

**FROM CP VIOLATION
TO ARROWS OF TIME:
A VOYAGE THROUGH
STRANGENESS AND BEAUTY**

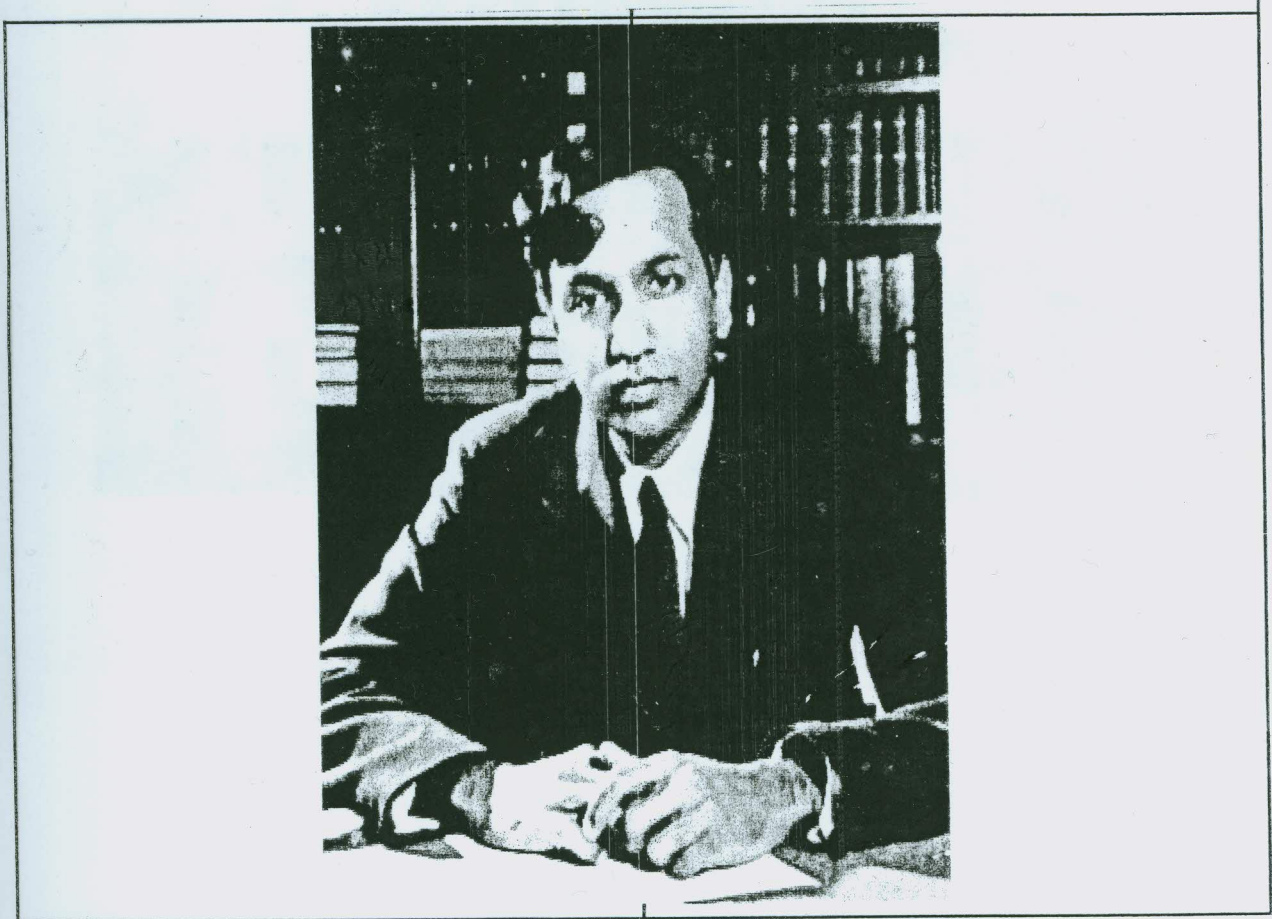
L.M. Sehgal

1. **SOME HISTORY, SOME
NOSTALGIE**
2. **UNDERSTANDING CP VIOLATION:
TRIUMPH OF CKM HYPOTHESIS**
2. **CP VIOLATION AND ARROWS
OF TIME**

