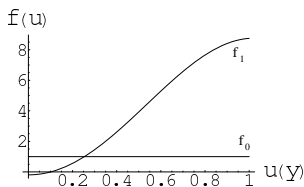
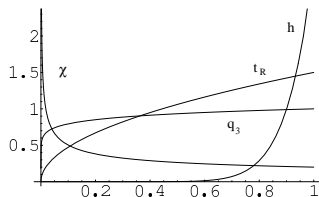
# Explaining SM (gauge & mass) hierarchies (WED)

Bulk Fermions explain SM mass hierarchy

[Gherghetta, Pomarol 00][Grossman, Neubert 00]

$$S^{(5)} \supset \int d^4x dy \left\{ c_\psi k \bar{\Psi}(x, y) \Psi(x, y) \right\}$$

Fermion bulk mass ( $c_\psi$  parameter) controls  $f^\psi(y)$  localization



RS-GIM keeps FCNC under control

For details, see our review: [Davoudiasl, SG, Ponton, Santiago, New  
J.Phys.12:075011,2010. arXiv:0908.1968 [hep-ph]]



# AdS/CFT Correspondence

## AdS/CFT Correspondence

[Maldacena, 1997]

- A classical supergravity theory in  $AdS_5 \times S_5$  at weak coupling is **dual** to a 4D large-N CFT at strong coupling
- The CFT is at the boundary of  $AdS$  [Witten 1998; Gubser, Klebanov, Polyakov 1998]

$$Z_{CFT}[\phi_0] = e^{-\Gamma_{AdS}[\phi_0]}$$

$S \supset \int d^4x \mathcal{O}_{CFT}(x) \phi_0(x)$ Eg: $\langle \mathcal{O}(x_1) \mathcal{O}(x_2) \rangle = \frac{\delta^2 Z_{CFT}[\phi_0]}{\delta \phi_0(x_1) \delta(x_2)}$ with $Z_{CFT}$ given by the RHS	$\Gamma_{AdS}[\phi]$ supergravity eff. action $\phi(y, x)$ is a solution of the EOM ( $\delta\Gamma = 0$ ) for given bndry value $\phi_0(x) = \phi(y = y_0, x)$
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# 4D Duals of Warped Models

[Arkani-Hamed, Porrati, Randall, 2000; Rattazzi, Zaffaroni, 2001]

- Dual of Randall-Sundrum model **RS1 (SM on IR Brane)**
  - Planck brane  $\implies$  UV Cutoff; Dynamical gravity in the 4D CFT
  - TeV (IR) brane  $\implies$  IR Cutoff; Conformal invariance broken below a TeV
    - All SM fields are composites of the CFT
  
- Dual of Warped Models with **Bulk SM**
  - UV localized fields are elementary
  - IR localized fields (Higgs) are composite
    - 4D dual is Composite Higgs model [Georgi, Kaplan 1984]
    - Shares many features with Walking Extended Technicolor
  - Partial Compositeness
    - AdS dual is weakly coupled and hence calculable!
  - KK states are dual to composite resonances





# Kaluza-Klein (KK) expansion

Eg: 5-Dimensional theory : Bulk fields :  $\Phi(x, y) = \{A_M, \phi, \Psi, \dots\}$

$$S = \int d^4x dy \mathcal{L}^{(5)} \quad ; \quad \mathcal{L}^{(5)} \supset \partial^M \phi^\dagger \partial_M \phi - m_\phi^2 \phi^\dagger \phi$$

$$\delta S^{(5)} = 0 \quad \implies \quad \text{Euler-Lagrange Equations of Motion (EOM)} : \quad \frac{\delta \mathcal{L}^{(5)}}{\delta \Phi} = \partial_M \frac{\delta \mathcal{L}^{(5)}}{\delta \partial_M \Phi}$$

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**KK expansion:** expand in a complete set of states  $f_n(y)$

$$\Phi(x, y) = \sum_{n=0}^{\infty} \phi^{(n)}(x) f^{(n)}(y) \quad \text{with} \quad \int dy f^{(n)}(y) f^{(m)}(y) = \delta_{nm}$$



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Plug into EOM,  $y$  dependent piece is  $\left[-\partial_y^2 + \hat{M}_\phi^2\right] f_{(n)}(y) = m_n^2 f_n(y)$

The solution is  $f_{(n)}(y) = \frac{1}{N_n} e^{im_n y}$  ;  $m_n = \frac{n}{R}$

Plug in the KK expansion into 5D action and integrate over  $y$

$$S = \int d^4x \left[ \sum_{n=-\infty}^{\infty} \left( \partial^\mu \phi^{(n)*} \partial_\mu \phi^{(n)} - m_n^2 \phi^{(n)*} \phi^{(n)} \right) \right]$$

Is the **equivalent 4D theory**

with an infinite tower of states (the **KK states**)



# Equivalent 4D theory (with interactions)

Similar procedure for interactions also

$$\mathcal{S}^{(4)} \supset \sum \int d^4x \, m_n^2 \phi^{(n)} \phi^{(n)} + g_{4D}^{(nmI)} \psi^{(n)} \psi^{(m)} A^{(I)} + \lambda_{4D}^{(nm)} \psi_L^{(n)} \psi_R^{(m)} H$$

$\phi^{(n)} \rightarrow$  KK tower with mass  $m_n$  ; Denote  $\phi^{(1)} \equiv \phi'$ ;  $m_1 \equiv m_{KK} \sim \text{TeV}$   
(for WED)

Some 4D couplings

- Yukawas:  $\lambda_{4D}^{(00)} = \lambda_{5D} \int dy f_0^{\psi L} f_0^{\psi R} f^H$
- Gauge couplings:  $g_{4D}^{(001)} = g_{5D} \int dy f_0^{\psi} f_0^{\psi} f_1^A$



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Similar procedure for interactions also

$$S^{(4)} \supset \sum \int d^4x \, m_n^2 \phi^{(n)} \phi^{(n)} + g_{4D}^{(nml)} \psi^{(n)} \psi^{(m)} A^{(l)} + \lambda_{4D}^{(nm)} \psi_L^{(n)} \psi_R^{(m)} H$$

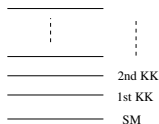
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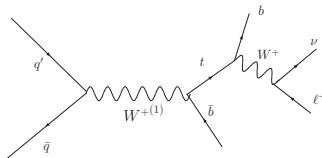
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In summary

- 5D (compact) field  $\leftrightarrow$  "Infinite" tower of 4D fields
- Look for this tower at the LHC

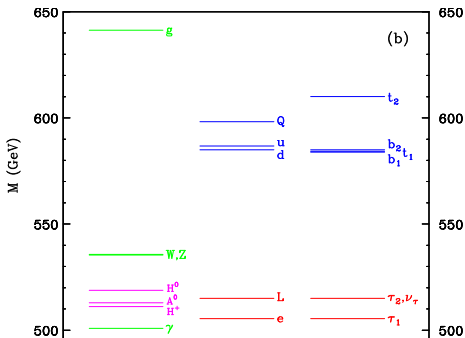


Example:



## UED Spectrum

- All KK states degenerate at leading order
  - Loop corrections split this



[Cheng, Matchev, Schmaltz]

LHC SUSY  $\leftrightarrow$  UED confusion!

# 4-D KK couplings in WED

$$\xi \equiv \sqrt{k\pi R} \approx 5$$

Compare to SM couplings:

- $\xi$  enhanced:  $t_R t_R A', hhA', \phi\phi A'$
- $1/\xi$  suppressed:  $\psi_{light} \psi_{light} A'_{++}$
- SM strength:  $t_L t_L A'$

(Equivalence Theorem  $\Rightarrow \phi \leftrightarrow A_L$ )

Note:  $\psi_{light} \psi_{light} A'_{-+} = 0$



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Effective coupling (Eg:  $Z'$ ):

$$\mathcal{L}^{4D} \supset \bar{\psi}_{L,R} \gamma^\mu \left[ eQ I A_{1\mu} + g_Z \left( T_L^3 - s_W^2 T_Q \right) I Z_{1\mu} + g_{Z'} \left( T_R^3 - s'^2 T_Y \right) I Z_{X1\mu} \right] \psi_{L,R}$$





# Challenge I : Precision EW Constraints in WED



## Precision Electroweak Constraints (S, T, $Zb\bar{b}$ )

- Bulk gauge symm -  $SU(2)_L \times U(1)$  (SM  $\psi$ , H on TeV Brane)
  - T parameter  $\sim (\frac{v}{M_{KK}})^2 (k\pi R)$  [Csaki, Erlich, Terning 02]
  - S parameter also  $(k\pi R)$  enhanced
  
- AdS bulk gauge symm  $SU(2)_R \Leftrightarrow$  CFT Custodial Symm [Agashe, Delgado, May, Sundrum 03]
  - T parameter - Protected
  - S parameter -  $\frac{1}{k\pi R}$  for light bulk fermions
  - Problem:  $Zb\bar{b}$  shifted
  
- 3rd gen quarks (2,2) [Agashe, Contino, DaRold, Pomarol 06]
  - $Zb\bar{b}$  coupling - Protected
  - Precision EW constraints  $\Rightarrow M_{KK} \gtrsim 2 - 3$  TeV

[Carena, Ponton, Santiago, Wagner 06,07] [Bouchart, Moreau-08] [Djouadi, Moreau, Richard 06]



# WED Bulk Gauge Group

[Agashe, Delgado, May, Sundrum 03]

Bulk gauge group :  $SU(3)_{QCD} \otimes SU(2)_L \otimes SU(2)_R \otimes U(1)_X$

- 8 gluons
- 3 neutral EW ( $W_L^3, W_R^3, X$ )
- 2 charged EW ( $W_L^\pm, W_R^\pm$ )



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Gauge Symmetry breaking:

- By Boundary Condition (BC):
  - $SU(2)_R \times U(1)_X \rightarrow U(1)_Y$
- By VEV of TeV brane Higgs
  - $SU(2)_L \times U(1)_Y \rightarrow U(1)_{EM}$

$$A_{-+}(x, y) \text{ BC: } A|_{y=0} = 0; \quad \partial_y A|_{y=\pi R} = 0$$

$$\text{Higgs } \Sigma = (2, 2)$$



# Fermion representation : $Zb\bar{b}$ not protected

[Agashe, Delgado, May, Sundrum '03]

- Complete  $SU(2)_R$  multiplet : Doublet  $t_R$  (DT) model
  - $Q_L \equiv (\mathbf{2}, \mathbf{1})_{1/6} = (t_L, b_L)$
  - $\psi_{t_R} \equiv (\mathbf{1}, \mathbf{2})_{1/6} = (t_R, b')$
  - $\psi_{b_R} \equiv (\mathbf{1}, \mathbf{2})_{1/6} = (t', b_R)$ 
    - "Project-out"  $b'$ ,  $t'$  zero-modes by  $(-, +)$  B.C.
    - New  $\psi_{VL} : b', t'$
- $b \leftrightarrow b'$  mixing
  - $Zb\bar{b}$  coupling shifted
    - So LEP constraint quite severe