CHANDIGARH 1961-62



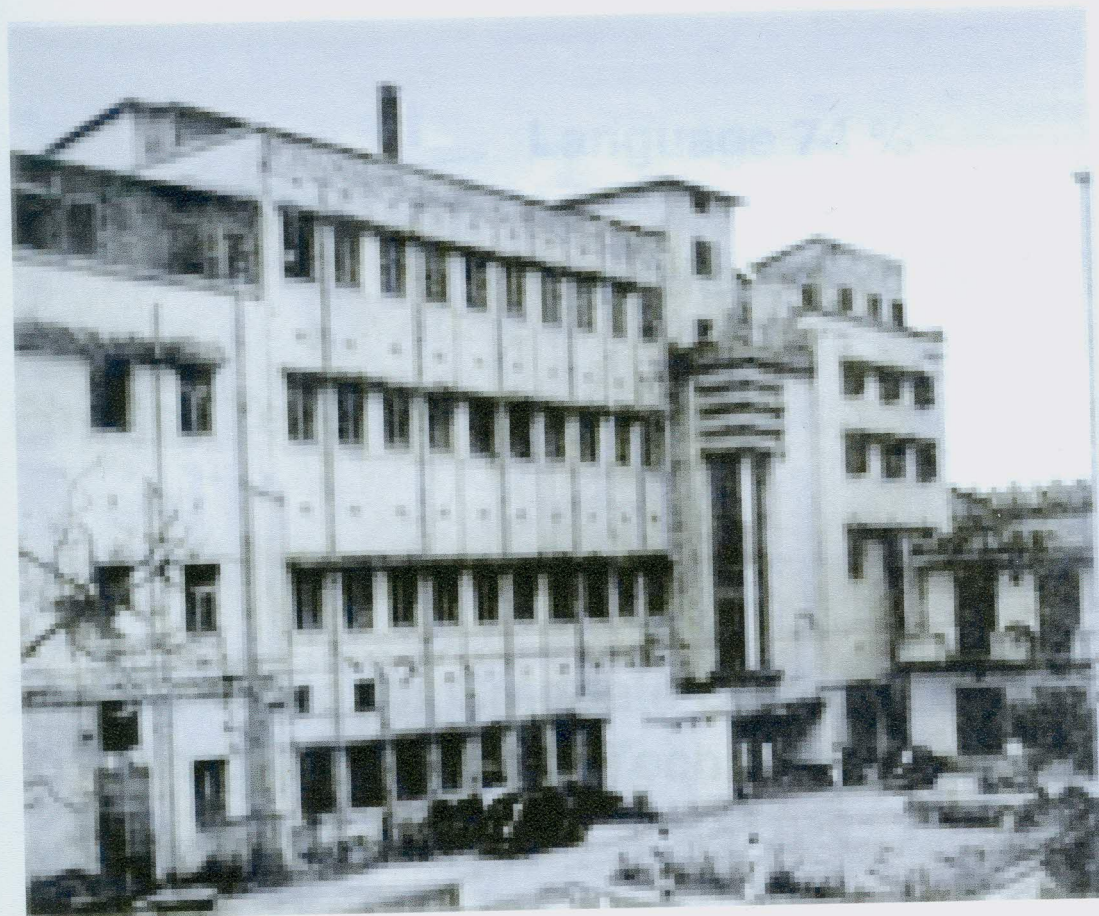
Physics Department, Panjab University



CALCUTTA 1962-63

1963: A Year of Good Things

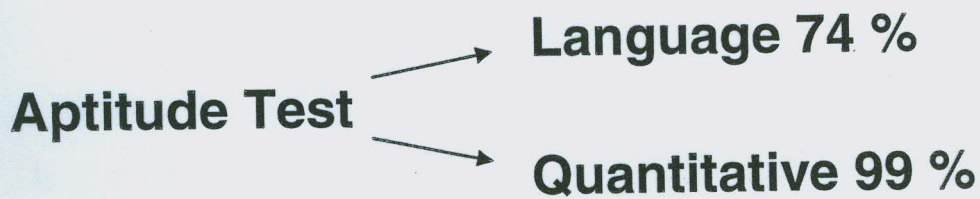
1. Graduate Program



Saha Institute of Nuclear Physics

1963: A Year of Good Tidings

1. Graduate Record Exam



Physics Test : 99 %

2. Fellowship for Graduate Study:
Carnegie Institute of Technology,
Pittsburgh

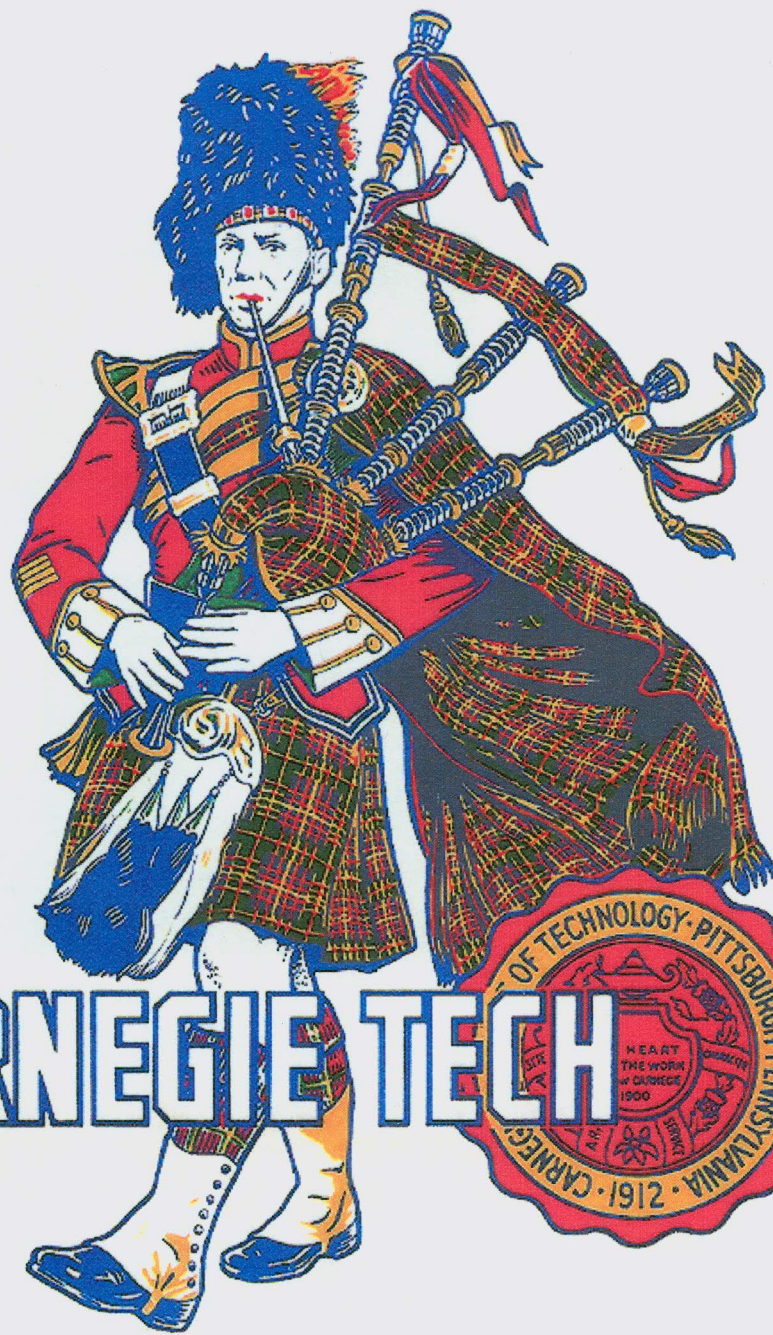
3. Fulbright award for travel to U.S.A.

BOMBAY, July 27, 1963

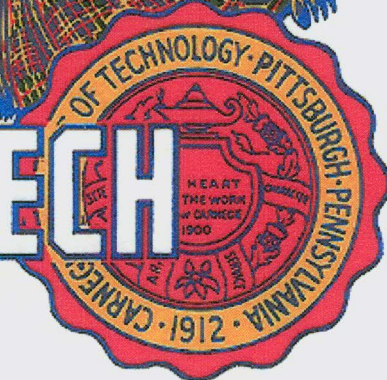


SS ORSOVA

PITTSBURGH, 1963-68



CARNEGIE TECH





Sergio De Benedetti

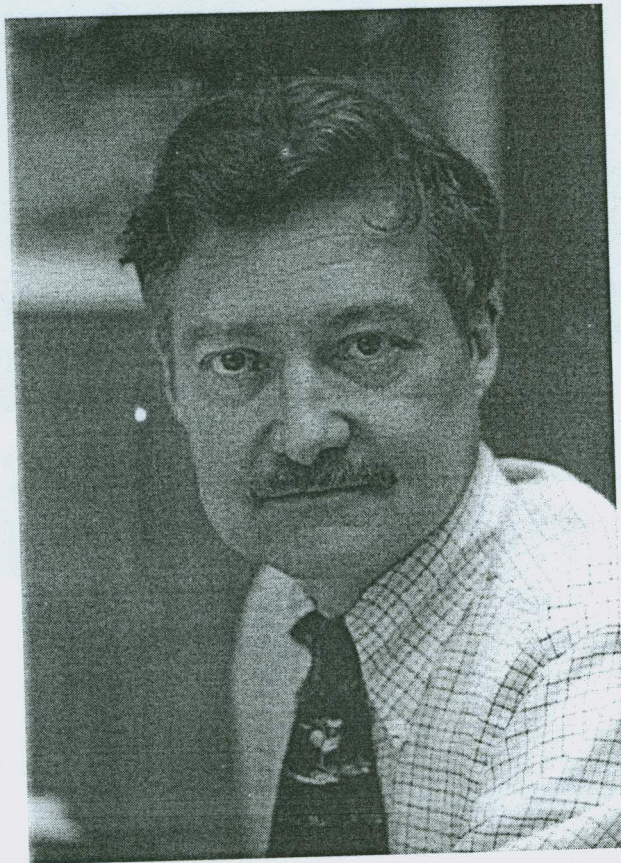
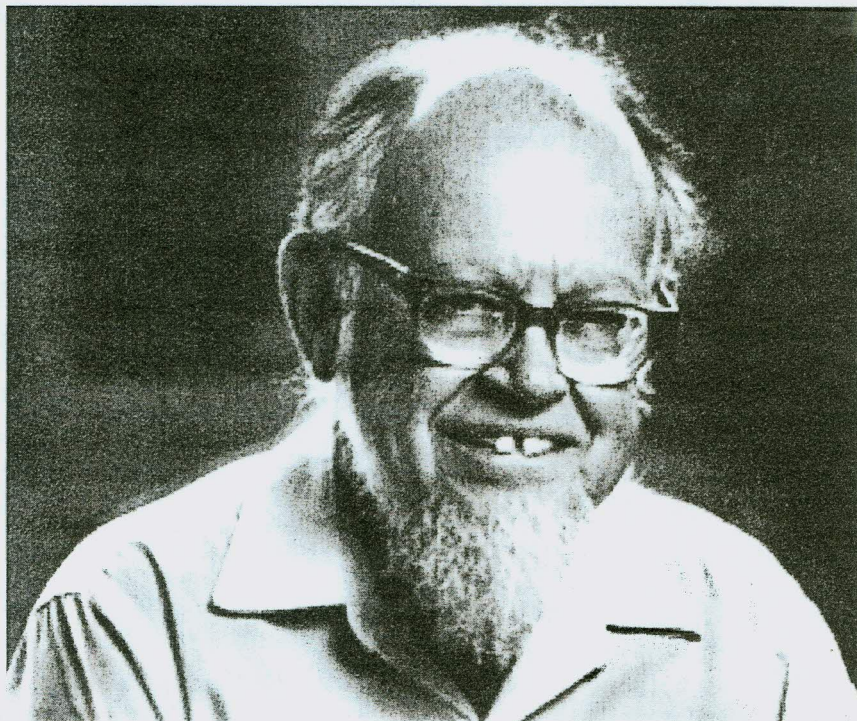


Figure 1: R. Cutkosky



Lionel Wolfenstein

1968-71: Tata Institute of Fundamental Research

BOMBAY

[T. Das, N. Mukunda, P. Divakaran, G. Rajasekaran, K.V.L. Sarma,
V. Singh, V. Gupta, S.M. Roy, D. Sankaranarayan, J. Pasupathy,
L. K. Pandit, and many others.]



IMPLICATIONS OF UNEQUAL CHARGE ASYMMETRY IN $K_L^0 \rightarrow \pi^\pm e^\mp \nu$ AND $K_L^0 \rightarrow \pi^\pm \mu^\mp \nu$

L. M. Sehgal
Tata Institute of Fundamental Research, Bombay, India
(Received 10 June 1968)

The possibility is considered that the charge asymmetries δ_e and δ_μ in the decays $K_L^0 \rightarrow \pi^\pm e^\mp \nu$ and $K_L^0 \rightarrow \pi^\pm \mu^\mp \nu$ might turn out to be different. Some implications, including a test of CPT, are pointed out.

Tests of CP and CPT Invariance in the Decay $K_L \rightarrow \bar{l}\bar{l}$

L. M. SEHGAL
Tata Institute of Fundamental Research, Bombay, India
(Received 29 January 1969)

Pais and Treiman have studied the implications of CP and CPT invariance for the decay $K_L \rightarrow \bar{l}\bar{l}$. We indicate how their results are modified when account is taken of the possibility of real intermediate states in this decay.

Electromagnetic Contribution to the Decays $K_S \rightarrow \bar{l}\bar{l}$ and $K_L \rightarrow \bar{l}\bar{l}^*$

L. M. SEHGAL
Tata Institute of Fundamental Research, Bombay, India
(Received 5 March 1969)

Using a model in which the decays $K_{S,L} \rightarrow \bar{l}\bar{l}$ occur through a two-photon intermediate state, and considering only the absorptive part of the amplitudes, we obtain lower bounds on the ratios $\text{Rate}(K_{S,L} \rightarrow \bar{l}\bar{l}) / \text{Rate}(K_{S,L} \rightarrow \gamma\gamma)$.

$\mu:e$ RATIO IN $\eta^0 \rightarrow \pi^0 l^+ l^-$ AND $X^0 \rightarrow \eta^0 l^+ l^-$ AS A TEST OF ELECTROMAGNETIC C NONINVARIANCE

L. M. Sehgal
Tata Institute of Fundamental Research, Bombay, India
(Received 23 April 1969)

If the decays $\eta^0 \rightarrow \pi^0 l^+ l^-$ occur via a C-nonconserving (isovector) electromagnetic interaction, the ratio $\Gamma(\eta^0 \rightarrow \pi^0 e^+ e^-) / \Gamma(\eta^0 \rightarrow \pi^0 \mu^+ \mu^-)$ should be 3.3. Similarly, if the decays $X^0 \rightarrow \eta^0 l^+ l^-$ are induced by a C-nonconserving (isoscalar) interaction, the ratio $\Gamma(X^0 \rightarrow \eta^0 e^+ e^-) / \Gamma(X^0 \rightarrow \eta^0 \mu^+ \mu^-)$ should be 2.9.