# Fermion representation : $Zb\bar{b}$ protected

- $Q_L = (2, 2)_{2/3} = \begin{pmatrix} t_L & \chi \\ b_L & t' \end{pmatrix}$  [Agashe, Contino, DaRold, Pomarol '06]
- $Zb_L\bar{b}_L$  protected by custodial  $SU(2)_{L+R} \otimes P_{LR}$  invariance  
 $Wt_L b_L$ ,  $Zt_L t_L$  not protected, so shifts



Fermion representation :  $Zb\bar{b}$  protected

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Two  $t_R$  possibilities:

① Singlet  $t_R$  (ST) :  $(1, 1)_{2/3} = t_R$       New  $\psi_{VL} : \chi, t'$

② Triplet  $t_R$  (TT) :

$$(1, 3)_{2/3} \oplus (3, 1)_{2/3} = \psi'_{tR} \oplus \psi''_{tR} = \begin{pmatrix} \frac{t_R}{\sqrt{2}} & \chi' \\ -\frac{t_R}{\sqrt{2}} & b' \end{pmatrix} \oplus \begin{pmatrix} \frac{t''}{\sqrt{2}} & \chi'' \\ b'' & -\frac{t''}{\sqrt{2}} \end{pmatrix}$$

New  $\psi_{VL} : \chi, t', \chi', b', \chi'', t'', b''$

# Flavor structure

[Agashe, Perez, Soni, 04]

$$\mathcal{L} \supset \bar{\Psi}^i i \Gamma^\mu D_\mu \Psi^i + M_{ij} \bar{\Psi}^i \Psi^j + y_{ij}^{5D} H \bar{\Psi}^i \Psi^j + h.c.$$

- Basis choice:  $M_{ij}$  diagonal  $\equiv M_i$ 
  - All flavor violation from  $y_{ij}^{5D}$
  - KK decompose and go to mass basis
    - $\implies g \bar{\Psi}_{(n)}^i W_\mu^{(k)} \Psi_{(m)}^j$  off-diagonal in flavor  
(due to non-degenerate  $f^i$  i.e.  $M^i$ )
- 5D fermion  $\Psi$  is vector-like
  - $M_{ij}$  is independent of  $\langle H \rangle = v$
  - But zero-mode made chiral (SM)



# FCNC couplings

- $h_{(0)}^{\mu\nu} \psi_{(0)} \psi_{(0)}$  : diagonal
- $\{A_{(0)}, g_{(0)}\} \psi_{(0)} \psi_{(0)}$  : diagonal (unbroken gauge symmetry)
- $\{Z_{(0)}, Z_{X(0)}\} \psi_{(0)} \psi_{(0)}$  : almost diagonal (non-diagonal due to EWSB effect)
- $h \psi_{(0)} \psi_{(0)}$  : diagonal (only source of mass is  $\langle h \rangle = v$ )

- 
- $h_{(1)}^{\mu\nu} \psi_{(0)} \psi_{(0)}$  : off-diagonal
  - $\{A_{(1)}, g_{(1)}\} \psi_{(0)} \psi_{(0)}$  : off-diagonal (i=1,2 almost diagonal)
  - $\{Z_{(1)}, Z_{X(1)}\} \psi_{(0)} \psi_{(0)}$  : off-diagonal

- 
- $h_{(0)}^{\mu\nu} \psi_{(0)} \psi_{(1)}$  : 0
  - $\{A_{(0)}, g_{(0)}\} \psi_{(0)} \psi_{(1)}$  : 0 (unbroken gauge symmetry)
  - $\{Z_{(0)}, Z_{X(0)}\} \psi_{(0)} \psi_{(1)}$  : off-diagonal (EWSB effect)
  - $h \psi_{(0)} \psi_{(1)}$  : off-diagonal (since  $M_\psi$  is extra source of mass)

$\psi_{(0)} \leftrightarrow \psi_{(1)}$  mixing due to EWSB





# FCCC couplings

- $W_{L(0)}^\pm \psi_{(0)}^i \psi_{(0)}^j : g V_{CKM}^{ij}$
- $\{W_{L(1)}^\pm, W_{R(1)}^\pm\} \psi_{(0)} \psi_{(0)} : g V_{100} [f_{W(1)} f_\psi f_\psi]$ 
  - [...] suppressed for  $i = 1, 2$ ; (Not suppr for  $b_L, t_L, t_R$ )
- $W_{L(0)}^\pm \psi_{(0)} \psi_{(1)} : g V_{001} [f_{W(1)} f_\psi f_{\psi(1)}]$



# Challenge II : Flavor Constraints in WED

- $K^0 \bar{K}^0$  mixing:

- Tree-level FCNC vertex  $g_{(1)} d s \propto V_L^{d\dagger} \begin{pmatrix} [g_{(1)} d d] & 0 \\ 0 & [g_{(1)} s s] \end{pmatrix} V_L^d$

- $b \rightarrow s \gamma$  :

- No tree-level contribution to helicity flip dipole operator
  - So 1-loop with  $g_{(1)} b s_{(1)}$  OR  $\phi^\pm b s_{(1)}$

- $b \rightarrow s \ell^+ \ell^-$  ,  $b \rightarrow s s \bar{s}$  ,  $K \rightarrow \pi \nu \bar{\nu}$  :

- Tree level FCNC vertex  $Z s d$

Bound :  $m_{KK} \gtrsim \text{few TeV}$

[Agashe et al][Buras et al][Neubert et al][Csaki et al]

Relaxed with flavor alignment : MFV, NMFV, flavor symmetries, ...

[Fitzpatrick et al][Agashe et al]

[SG, A.Iyer, S.Vempati Ongoing]



# LHC Phenomenology



# LED KK Graviton @ LHC

[Giudice, Rattazzi, Wells 1998][Hewett 1998] [Han, Lykken, Zhang 1998]

Look for KK Gravitons ( $h_{\mu\nu}^{(n)}$ ) : Missing energy (MET)

- Small KK spacing : sum over huge number of states
  - Cutoff dependence
- Final state Gravitons :  $pp \rightarrow \gamma h^{(n)}, j h^{(n)}$
- Virtual Gravitons :  $pp \rightarrow h^{(n)} \rightarrow \ell^+ \ell^-, \dots$



LED LHC Limit  $pp \rightarrow h_{\mu\nu}^{(n)} \rightarrow \ell^+ \ell^-$ 

TABLE VIII. Observed 95% C.L. lower limits on  $M_S$  (in units of TeV), including systematic uncertainties, for ADD signal in the GRW, Hewett and HLZ formalisms with  $K$  factors of 1.6 and 1.7 applied to the signal for the dilepton and diphoton channels, respectively. Separate results are provided for the different choices of flat priors:  $1/M_S^4$  and  $1/M_S^8$ .

Channel	Prior	GRW	Hewett	HLZ				
				$n=3$	$n=4$	$n=5$	$n=6$	$n=7$
$ee$	$1/M_S^4$	2.95	2.63	3.51	2.95	2.66	2.48	2.34
	$1/M_S^8$	2.82	2.67	3.08	2.82	2.68	2.59	2.52
$\mu\mu$	$1/M_S^4$	3.07	2.74	3.65	3.07	2.77	2.58	2.44
	$1/M_S^8$	2.82	2.67	3.08	2.82	2.68	2.59	2.52
$ee + \mu\mu$	$1/M_S^4$	3.27	2.92	3.88	3.27	2.95	2.75	2.60
	$1/M_S^8$	3.09	2.92	3.37	3.09	2.94	2.84	2.76
$ee + \mu\mu + \gamma\gamma$	$1/M_S^4$	3.51	3.14	4.18	3.51	3.17	2.95	2.79
	$1/M_S^8$	3.39	3.20	3.69	3.39	3.22	3.11	3.02

ATLAS : 1211.1150 : 7TeV, 5  $fb^{-1}$

## WED KK Graviton

[Agashe et al, 07] [Fitzpatrick et al, 07]

$$m_n = x_n k e^{-k\pi r} \quad x_n = 3.83, 7.02, \dots$$

$$\mathcal{L} \supset -\frac{C^{ffG}}{\Lambda} T^{\alpha\beta} h_{\alpha\beta}^{(n)} \quad \Lambda = \bar{M}_P e^{-k\pi r}$$

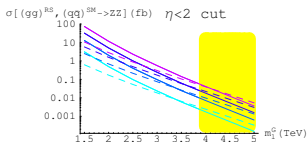
- SM on IR brane

- CDF & D0 bounds :  $m_1 > 300 - 900$  GeV for  $\frac{k}{M_p} = 0.01-0.1$
- ATLAS & CMS reach : 3.5 TeV with  $100 fb^{-1}$

$$gg \rightarrow h^{(1)} \rightarrow ZZ \rightarrow 4\ell$$

- SM in Bulk (flavor)

- light fermion couplings highly suppressed
- gauge field couplings  $\frac{1}{k\pi r}$  suppressed
- Decays dominantly to  $t, h, V_{Long}$

various  $\frac{k}{M_p}$  ; SM dashed

[Agashe, Davoudiasl, Perez, Soni, 2007]





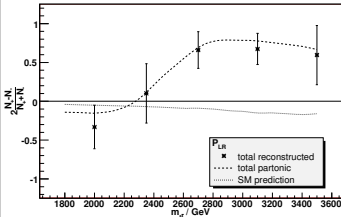
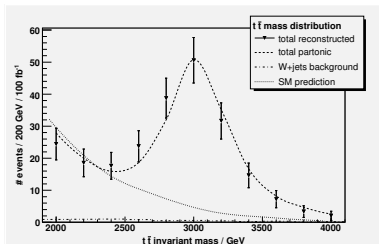
# KK Gluon

[Agashe et al, 06] [Lillie et al, 07]

$$m_n = x_n k e^{-k\pi r} \quad x_n \approx 2.45, 5.57, \dots \quad \text{Width } \Gamma \approx \frac{M}{6}$$

$g^{(1)} t\bar{t}$  : parity violating couplings!

$$\text{LHC: } q\bar{q} \rightarrow g^{(1)} \rightarrow t\bar{t}$$



$$P_{LR} = 2 \frac{N_+ - N_-}{N_+ + N_-} \quad N_+ \text{ forward going } \ell \text{ wrt } k_t$$

LHC reach: About 4 TeV with 100  $fb^{-1}$



# WED $Z'$ channels summary

[Agashe, Davoudiasl, SG, Han, Huang, Perez, Si, Soni - arXiv:0709.0007 [hep-ph]]  
( $\mathcal{L}_2$  TeV;  $\mathcal{L}_3$  TeV) in  $fb^{-1}$

- $pp \rightarrow Z' \rightarrow W^+ W^-$ 
  - Fully leptonic :  $W \rightarrow \ell\nu$  ;  $W \rightarrow \ell\nu$   $\mathcal{L} : (100; 1000) fb^{-1}$
  - Semi leptonic :  $W \rightarrow \ell\nu$  ;  $W \rightarrow (jj)$   $\mathcal{L} : (100; 1000) fb^{-1}$
  
- $pp \rightarrow Z' \rightarrow Z h$ 
  - $m_h = 120\text{GeV} : Z \rightarrow \ell^+ \ell^-$  ;  $h \rightarrow b \bar{b}$   $\mathcal{L} : (200; 1000) fb^{-1}$
  - $m_h = 150\text{GeV} : Z \rightarrow (jj)$  ;  $h \rightarrow W^+ W^- \rightarrow (jj) \ell\nu$   $\mathcal{L} : (75; 300) fb^{-1}$
  
- $pp \rightarrow Z' \rightarrow \ell^+ \ell^-$   $\mathcal{L} : (1000; -) fb^{-1}$ 
  - $BR_{\ell\ell} \sim 10^{-3}$  Tiny!
  