ELECTROMAGNETIC CORRECTIONS TO THE COHERENT K_L - K_S REGENERATION AMPLITUDE IN HYDROGEN

K. V. L. SARMA and L. M. SEHGAL
Tata Institute of Fundamental Research, Bombay 5, India

Received 8 February 1971

Abstract: Electromagnetic corrections to the coherent K_L - K_S regeneration amplitude from protons. $f_{21} = f(0) - \bar{f}(0)$ are estimated in a model based on elastic unitarity and Regge behaviour. The correction to $\text{Im} f_{21}/k$ is found to vanish asymptotically as $(\ln s)^{-2}$. The correction to $\text{Re} f_{21}/k$, assuming additivity of the Coulomb- and strong-phase shifts, is also finite. Numerical values are given at a typical energy.

T, P, and C Symmetries in $K_{L,S} \rightarrow \gamma\gamma$

L. M. Sehgal
Tata Institute of Fundamental Research, Bombay 5, India
(Received 8 February 1971)

The Bernstein-Michel analysis of $\pi^0 \rightarrow \gamma\gamma$ is applied to the decays $K_{L,S} \rightarrow \gamma\gamma$. It is shown that, in contrast to the situation in $\pi^0 \rightarrow \gamma\gamma$, a hypothetical violation of CP invariance in $K_{L,S} \rightarrow \gamma\gamma$ can, in principle, be detected by a measurement of the circular polarization of one of the two photons.

Sept. 1971 : RWTH Aachen



H. Faissner, K. Schultze, J. von Krogh, J. Morfin,
H. Reithler, E. Radermacher, K. Eggert, A. Böhm,
F. Hasert, H. Weerts, D. Lanske et al



Theorie : R. Rodenberg, D. Rein,
G. Köpp, B.R. Kim

June 1972 : Balatonfüred , Neutrino '72



R. P. Feynman , T. D. Lee , R. Marshak , V. Weisskopf ,
B. Pontecorvo , Y. Zeldovich , V. Gribov , V. Telegdi ,
F. Reines , R. Davis , J. Bahcall , B. Barish , D. Cline ,
C. Baltay et al

TIFR/TH/72-9

YANG-MILLS FIELDS AND THEORY OF WEAK
INTERACTIONS

G. RAJASEKARAN
Tata Institute of Fundamental Research
BOMBAY - 5



LECTURES GIVEN AT
SAHA INSTITUTE OF NUCLEAR PHYSICS
92, Acharya Prafulla Chandra Road
CALCUTTA-9

(JUNE, 1971)

(This was previously issued as a Saha Institute Report. The present version incorporates some minor corrections and an addendum.)

Dec. 1972 : Aachen Event

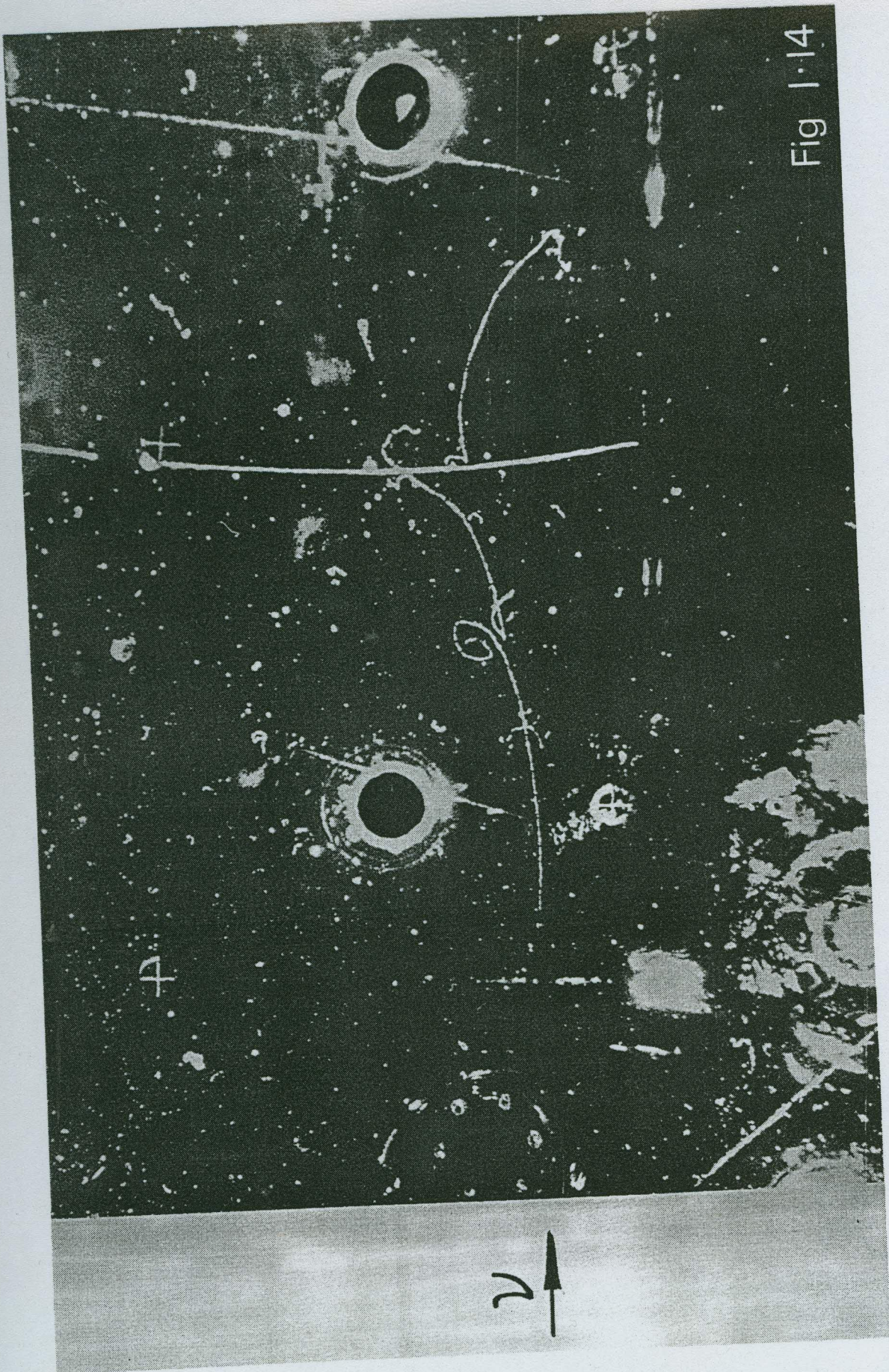


Fig 1.14

First Observation of $\bar{\nu}_\mu + e^- \rightarrow \bar{\nu}_\mu + e^-$

III. Physikalisches Institut

der Rheinisch-Westfälischen Technischen Hochschule

Aachen

PITHA-(1973) NR 68

Unified Theories of Weak and
Electromagnetic Interactions:
An Elementary Introduction

L.M. Sehgal

III. Physikalisches Institut
Technische Hochschule Aachen

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23698y cern ch

geneva 12.4.1973 our telex ref 4018 15.25 mh

dr lm sehgal
physikalisches institut
technische hochschule

could you kindly send us 25 additional copies of your report
pitha-(1973)nr 68, 'unified theories of weak and electromagnetic
interactions: an elementary introduction.

thank you

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t

TELEX

PREDICTIONS OF THE WEINBERG MODEL FOR NEUTRAL CURRENTS IN INCLUSIVE NEUTRINO REACTIONS*

L.M. SEHGAL

III. Physikalisches Institut, Technische Hochschule Aachen, Aachen, W-Germany

Received 19 June 1973

Abstract: We investigate the consequences of the Weinberg theory for neutral current reactions of the type $\nu(\bar{\nu}) + \text{nucleon} \rightarrow \nu(\bar{\nu}) + \text{hadrons}$, using a quark parton model. The total cross section ratios $R = \sigma(\nu \rightarrow \nu)/\sigma(\nu \rightarrow \mu^-)$ and $\bar{R} = \sigma(\bar{\nu} \rightarrow \bar{\nu})/\sigma(\bar{\nu} \rightarrow \mu^+)$ are obtained as functions of the Weinberg angle θ , and have the minimum values $R_{\min} = 0.17$, $\bar{R}_{\min} = 0.37$. An approximate relation between R and \bar{R} is obtained, which is independent of the Weinberg angle: $\frac{1}{2}(1 - 3R + \bar{R}) = [\frac{2}{3}(\bar{R} - R)]^{\frac{1}{2}}$. Predictions are made for the average ν and average Q^2 in comparison to those in charged current reactions. Preliminary results of the Gargamelle experiment are compared with the theory.

1. Introduction

The Weinberg model unifying weak and electromagnetic interactions predicts the existence of neutral lepton and neutral hadron currents in weak processes [1]. The coupling of such currents to each other should produce observable effects such as semi-leptonic reactions which are distinguished from the normal weak reactions by the fact that no charge is transferred from the lepton to the hadron system. Of particular interest is the prediction of neutrino induced reactions of the type $\nu(\bar{\nu}) + N \rightarrow \nu(\bar{\nu}) + \text{hadrons}$ ($N = \text{nucleon}$) which differ from the normal reactions $\nu(\bar{\nu}) + N \rightarrow \mu^-(\mu^+) + \text{hadrons}$ by the absence of a charged lepton in the final state. It was shown by Pais and Treiman [2] and by Paschos and Wolfenstein [3] that the inclusive cross sections for such neutral current reactions have, in the Weinberg model, lower limits which are quite large, and which therefore make these reactions suitable for an experimental test of the model.

The purpose of this paper is to examine closely the quantitative predictions of the Weinberg theory for neutral currents in inclusive neutrino reactions. We assume that the neutral current process, like its charged current counterpart, shows a scaling behaviour at high energies, and adopt a parton model for the description of the deep inelastic scattering [4–6]. The parton model employed is one which affords a satis-

* Work supported by the German Bundesministerium für Technologie and Wissenschaft.