- $pp \rightarrow Z' \rightarrow t \bar{t}, b \bar{b}$ 
  - KK gluon “pollution” [Djouadi, Moreau, Singh 07]

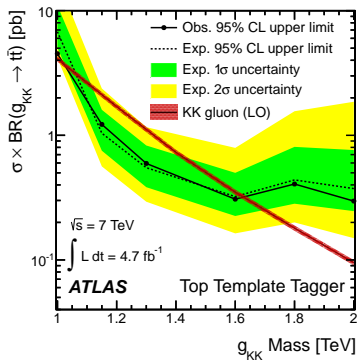


# $W'^{\pm}$ Channels summary

[Agashe, SG, Han, Huang, Soni, 08: arXiv:0810.1497]  
( $\mathcal{L}_2$  TeV;  $\mathcal{L}_3$  TeV) in  $fb^{-1}$

- $W'^{\pm} \rightarrow t b$ :
  - Leptonic  $\mathcal{L} : (100; 1000) fb^{-1}$ 
    - $t \bar{t}$  becomes (reducible) bkgnd since collimated  $t$  can fake a b-jet  
Jet-mass cut : cone size 1.0 and  $0 < j_M < 75 \Rightarrow 0.4\%$  of  $tops$  fake  $b$
- $W'^{\pm} \rightarrow Z W$ :
  - Fully leptonic  $\mathcal{L} : (100; 1000) fb^{-1}$
  - Semi leptonic  $\mathcal{L} : (300; -) fb^{-1}$
- $W'^{\pm} \rightarrow W h$ :  $\mathcal{L} : (100; 300) fb^{-1}$ 
  - $m_h \approx 120 : h \rightarrow b b$ 
    - What is b-tagging eff at large  $p_{T_b}$ ?
  - $m_h \approx 150 : h \rightarrow W W$ 
    - Use W jet-mass to reject light jet

## LHC KK-gluon search



ATLAS JHEP01(2013) 116 : Limit (7 TeV,  $4.7 \text{ fb}^{-1}$ ):  $M_{KK} > 1.6 \text{ TeV} @ 95\% \text{ CL}$

# WED KK Fermions @ LHC

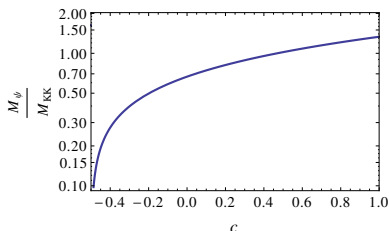
- SM fermions :  $(+, +)$  BC  $\rightarrow$  zero-mode
- “Exotic” fermions :  $(-, +)$  BC  $\rightarrow$  No zero-mode
  - 1<sup>st</sup> KK vectorlike fermion

- Typical  $c_{tR}, c_{tL}$  :  $(-, +)$  top-partners “light”

$c$  : Fermion bulk mass parameter

[Choi, Kim, 2002] [Agashe, Delgado, May, Sundrum, 03]  
 [Agashe, Perez, Soni, 04] [Agashe, Servant 04]

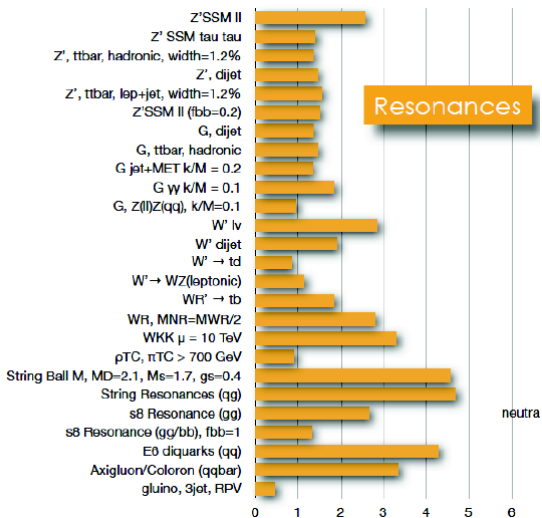
- Look for it at the LHC



[Dennis et al, '07] [Carena et al, '07] [Contino, Servant, '08]  
 [Atre et al, '09, '11] [Aguilar-Saavedra, '09] [Mrazek, Wulzer, '09]  
 [SG, Moreau, Singh, '10] [SG, Mandal, Mitra, Tibrewala, '11] [SG, Mandal, Mitra, Moreau : '13]



## CMS Resonances Limits (Moriond 2013)



# ATLAS Extra Dimensions Limits (Moriond 2013)

ATLAS Exotics Searches\* - 95% CL Lower Limits (Status: HCP 2012)

Large ED (ADD) : microjet + $E_{T,miss}$	$L=4.7 \text{ fb}^{-1}$ , 7 TeV [1210.4491]	4.37 TeV	$M_D$ ( $\delta=2$ )
Large ED (ADD) : monophoton + $E_{T,miss}$	$L=4.6 \text{ fb}^{-1}$ , 7 TeV [1209.4525]	1.93 TeV	$M_D$ ( $\delta=2$ )
Large ED (ADD) : diphoton & dilepton, $m_{\gamma\gamma}$	$L=4.7 \text{ fb}^{-1}$ , 7 TeV [1211.1190]	4.10 TeV	$M_S$ (HLZ $\delta=3$ , NLO)
UED : diphoton + $E_{T,miss}$	$L=4.8 \text{ fb}^{-1}$ , 7 TeV [ATLAS-CONF-2012-072]	1.41 TeV	Compact scale $R^{-1}$
$S^1/Z_2$ ED : dilepton, $m_{ll}$	$L=4.9-5.3 \text{ fb}^{-1}$ , 7 TeV [1209.2535]	4.71 TeV	$M_{KK} \sim R^{-1}$
RS1 : diphoton & dilepton, $m_{\gamma\gamma}$	$L=4.7-5.3 \text{ fb}^{-1}$ , 7 TeV [1210.5359]	2.23 TeV	Graviton mass ( $k/M_{Pl} = 0.1$ )
RS1 : ZZ resonance, $m_{ll}$	$L=1.0 \text{ fb}^{-1}$ , 7 TeV [1203.0718]	345 GeV	Graviton mass ( $k/M_{Pl} = 0.1$ )
RS1 : WW resonance, $m_{\gamma\gamma}$	$L=4.7 \text{ fb}^{-1}$ , 7 TeV [1208.2583]	1.23 TeV	Graviton mass ( $k/M_{Pl} = 0.1$ )
$S g_{KK} \rightarrow tt$ (BR=0.925) : $tt \rightarrow l+jets$ , $m_{jj}$	$L=4.7 \text{ fb}^{-1}$ , 7 TeV [ATLAS-CONF-2012-136]	1.9 TeV	$g_{KK}$ mass
ADD BH ( $M_{Pl}/M_D=3$ ) : SS dimuon, $N_{col,part}$	$L=1.3 \text{ fb}^{-1}$ , 7 TeV [1111.0686]	1.25 TeV	$M_D$ ( $\delta=6$ )
ADD BH ( $M_{Pl}/M_D=3$ ) : leptons + jets, $2p_T$	$L=1.0 \text{ fb}^{-1}$ , 7 TeV [1204.4545]	1.5 TeV	$M_D$ ( $\delta=6$ )
Quantum black hole : dijet, $F(m_{jj})$	$L=4.7 \text{ fb}^{-1}$ , 7 TeV [1210.1715]	4.11 TeV	$M_D$ ( $\delta=6$ )

ATLAS  
Preliminary

$$\int L dt = (1.0 - 13.0) \text{ fb}^{-1}$$

$$\sqrt{s} = 7, 8 \text{ TeV}$$



# Conclusions

- LED “solves” the Heirarchy Problem
  - Quantum gravity at the TeV scale
  - LHC limits already strong
- UED provides Dark Matter candidate
  - Does not solve the hierarchy problem
- WED (AdS) warped models dual to 4D strongly coupled theory
  - Model with bulk fields : limits weaker
  - **LHC 14TeV high luminosity run crucial**



# BACKUP SLIDES

BACKUP SLIDES





# KK decomposition : 5-Dimensional Theory

Bulk fields  $\Phi(x, y) = \{A_M, \phi, \Psi, \dots\}$

$$S^{(5)} = \int d^4x dy \mathcal{L}^{(5)} \quad ; \quad \mathcal{L}^{(5)} \supset \sqrt{|g|} M_*^3 \mathcal{R} + \mathcal{L}_A^{(5)} + \mathcal{L}_\Psi^{(5)} + \mathcal{L}_\phi^{(5)} + \mathcal{L}_{int}^{(5)}$$

$$\mathcal{L}_\Psi^{(5)} \supset \sqrt{|g|} \left\{ \bar{\Psi} i \Gamma^M \partial_M \Psi + c_\psi k \bar{\Psi} \Psi \right\}$$

$$\mathcal{L}_\phi^{(5)} \supset \sqrt{|g|} \left\{ \partial^M \phi^\dagger \partial_M \phi + m_\phi^2 \phi^\dagger \phi \right\};$$

$$\mathcal{L}_A^{(5)} \supset \sqrt{|g|} \left\{ -\frac{1}{4} F^{MN} F_{MN} \right\}$$

$$\mathcal{L}_{int}^{(5)} \supset \sqrt{|g|} \left\{ g_5 \bar{\Psi} \Gamma^M \Psi A_M + (\lambda_5 \phi \bar{\Psi}_L \Psi_R + h.c.) - \mathcal{V}(\phi^\dagger \phi) \right\}$$



# Kaluza-Klein (KK) expansion

$\delta S^{(5)} = 0 \implies$  Euler-Lagrange Equations of Motion (EOM)

- $\frac{\delta \mathcal{L}^{(5)}}{\delta \Phi} = \partial_M \frac{\delta \mathcal{L}^{(5)}}{\delta \partial_M \Phi}$