1974: A Busy Year

January: - Seminar in Rutherford Lab
- Seminar in Trinity College, Dublin

February: - Plenary talk, DPG Tagung
Hamburg

March: - Visit to CERN (met Wolfenstein)

May: - Seminar in Liège

June: - Seminar in Karlsruhe

September: - Talk in Weak Interaction Meeting,
Strobl (got to know Pais)

+

Nine papers written !

13

ANL-HEP-PR-75-45

PHENOMENOLOGY OF NEUTRINO REACTIONS

L. M. Sehgal

III. Physikalisches Institut
Technische Hochschule Aachen
Aachen, W. Germany

(Lectures given at Argonne National Laboratory, August 1975)



U.S. GOVERNMENT PRINTING OFFICE: 1975 O 244-124

HIGH ENERGY PHYSICS DIVISION
ARGONNE NATIONAL LABORATORY
ARGONNE, ILLINOIS

ORGANISATION EUROPÉENNE POUR LA RECHERCHE NUCLÉAIRE
CERN EUROPEAN ORGANIZATION FOR NUCLEAR RESEARCH

SIEGE: GENEVE/SUISSE

CERN LABORATOIRE I

ADDRESS POSTAL / POSTAL ADDRESS:
1211 GENEVE 23
SUISSE / SWITZERLAND

27/2/76

Dear Sehgal:

I have been studying your notes with great profit to myself. They are clear and precise and to the point. I have also suggested, without success, that you be asked to give the lectures, since you know the material much better and will be there anyway, but they (Weyer) insist on an experimenter. I will, of course, try to stay as much as possible with experiment. But

may I ask if it would be possible for you to have a copy of your Argonne lectures for every student?

Sincerely yours
J Steinberger

1976 : Another Busy Year

- January:** - Seminar in Mainz
- February:** - Seminar in Strasbourg
- March:** - Seminar in Orsay
- May:** - Seminar in Bielefeld
- June:** - CERN School of Physics,
Wepion (Tutor to Jack
Steinberger)
- Neutrino Conference, Aachen
- July:** - Seminar in Siegen
- August:** - Gordon Conference, Tilton, NH
(talk)
- Seminar in Brookhaven
- September:** - Minerva Symposium,
Kleinwalsertal (talk)
- November:** - Seminar in Heidelberg
- Seminar in Dortmund
- Seminar im CERN
- December:** - Seminar in Bonn
- Seminar in Wuppertal