KK expansion:  $\Phi(x, y) = \sum_{n=0}^{\infty} f_{(n)}^{\phi}(y) \phi^{(n)}(x)$  with  $\int dy f_{(n)}^{\phi}(y) f_{(m)}^{\phi}(y) = \delta_{nm}$

Plug into EOM,  $y$  dependent piece is (for WED) [Gherghetta, Pomarol, 2000]

$$\left[ -e^{sk|y|} \partial_5 (e^{-sk|y|} \partial_5) + \hat{M}_{\Phi}^2 \right] f_{(n)}(y) = e^{2k|y|} m_n^2 f_n(y)$$

$$s = \{2, 4, 1\}; \quad \hat{M}_{\Phi}^2 = \{0, ak^2, c(c \pm 1)k^2\}$$

The solution is

$$f_{(n)}(y) = \frac{1}{N_n} e^{sk|y|/2} \left[ J_{\alpha} \left( \frac{m_n}{k} e^{k|y|} \right) + b_{\alpha} Y_{\alpha} \left( \frac{m_n}{k} e^{k|y|} \right) \right]$$



# Supersymmetry (SUSY)

Reviews: [Martin] [Dress]

SUSY: Fermions  $\leftrightarrow$  Bosons :  
(Doubles particle spectrum)

$$Q|\Phi\rangle = |\Psi\rangle \quad ; \quad Q|\Psi\rangle = |\Phi\rangle$$

Introduce fermionic (Grassmann) coordinate  $\theta$  :  $\{\theta, \theta\} = \{\theta, \bar{\theta}\} = \{\bar{\theta}, \bar{\theta}\} = 0$

**Superfield** :  $\Phi(x_\mu, \theta, \bar{\theta})$

Chiral Superfield:  $\bar{D}\Phi_L = 0$  ;  $D\Phi_R = 0$

$$\Phi_L = \phi(x) + \sqrt{2}\theta\psi(x) + \theta\theta F(x)$$

Vector Superfield:  $v = v^\dagger$

$$V(x, \theta, \bar{\theta}) = -\theta\sigma_\mu\bar{\theta}A^\mu(x) + i\theta\theta\bar{\theta}\bar{\lambda}(x) - \bar{\theta}\bar{\theta}\theta\lambda(x) + \frac{1}{2}\theta\theta\bar{\theta}\bar{\theta}D(x)$$

Minimal Supersymmetric Standard Model (**MSSM**)

$$\text{MSSM Superpotential} : \mathcal{W} = y_u U^c Q H_u - y_d D^c Q H_d - y_e E^c L H_d + \mu H_u H_d$$

SUSY algebra:

$$\{Q_\alpha, \bar{Q}_{\dot{\beta}}\} = 2\sigma_{\alpha\dot{\beta}}^\mu P_\mu$$

$$\{Q_\alpha, Q_\beta\} = \{\bar{Q}_{\dot{\alpha}}, \bar{Q}_{\dot{\beta}}\} = 0$$

$$[P^\mu, Q_\alpha] = [P^\mu, \bar{Q}_{\dot{\alpha}}] = 0$$



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$$\Phi_L = \phi(x) + \sqrt{2}\theta\psi(x) + \theta\theta F(x)$$

Vector Superfield:  $v = v^\dagger$

$$V(x, \theta, \bar{\theta}) = -\theta\sigma_\mu\bar{\theta}A^\mu(x) + i\theta\theta\bar{\theta}\bar{\lambda}(x) - \bar{\theta}\bar{\theta}\theta\lambda(x) + \frac{1}{2}\theta\theta\bar{\theta}\bar{\theta}D(x)$$

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$$\text{MSSM Superpotential} : \mathcal{W} = y_u U^c Q H_u - y_d D^c Q H_d - y_e E^c L H_d + \mu H_u H_d$$

SUSY  $\implies M_\psi = M_\phi$     Experiment  $\implies$  **SUSY broken**



# SUSY solves gauge hierarchy problem

The diagram shows two Feynman diagrams added together. The first diagram is a loop diagram with a solid circle representing a top quark loop. It has two external dashed lines labeled  $h$  and two internal lines labeled  $t_L, t_R$ . Below the loop is the label  $-i\frac{y_t}{\sqrt{2}}$ . The second diagram is a loop diagram with a dashed circle representing a stop squark loop. It has two external dashed lines labeled  $h$  and two internal lines labeled  $\tilde{t}_L, \tilde{t}_R$ . Below the loop is the label  $-i\frac{y_{\tilde{t}}}{2}$ . The two diagrams are separated by a plus sign, and the entire sum is set equal to zero.

$\Lambda^2$  divergence cancelled

[Romes Kaul 1981, 82]

Similarly  $h, W^\pm, Z$  divergences cancelled by  $\tilde{\lambda}$



# SUSY solves gauge hierarchy problem

The diagram shows two Feynman diagrams representing loop corrections to a Higgs self-energy. The first diagram is a top quark loop with external Higgs lines labeled  $h$  and internal top quark lines labeled  $t_L, t_R$ . The loop is a solid circle with a vertex factor of  $-i\frac{y_t}{\sqrt{2}}$ . The second diagram is a stop squark loop with external Higgs lines labeled  $h$  and internal stop squark lines labeled  $\tilde{t}_L, \tilde{t}_R$ . The loop is a dashed circle with a vertex factor of  $-i\frac{y_t^2}{2}$ . The two diagrams are summed together, indicated by a plus sign, and set equal to zero.

$\Lambda^2$  divergence cancelled

[Romes Kaul 1981, 82]

Similarly  $h, W^\pm, Z$  divergences cancelled by  $\tilde{\lambda}$

Gauge Coupling Unification - GUT SUSY  $SO(10)$

Includes  $\nu_R \Rightarrow$  Neutrino seesaw mass



# SUSY breaking

SUSY has to be broken

- Spectrum depends on SUSY Breaking/Mediation + RGE
- Minimal Supersymmetric SM (MSSM) general parametrization

$$\mathcal{L}_{SUSY}^{soft} \supset -\frac{1}{2} M_{\tilde{\chi}} \tilde{\chi} \tilde{\chi} - \tilde{u}^c a_u \tilde{Q} H_u - \tilde{Q}^\dagger \tilde{m}_Q^2 \tilde{Q} - m_H^2 H^* H - b\mu H_u H_d + \dots$$

MSSM predicts a LIGHT Higgs. At tree level:  $m_h < m_Z$ .

- But LEP bound  $m_h \gtrsim 114 \text{ GeV}$
- Sizable one loop correction:  $\delta m_h^2 \lesssim \frac{3}{4\pi^2} y_t^2 m_t^2 \log \frac{\tilde{m}_1 \tilde{m}_2}{m_t^2}$ 
  - LEP Higgs bound needs heavy stop  $\Rightarrow$  "Little hierarchy problem"



# R-parity

SM gauge symmetry allows

$$W_{\Delta L} = LH_u + LE^c L + QD^c L ; \quad W_{\Delta B} = U^c D^c D^c$$

These induce proton decay :  $\tau_p \sim 10^{-10} s$  for  $\tilde{m} \sim 1$  TeV

Impose Matter Parity  $R_M = (-1)^{3(B-L)}$  to forbid  $\Delta L$  and  $\Delta B$  terms

For components this implies : **R-parity**  $R_p = (-1)^{3(B-L)+2s}$

Consequence : The **Lightest SUSY Particle (LSP) is stable**

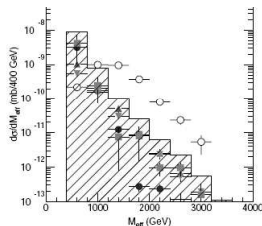
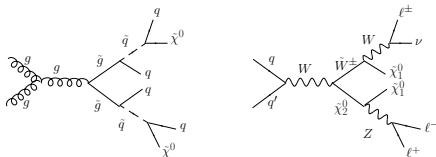
- Cosmologically stable Dark Matter
- Missing Energy at Colliders





# SUSY at LHC

- Cascade decays
- Missing energy signals

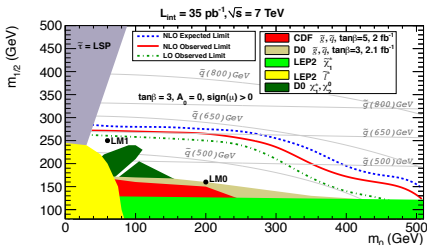
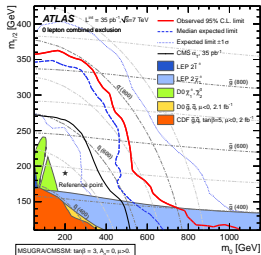
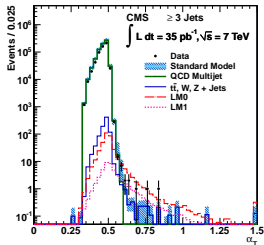
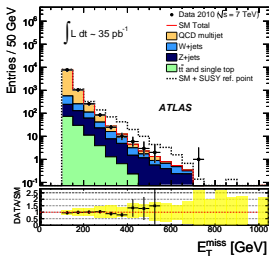


[ATLAS Physics TDR]

- Can we determine the spin and couplings to show SUSY?
  - Angular distributions



# LHC Data ! (SUSY jets + MET)



# Yukawa Couplings

## Yukawa Couplings

- No  $Zb\bar{b}$  protection

- DT  $\mathcal{L}_{\text{Yuk}} \supset \lambda_t \bar{Q}_L \Sigma \psi_{t_R} + \lambda_b \bar{Q}_L \Sigma \psi_{b_R} + h.c.$

- With  $Zb\bar{b}$  protection

- ST  $\mathcal{L}_{\text{Yuk}} \supset \lambda_t \text{Tr}[\bar{Q}_L \Sigma] t_R + h.c.$

- TT  $\mathcal{L}_{\text{Yuk}} \supset \lambda_t \text{Tr}[\bar{Q}_L \Sigma \psi'_{t_R}] + \lambda'_t \text{Tr}[\bar{Q}_L \Sigma \psi''_{t_R}] + h.c.$

- $b$  Yukawa requires triplet  $b_R$

$$(1, 3)_{2/3} \oplus (3, 1)_{2/3} = \psi'_{b_R} \oplus \psi''_{b_R} = \begin{pmatrix} \frac{t'_b}{\sqrt{2}} & \chi'_b \\ b_R & -\frac{t'_b}{\sqrt{2}} \end{pmatrix} \oplus \begin{pmatrix} \frac{t''_b}{\sqrt{2}} & \chi''_b \\ b''_b & -\frac{t''_b}{\sqrt{2}} \end{pmatrix}$$

$$\mathcal{L}_{\text{Yuk}} \supset \lambda_b \text{Tr}[\bar{Q}_L \Sigma \psi'_{b_R}] + \lambda'_b \text{Tr}[\bar{Q}_L \Sigma \psi''_{b_R}] + h.c.$$

$c_{b_R}$  such that new  $\psi'_b, \psi''_b \gtrsim 3$  TeV, so ignore them



# WED $pp \rightarrow g^{(1)} \rightarrow t\bar{t}$ (semi-leptonic)

!!!Warning!!! Very rough estimates!

- $\sigma(M_{g^{(1)}} = 2\text{TeV}, \sqrt{S} = 14\text{TeV}, k\pi R = 35) \approx 600\text{fb}$ 
  - $\mathcal{L}^{5\sigma}(M_{g^{(1)}} = 2\text{TeV}, \sqrt{S} = 14\text{TeV}, k\pi R = 35) = 1.2\text{fb}^{-1}$
- $14\text{TeV} \rightarrow 7\text{TeV}$  :  $\sigma(g^{(1)} = 2\text{TeV})$  falls by a factor of 25
  - $\mathcal{L}^{5\sigma}(M_{g^{(1)}} = 2\text{TeV}, \sqrt{S} = 7\text{TeV}, k\pi R = 35) = 30\text{fb}^{-1}$   
(Assumed : Bkgnd falls with same factor)
- $\mathcal{L}^{5\sigma}(M_{g^{(1)}} = 2\text{TeV}, \sqrt{S} = 7\text{TeV}, k\pi R = 7) = 1\text{fb}^{-1}$



# Bulk EW Gauge Sector

Bulk EW Gauge group :  $SU(2)_L \times SU(2)_R \times U(1)_X$

- Three neutral gauge bosons:  $(W_L^3, W_R^3, X)$
- Two charged gauge bosons:  $(W_L^\pm, W_R^\pm)$

Symmetry Breaking:

- By Boundary Condition (BC):

$$Z_X(-, +) \text{ means } Z_X|_{y=0} = 0; \partial_y Z_X|_{y=\pi R} = 0$$

- $SU(2)_R \times U(1)_X \rightarrow U(1)_Y$  :  $(W_R^3, W_L^3, X) \rightarrow (W_L^3, B, Z_X)$   
 $A \rightarrow (+, +); Z \rightarrow (+, +); Z_X \rightarrow (-, +)$
- $Z_X \equiv \frac{1}{\sqrt{g_X^2 + g_R^2}} (g_R W_R^3 - g_X X) \rightarrow (-, +)$  ;  $W_R^\pm \rightarrow (-, +)$
- $B \equiv \frac{1}{\sqrt{g_X^2 + g_R^2}} (g_X W_R^3 + g_R X) \rightarrow (+, +)$  ;  $W_L^\pm \rightarrow (+, +)$



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- $Z_X \equiv \frac{1}{\sqrt{g_X^2 + g_R^2}}(g_R W_R^3 - g_X X) \rightarrow (-, +)$  ;  $W_R^\pm \rightarrow (-, +)$
- $B \equiv \frac{1}{\sqrt{g_X^2 + g_R^2}}(g_X W_R^3 + g_R X) \rightarrow (+, +)$  ;  $W_L^\pm \rightarrow (+, +)$

- By VEV of TeV brane Higgs

- $SU(2)_L \times U(1)_Y \rightarrow U(1)_{EM}$  :  $(W_L^3, B, Z_X) \rightarrow (A, Z, Z_X)$



# Gauge EW KK States

## Gauge Boson

- “Zero” modes:  $A^{(0)}, Z^{(0)}$  ;  $W_L^{(0)}$
- First KK modes:  $A^{(1)}, Z^{(1)}, Z_X^{(1)} \rightarrow Z'$  ;  $W_L^{(1)}, W_R^{(1)}$

EWSB mixes :  $Z^{(0)} \leftrightarrow Z^{(1)}$  ;  $Z^{(0)} \leftrightarrow Z_X^{(1)}$  ;  $Z^{(1)} \leftrightarrow Z_X^{(1)}$   
 $W_L^{(0)} \leftrightarrow W_L^{(1)}$  ;  $W_L^{(0)} \leftrightarrow W_R^{(1)}$  ;  $W_L^{(1)} \leftrightarrow W_R^{(1)}$

## Mass eigenstates :

- “Zero” modes:  $A, Z$  ;  $W^\pm$
- First KK modes:  $A_1, \tilde{Z}_1, \tilde{Z}_{X_1} \rightarrow Z'$  ;  $\tilde{W}_{L_1}, \tilde{W}_{R_1} \rightarrow W'^\pm$



## Z' Overlap Integrals

Define:  $\xi \equiv \sqrt{k\pi R} = 5.83$

Z' overlap with Higgs  $\rightarrow \xi$

Z' overlap with fermions:

	$Q_L^3$	$t_R$	other fermions
$\mathcal{I}^+$	$-\frac{1.13}{\xi} + 0.2\xi \approx 1$	$-\frac{1.13}{\xi} + 0.7\xi \approx 3.9$	$-\frac{1.13}{\xi} \approx -0.2$
$\mathcal{I}^-$	$0.2\xi \approx 1.2$	$0.7\xi \approx 4.1$	0

Compared to SM

- Z' couplings to  $h$  enhanced (also  $V_L$  - Equivalence Theorem!)
- Z' couplings to  $t_R$  enhanced
- Z' couplings to  $\chi$  suppressed

$$\bar{\psi}_{L,R} \gamma^\mu \left[ eQI A_{1\mu} + g_Z (T_L^3 - s_W^2 T_Q) IZ_{1\mu} + g_{Z'} (T_R^3 - s'^2 T_Y) IZ_{X1\mu} \right] \psi_{L,R}$$

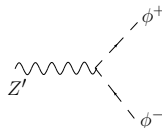




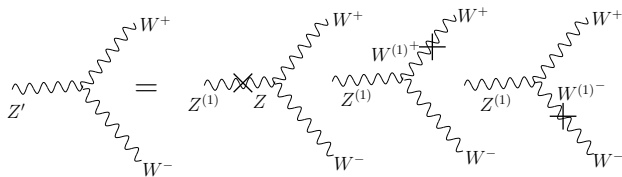
EWSB induced  $Z'W^+W^-$  coupling

$Z^{(1)}V^{(0)}V^{(0)}$  is zero by orthogonality ...  
 ... but induced after EWSB

Using Goldstone equivalence:



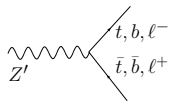
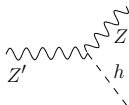
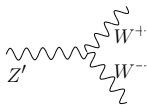
In Unitary Gauge:



Even though  $\xi \cdot \left(\frac{v}{M_{KK}}\right)^2$  suppressed ...

## Z' decays

[Agashe, Davoudiasl, SG, Han, Huang, Perez, Si, Soni - arXiv:0709.0007 [hep-ph]]



$$\Gamma(A_1 \rightarrow W_L W_L) = \frac{e^2 \kappa^2}{192\pi} \frac{M_{Z'}^5}{m_W^4}; \quad \kappa \propto \sqrt{k\pi r_c} \left( \frac{m_W}{M_{W_1^\pm}} \right)^2,$$

$$\Gamma(\tilde{Z}_1, \tilde{Z}_{X1} \rightarrow W_L W_L) = \frac{g_L^2 c_W^2 \kappa^2}{192\pi} \frac{M_{Z'}^5}{m_W^4}; \quad \kappa \propto \sqrt{k\pi r_c} \left( \frac{m_Z}{(M_{Z_1}, M_{Z_{X1}})} \right)^2,$$

$$\Gamma(\tilde{Z}_1, \tilde{Z}_{X1} \rightarrow Z_L h) = \frac{g_Z^2 \kappa^2}{192\pi} M_{Z'}; \quad \kappa \propto \sqrt{k\pi r_c},$$

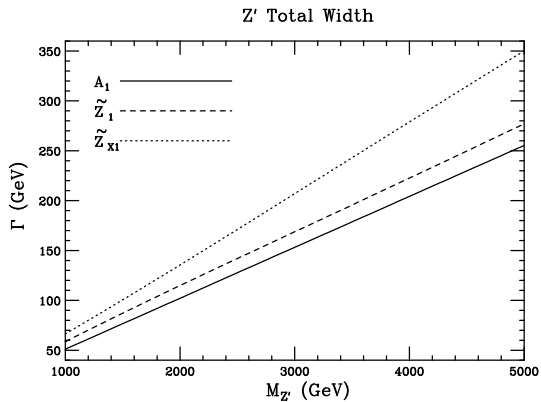
$$\Gamma(Z' \rightarrow f\bar{f}) = \frac{(e^2, g_Z^2)}{12\pi} (\kappa_V^2 + \kappa_A^2) M_{Z'}.$$



Widths & BR's (For  $M_{Z'} = 2\text{TeV}$ )

	$A_1$		$\tilde{Z}_1$		$\tilde{Z}_{X1}$	
	$\Gamma(\text{GeV})$	BR	$\Gamma(\text{GeV})$	BR	$\Gamma(\text{GeV})$	BR
$\bar{t}t$	55.8	0.54	18.3	0.16	55.6	0.41
$\bar{b}b$	0.9	$8.7 \times 10^{-3}$	0.12	$10^{-3}$	28.5	0.21
$\bar{u}u$	0.28	$2.7 \times 10^{-3}$	0.2	$1.7 \times 10^{-3}$	0.05	$4 \times 10^{-4}$
$\bar{d}d$	0.07	$6.7 \times 10^{-4}$	0.25	$2.2 \times 10^{-3}$	0.07	$5.2 \times 10^{-4}$
$\ell^+\ell^-$	0.21	$2 \times 10^{-3}$	0.06	$5 \times 10^{-4}$	0.02	$1.2 \times 10^{-4}$
$W_L^+ W_L^-$	45.5	0.44	0.88	$7.7 \times 10^{-3}$	50.2	0.37
$Z_L h$	-	-	94	0.82	2.7	0.02
Total	103.3		114.6		135.6	

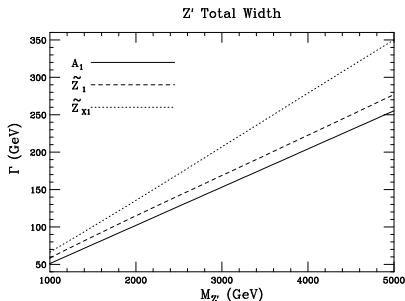
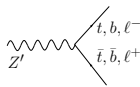
## Total Widths



$M_{Z'} = 2\text{TeV}$	$A_1$	$Z_1$	$Z_{X1}$
$\Gamma$ (GeV)	103.3	114.6	135.6

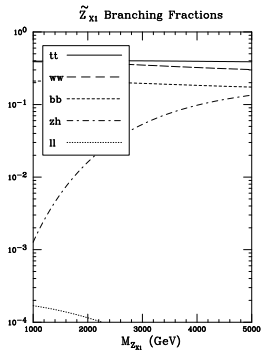
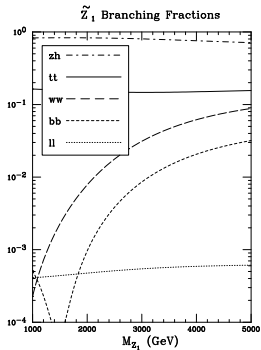
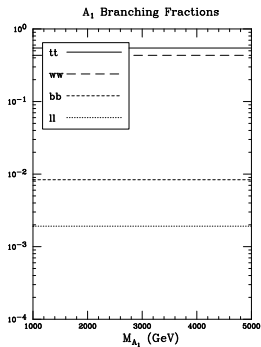
## Z' decays in WED

[Agashe, Davoudiasl, SG, Han, Huang, Perez, Si, Soni - arXiv:0709.0007 [hep-ph]]

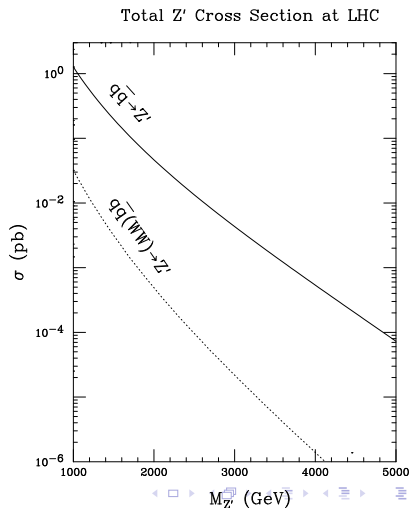
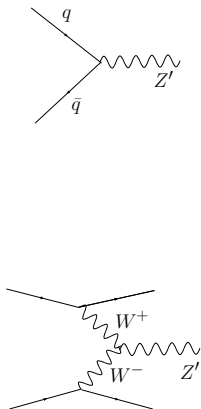


$M_{Z'} = 2\text{TeV}$	$A_1$	$Z_1$	$Z_{X1}$
$\Gamma$ (GeV)	103.3	114.6	135.6

## Z' Branching Ratios in WED

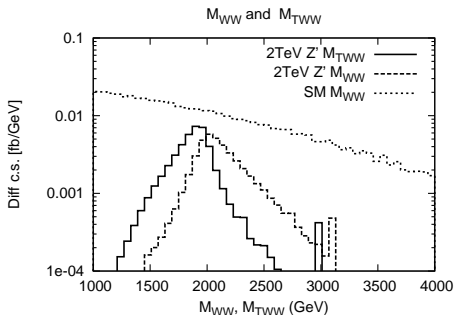


## WED Z' production at the LHC

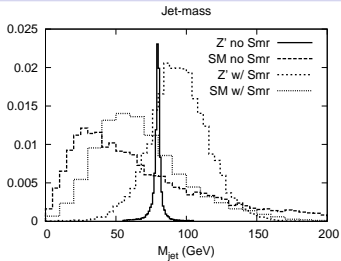
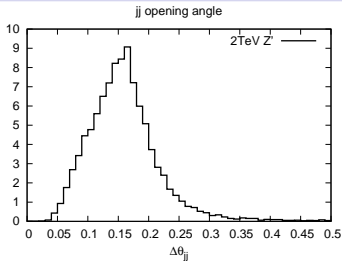


$$pp \rightarrow Z' \rightarrow W^+W^- \rightarrow \ell \nu jj$$

$$M_{eff} \equiv p_{T_{jj}} + p_{T_\ell} + \cancel{p}_T \quad M_{T_{WW}} \equiv 2\sqrt{p_{T_{jj}}^2 + m_W^2}$$





$$pp \rightarrow Z' \rightarrow W^+W^- \rightarrow \ell \nu jj \quad (\text{Boosted } W \rightarrow (jj))$$


jj Collimation implies forming  $m_W$  nontrivial : use jet-mass

In our study: Jet-mass after Parton shower in Pythia

[Thanks to Frank Paige for discussions]

To account for (HCal) expt. uncert.

Smearing by  $\delta E = 80\%/\sqrt{E}$  ;  $\delta\eta, \delta\phi = 0.05$

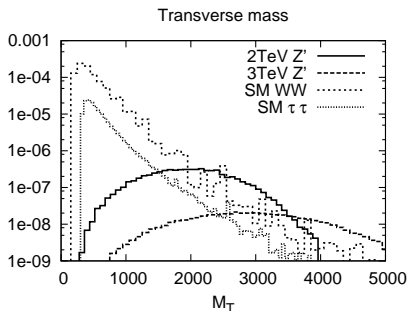
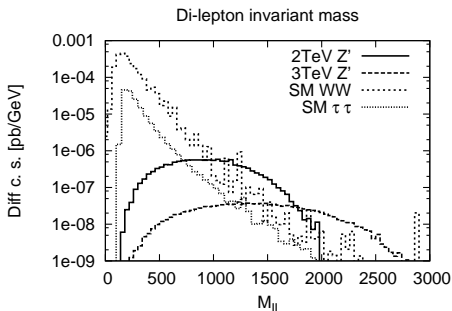
Tracker + ECal (2 cores?) have better resolutions

[F. Paige; M. Strassler]





2  $\nu$ 's  $\Rightarrow$  cannot reconstruct event



$$M_{eff} \equiv p_{T_{\ell_1}} + p_{T_{\ell_2}} + \cancel{p}_T \quad M_{T_{WW}} \equiv 2\sqrt{p_{T_{\ell\ell}}^2 + M_{\ell\ell}^2}$$

$\mathcal{L}$  needed:  $100 \text{ fb}^{-1}$  (2 TeV) ;  $1000 \text{ fb}^{-1}$  (3 TeV)



$$pp \rightarrow Z' \rightarrow W^+ W^- \rightarrow \ell \nu \ell \nu$$

Cross-section (in fb) after cuts:

2 TeV	Basic cuts	$ \eta_\ell  < 2$	$M_{eff} > 1$ TeV	$M_T > 1.75$ TeV	# Evts	S/B	$S/\sqrt{B}$
Signal	0.48	0.44	0.31	0.26	26	0.9	4.9
WW	82	52	0.4	0.26	26		
$\tau\tau$	7.7	5.6	0.045	0.026	2.6		
3 TeV	Basic cuts	$ \eta_\ell  < 2$	$1.5 < M_{eff} < 2.75$	$2.5 < M_T < 5$	# Evts	S/B	$S/\sqrt{B}$
Signal	0.05	0.05	0.03	0.025	25		
WW	82	52	0.08	0.04	40	0.6	3.8
$\tau\tau$	7.7	5.6	0.015	0.003	3		

# events above is for

- 2 TeV :  $100 \text{ fb}^{-1}$
- 3 TeV :  $1000 \text{ fb}^{-1}$



$$pp \rightarrow Z' \rightarrow W^+W^- \rightarrow \ell \nu jj$$

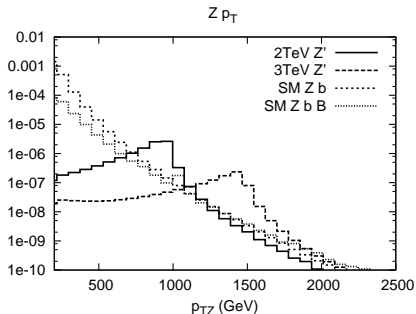
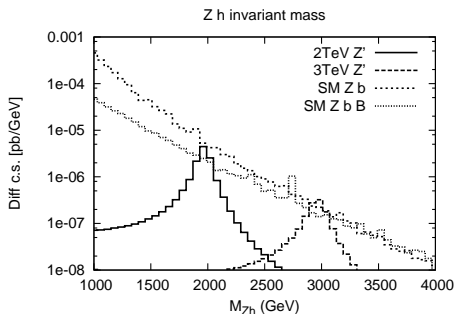
Cross-section (in fb) after cuts:

$M_{Z'} = 2 \text{ TeV}$	$p_T$	$\eta_{\ell,j}$	$M_{eff}$	$M_{T_{WW}}$	$M_{jet}$	# Evts	$S/B$	$S/\sqrt{B}$
Signal	4.5	2.40	2.37	1.6	1.25	125	0.39	6.9
W+1j	$1.5 \times 10^5$	$3.1 \times 10^4$	223.6	10.5	3.15	315		
WW	$1.2 \times 10^3$	226	2.9	0.13	0.1	10		
$M_{Z'} = 3 \text{ TeV}$								
Signal	0.37	0.24	0.24	0.12	-	120	0.17	4.6
W+1j	$1.5 \times 10^5$	$3.1 \times 10^4$	88.5	0.68	-	680		
WW	$1.2 \times 10^3$	226	1.3	0.01	-	10		

# events above is for

- 2 TeV :  $100 \text{ fb}^{-1}$
- 3 TeV :  $1000 \text{ fb}^{-1}$

$$pp \rightarrow Z' \rightarrow Zh \rightarrow \ell^+ \ell^- b \bar{b} \quad (m_h = 120 \text{ GeV})$$



How well can we tag high  $p_T$  b's ?

For  $\epsilon_b = 0.4$ , expect  $R_j \approx 20 - 50$ ;  $R_c = 5$

Two b's close :  $\Delta R_{bb} \sim 0.16$

$\mathcal{L}$  needed:  $200 \text{ fb}^{-1}$  (2 TeV) ;  $1000 \text{ fb}^{-1}$  (3 TeV)



$$pp \rightarrow Z' \rightarrow Zh \rightarrow \ell^+ \ell^- b \bar{b} \quad (m_h = 120 \text{ GeV})$$

Cross-section (in fb) after cuts:

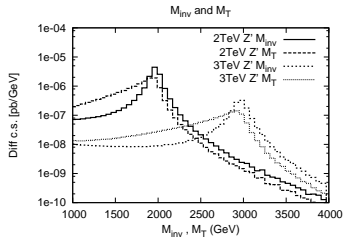
$M_{Z'} = 2 \text{ TeV}$	Basic	$p_{T, \eta}$	$\cos \theta_{Zh}$	$M_{inv}$	b-tag	# Evts	S/B	$S/\sqrt{B}$
$Z' \rightarrow hZ \rightarrow b\bar{b} \ell\ell$	0.81	0.73	0.43	0.34	0.14	27	1.1	5.3
SM $Z + b$	157	1.6	0.9	0.04	0.016	3		
SM $Z + b\bar{b}$	13.5	0.15	0.05	0.01	0.004	0.8		
SM $Z + q_l$	2720	48	22.4	1.5	0.08	15		
SM $Z + g$	505.4	11.2	5.8	0.5	0.025	5		
SM $Z + c$	184	1.9	1.1	0.05	0.01	2		
$M_{Z'} = 3 \text{ TeV}$								
$Z' \rightarrow hZ \rightarrow b\bar{b} \ell\ell$	0.81	0.12	0.05	0.04	0.016	16	2	5.7
SM $Z + b$	157	0.002	0.001	$3 \times 10^{-4}$	$1.2 \times 10^{-4}$	0.12		
SM $Z + b\bar{b}$	13.5	0.018	0.014	0.002	0.001	1		
SM $Z + q_l$	2720	1.1	0.7	0.1	0.005	5		
SM $Z + g$	505.4	0.3	0.2	0.03	0.0015	1.5		
SM $Z + c$	183.5	0.03	0.02	0.002	$4 \times 10^{-4}$	0.4		

# events above is for

- 2 TeV : 200 fb<sup>-1</sup>
- 3 TeV : 1000 fb<sup>-1</sup>



$pp \rightarrow Z' \rightarrow Z h : Z \rightarrow jj ; h \rightarrow W^+ W^- \rightarrow jj \ell \nu$   
 ( $m_h = 150$  GeV)



$$M_{TZh} \equiv \sqrt{p_{TZ}^2 + m_Z^2} + \sqrt{p_{Th}^2 + m_h^2}$$

$M_{Z'} = 2$ TeV $m_h = 150$ GeV	Basic	$p_T, \eta$	$\cos \theta$	$M_T$	$M_{jet}$	# Evts	$S/B$	$S/\sqrt{B}$
$Z' \rightarrow hZ \rightarrow \ell \cancel{E}_T (jj) (jj)$	2.4	1.6	0.88	0.7	0.54	54	2.5	11.5
SM $W jj$	$3 \times 10^4$	35.5	12.7	0.62	0.19	19		
SM $W Z j$	184	0.45	0.15	0.02	0.02	2		
SM $W W j$	712	0.54	0.2	0.02	0.01	1		
$M_{Z'} = 3$ TeV $m_h = 150$ GeV								
$Z' \rightarrow hZ \rightarrow \ell \cancel{E}_T (jj) (jj)$	0.26	0.2	0.14	0.06	—	18	1.2	4.7
SM $W jj$	$3 \times 10^4$	4.1	0.05	—	—	15		

# events above is for

- 2 TeV : 100 fb<sup>-1</sup>
- 3 TeV : 300 fb<sup>-1</sup>



$$pp \rightarrow Z' \rightarrow \ell^+ \ell^-$$

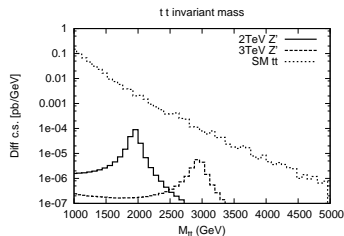
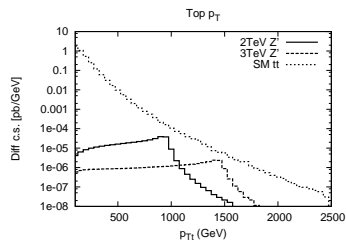
$M_{Z'} = 2 \text{ TeV}$	Basic	$p_{T\ell}$	$M_{\ell\ell}$	# Evts	S/B	$S/\sqrt{B}$
Signal	0.1	0.09	0.06	60	0.3	4.2
SM $\ell\ell$	$3 \times 10^4$	5.4	0.2	200		
SM WW	295	0.03	0.002	2		

# events above is for

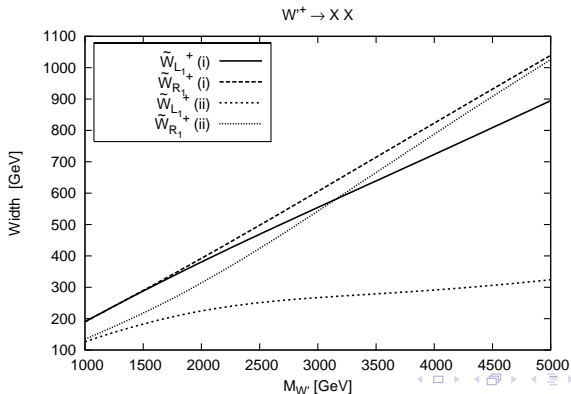
- 2 TeV : 1000 fb<sup>-1</sup>

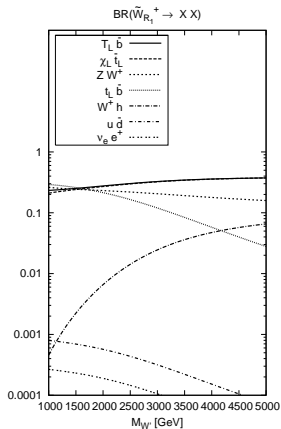
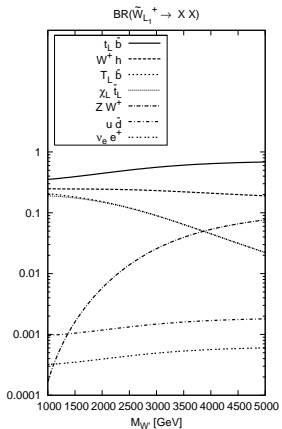
Experimentally clean, but needs a LOT of luminosity



$$pp \rightarrow Z' \rightarrow t\bar{t}$$


$M_{Z'} = 2 \text{ TeV}$	Basic	$p_T > 800$	$1900 < M_{t\bar{t}} < 2100$
Signal	17	7.2	5.6
SM $t\bar{t}$	$1.9 \times 10^5$	31.1	19.1
$M_{Z'} = 3 \text{ TeV}$	Basic	$p_T > 1250$	$2850 < M_{t\bar{t}} < 3100$
Signal	1.7	0.56	0.45
SM $t\bar{t}$	$1.9 \times 10^5$	4.1	1.1

$W'^{\pm}$  width

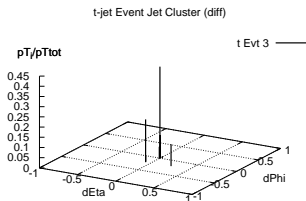
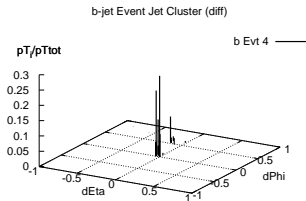
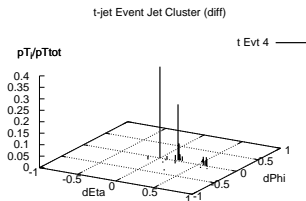
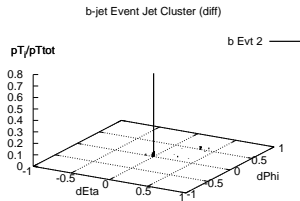


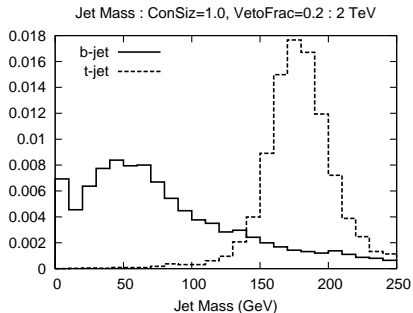
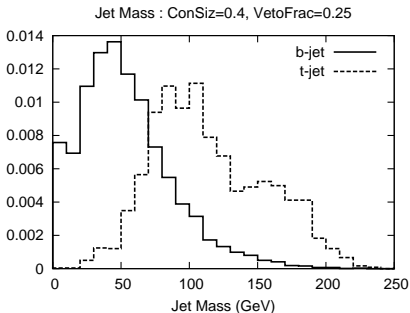
$$W'^{\pm} \rightarrow t b \rightarrow \ell \nu b b$$

Signal c.s.  $\sim 1fb$

Bkgnd is single top + QCD W b b .... AND ...

$t\bar{t}$  : hadronically decaying top can fake a  $b$



$W'^{\pm} \rightarrow t b \rightarrow \ell \nu b b$ 

Jet-mass cut: cone size 1.0 and  $0 < j_M < 75 \Rightarrow 0.4\%$  of *top fakes b*  
 $\mathcal{L}$  needed:  $100 \text{ fb}^{-1}$  (2 TeV)

$W'^{\pm} \rightarrow Z W$  and  $W h$  $W'^{\pm} \rightarrow Z W$ :

- Fully leptonic  $\rightarrow \mathcal{L} : 100 \text{ fb}^{-1}$  (2 TeV) ;  $1000 \text{ fb}^{-1}$  (3 TeV)
- Semi leptonic  $\rightarrow \mathcal{L} : 300 \text{ fb}^{-1}$  (2 TeV) (SM  $W/Z + 1j$  large)

# $W'^{\pm} \rightarrow Z W$ and $W h$

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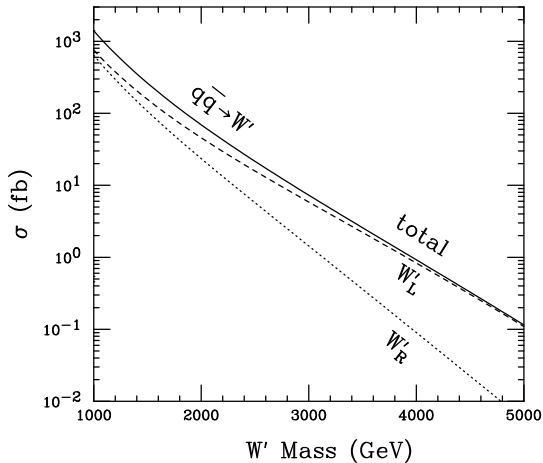
- $m_h \approx 120 : h \rightarrow b b$ 
  - What is b-tagging eff?
- $m_h \approx 150 : h \rightarrow W W$ 
  - Use W jet-mass to reject light jet

$\mathcal{L}$  needed:  $100 \text{ fb}^{-1}$  (2TeV) ;  $300 \text{ fb}^{-1}$  (3TeV)

## W' cross section

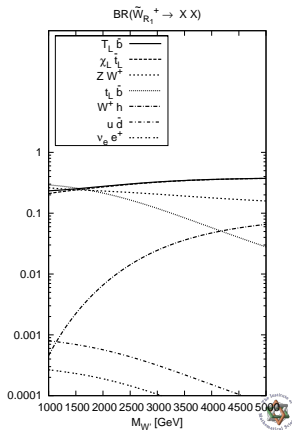
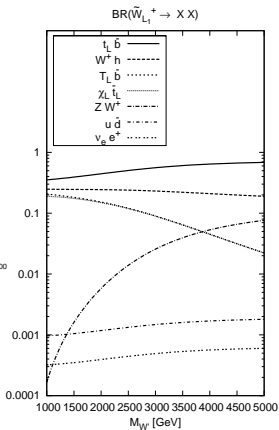
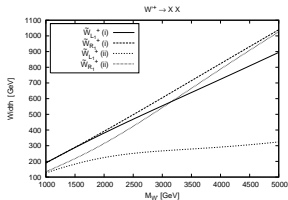
[Agashe, SG, Han, Huang, Soni, 08: arXiv:0810.1497]

Total W' Cross Section at LHC





# $W'^{\pm}$ Width and BR



# Measuring $W'$ Chirality in $(pp) u\bar{d} \rightarrow W'^+ \rightarrow t\bar{b} \rightarrow \ell^+ \nu b\bar{b}$ (WED)

## A Model Independent Study

[SG, Han, Lewis, Si, Zhou, 2010: arXiv:1008.3508]

$$L \supset \bar{\psi}_u (g_L P_L + g_R P_R) \psi_d W'$$

- Can we measure  $g_{L,R}^{ud}$ ,  $g_{L,R}^{tb}$ ?
- Yes, encoded in **top polarization!**



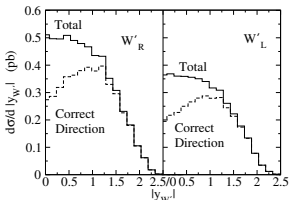
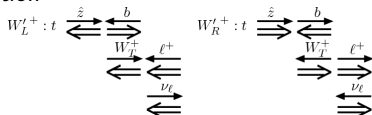
Measuring  $W'$  Chirality in  $(pp) u\bar{d} \rightarrow W'^+ \rightarrow t\bar{b} \rightarrow \ell^+ \nu b\bar{b}$  (WED)

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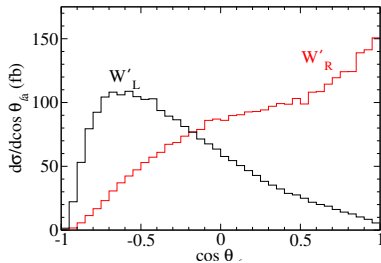
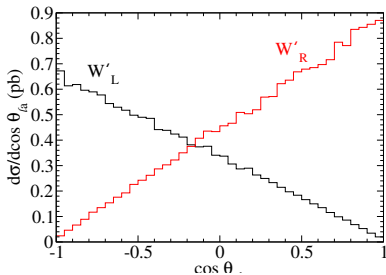
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Need to fix  $u$  direction:Statistical only: On avg  $u$  carries higher momentum fraction than  $\bar{d}$ ∴ direction of  $y_{W'} > 0.8$  is  $u$  direction $\theta_\ell$  distribution analyzes top polarization

Analyze in top rest frame

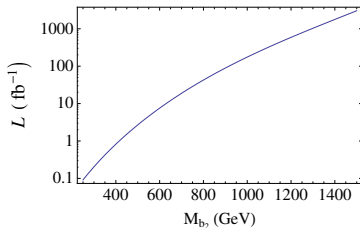
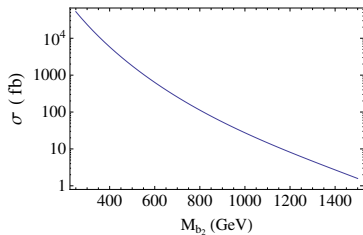
## Measuring W' Chirality (Results)



# $b'$ Pair Production

[SG, T.Mandal, S.Mitra, R.Tibrewala, arXiv:1107.4306]

Pair Production :  $pp \rightarrow b'\bar{b}' \rightarrow bZ\bar{b}Z \rightarrow bj\bar{j}l\bar{l}$



**Cuts:**

- Rapidity:*  $-2.5 < y_{b,j,Z} < 2.5$ ,
- Transverse momentum:*  $p_{T,b,j,Z} > 25$  GeV,
- Invariant mass cuts:*
- $M_Z - 10$  GeV  $< M_{jj} < M_Z + 10$  GeV,
- $0.95M_{b_2} < M_{(bZ)} < 1.05M_{b_2}$ .



# KK states at the LHC

- $h_{\mu\nu}^{(1)}$  (KK Graviton)

$$gg \rightarrow h^{(1)} \rightarrow t\bar{t}$$

$L = 300 \text{ fb}^{-1}$  LHC reach is about 2 TeV

[Agashe, Davoudiasl, Perez, Soni 07]  
[Fitzpatrick, Kaplan, Randall, Wang 07]

- $g_{\mu}^{(1)}$  (KK Gluon)

$$q\bar{q} \rightarrow g^{(1)} \rightarrow t\bar{t}$$

$L = 100 \text{ fb}^{-1}$  LHC reach is 4 TeV

[Agashe, Belyaev, Krupovnickas, Perez, Virzi 06]  
[Lillie, Randall, Wang, 07] [Lillie, Shu, Tait 07]

- $Z_{\mu}^{(1)}, W_{\mu}^{(1)\pm}$  ( $Z_{KK} \equiv Z'$ ,  $W_{KK}^{\pm} \equiv W'$ )

$$q\bar{q} \rightarrow Z', W' \rightarrow XX$$

[Agashe, Davoudiasl, SG, Han, Huang, Perez, Si, Soni 0709.0007 & 0810.1497]

- $b', t', \chi$  (KK Fermions)

[Agashe, Servant 04][Dennis et al 07][Contino, Servant 08][SG, Mandal, Mitra, Moreau ongoing]

- Radion



# Little RS (LRS) ( $Z' \rightarrow l^+ l^-$ )

$$M_{EW} \sim k e^{-k\pi R} ; \text{ Vary } k, k\pi R ; (k\pi R)_{LRS} < (k\pi R)_{RS} = 35$$

- RS:  $k \lesssim M_{pl}$
- **LRS:**  $k \ll M_{pl}$  ;  $k\pi R = 7 \implies k \approx 1000 \text{ TeV}$  [Davoudiasl, Perez, Soni 08]
- RS as a theory of flavor! (*give-up solution to hierarchy problem*)

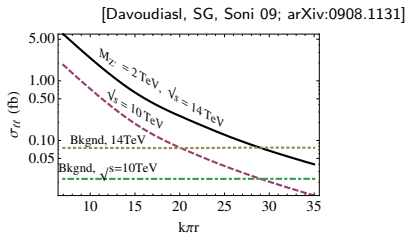
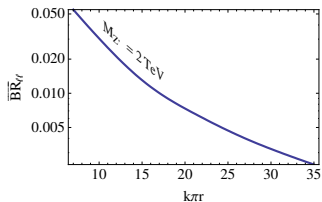


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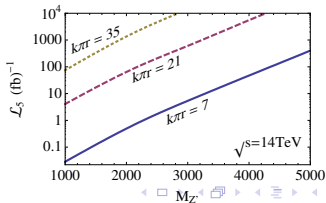
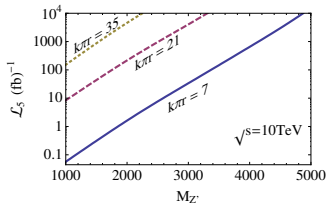
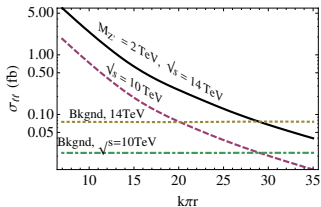
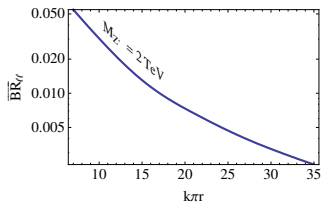
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$pp \rightarrow Z'_{LRS} \rightarrow l^+ l^-$

[Davoudiasl, SG, Soni 09; arXiv:0908.1131]



LED Bulk  $\nu_R$ 

[Dienes, Dudas, Gherghetta]  
 [Davoudiasl, Langacker, Perelstein]  
 [Cao, SG, Yuan 2003, 2004]

- Introduce Bulk  $\nu_R$  propagating in  $\delta$  dimensions

- $\Psi^\alpha(x^\mu, y) = \begin{pmatrix} \psi_L^\alpha(x^\mu, y) \\ \psi_R^\alpha(x^\mu, y) \end{pmatrix} \quad (\delta = 1) \quad \alpha \rightarrow \text{Generation}$

- $\mathcal{L}_{\text{Bulk}} \supset \bar{\Psi}^\alpha i \Gamma^M D_M \Psi^\alpha$

$$\mathcal{L}_{\text{Brane}} \supset \mathcal{L}_{\text{SM}} - \left( \frac{\Lambda_{\alpha\beta}^\nu}{\sqrt{M_*^\delta}} h \psi_R^\beta \nu_L^\alpha + h.c. \right)$$

- $\nu_L \rightarrow$  Usual SM left-handed neutrino
- $\psi_R \rightarrow$  Bulk right-handed neutrino  $\equiv \nu_R$
- $\psi_L \rightarrow$  No direct coupling to SM



LED Bulk  $\nu_R$  at colliders

- $\nu_R$  couples only to  $\nu_L$  and  $h$  (Yukawa)

$$\bullet \mathcal{L}^{(4)} \supset - \left[ \frac{\bar{m}_\nu^{i\beta}}{v} \left( h \nu_R^i \nu_L^\beta + \sum_{\hat{n}} \sqrt{2} h \nu_R^{i(\hat{n})} \nu_L^\beta \right) + h.c. \right] \quad \bar{m}_\nu \equiv m_0 l^\dagger$$

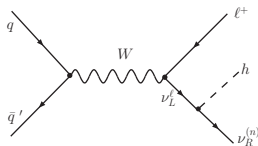
- New Higgs production mechanism (Signal)

$$q \bar{q}' \rightarrow W^* \rightarrow \ell^+ h \nu_R^{(n)} \quad (\ell = e, \mu, \tau)$$

- Signal can be enhanced due to large number of final state  $\nu_R^{(n)}$

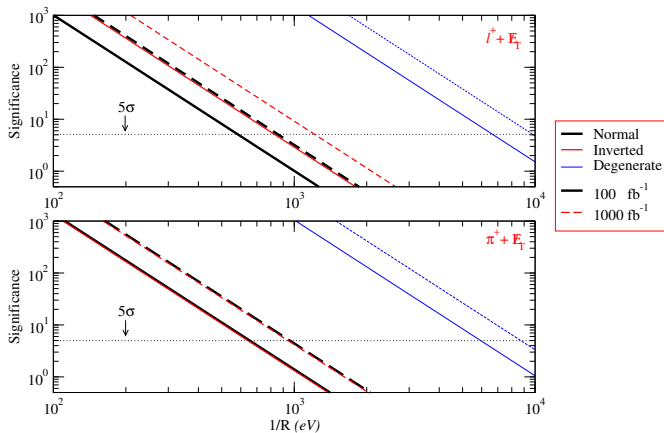
- New Higgs decay mode

- Invisible mode: ( $h \rightarrow \nu_L \nu_R^{(n)}$ )
- (SM:  $h \rightarrow b \bar{b}$ )



LED Bulk  $\nu_R$  @ LHC

$$\delta = 3, \sqrt{S} = 14 \text{ TeV}$$



# Storage Area

- Warped (RS) model
- Heavy EW gauge bosons : 3 neutral ( $Z'$ ) & 2 charged ( $W'^{\pm}$ )
  - Precision electroweak observables require  $M_{Z'}$  ,  $M_{W_1^{\pm}} \gtrsim 2$  TeV
    - Makes discovery challenging at the LHC