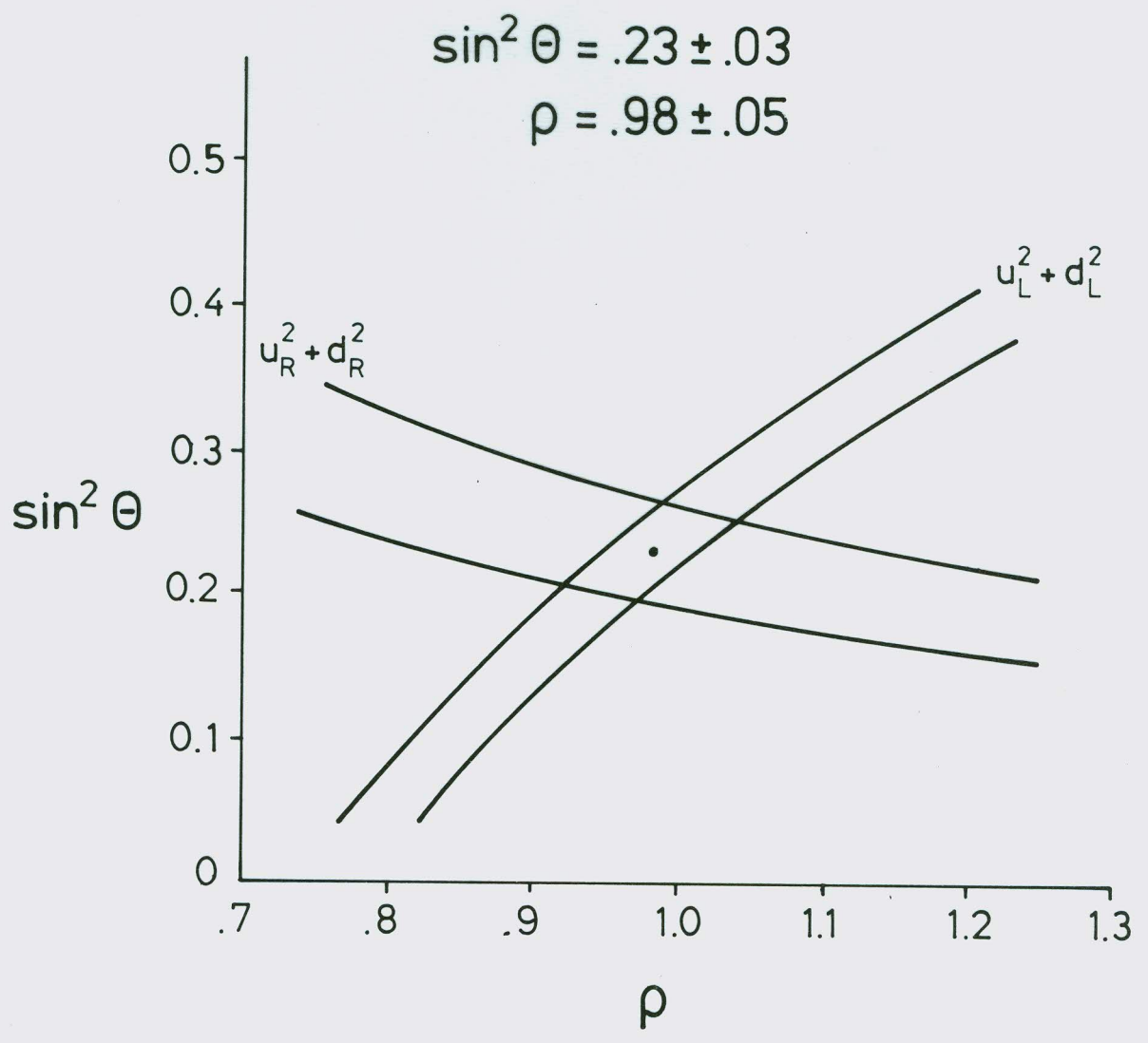
Neutrino Conference Aachen 1976

Highlights

1. Neutral Currents (Sakurai, Gourdin)
2. Charm (De Rujula, Gaillard)
3. τ -Lepton (Perl)
4. CP Violation (Wolfenstein)
5. Reactor Neutrinos (Reines)
6. Proposal: $\bar{p}p$ Collider (Rubbia)
7. Summary (B. W. Lee)



Neutrino '78 Conference Purdue



A Salaam To A. Salam

THIS article is a salute, a salaam, to Abdus Salam, who was awarded the Nobel Prize in Physics recently for his work on the unification of two forces of nature in one mathematical scheme.

He was born in Jhang town of the Punjab (now in West India) on January 29, 1926. He is a citizen of Pakistan although he has lived and worked outside it for the last 25 years. Salam belongs to the Ahmadiya sect which is a branch of Islam. Ahmed, who died in 1860 near Amritsar in 1908. It is of interest to know that Ahmed proclaimed himself as the Mahad as well as the Messiah, and he predicted Jihad as striving for followers to seek knowledge and serve others.

Pakistan in its peculiar character for the purity of Islam, however, declared Ahmadiyas as non-Muslims, a few years ago. Salam is as good a Muslim as do the decreed devotees (Namas) regularly. He attributed the Nobel award to the Grace of Allah and has donated the prize money to the benefit of Pakistan's children all that he would like to see is that the benefit of Pakistan's children which is \$ 60,000, since he shares it with the Americans, Weisberg and Ghoshlow.

Salam, took a masters' degree from the University of Delhi, allied to get a job at the Delhi Institute of Technology. A similar situation arose later when Hargebid Khorana could not find employment in India. He had to go to London already two many molecular biologists in India. Salam got a "small farmer's" scholarship from the Punjab, went to England and took a Ph.D. from Cambridge, in 1952, years which he worked for three years in the Physics Department of the University of Cambridge. He had to abandon this post, however, because he found it impossible to establish a school of research. Yet, he was contented with it. He was a non-Muslim. Interestingly, he was co-authored a report entitled "Resurrection of Ahmadiyas" in Pakistan.

Salam was elected Fellow of the Royal Society of London in 1959. He was awarded the Nobel Prize in 1979. He has also been given the Hughes medal and the Royal Institute Medal. He is a member of the Royal Society of Sciences and the International Union of Pure and Applied Physics. He is also a member of the International Union of Theoretical Physics. He has received several other honours and awards, including the Padma Vibhushan in India. He is a very concerned person about the unification of physics and the search for a grand theory.

some of the participating particularly can never be made visible. Salam cannot yet be made from the explanation of physics. Salam is an Indian scientist. L. M. Sehgal, working in Germany, made the most detailed analysis of the Gargamelle results to allow that they strongly corroborate the new theory of weak interactions (with Marshak) in 1957. And G-S-W theory could not simply have taken off without the crucial recent work of effacing young Gt. of the Netherlands. Nor can one, in all fairness, leave out in the cold the experimental physicists and engineers without whose efforts the democratic process requiring the

I am sure the Nobel committee was in a fix. The physics prizes have usually been given to one person, sometimes to two and rarely to three for the same reason. Salam's committee must revise their idea and must be coming more and more of democratic process requiring the

proceeded so far as to claim that



A TOAST TO SCIENCE: Abdus Salam at the banquet-table with Queen Silvia of Sweden. The dinner to honour this year's Nobel Laureates was held at Stockholm's town-hall on December 10.

force exerted by the earth on the apple is precisely the same as that of the small apple on the earth. Salam showed that the symmetric properties of working of clocks are affected by gravitating bodies, and this is Newton's theory extended to a modification. But even Einstein's theory is not clear as to how gravitational effects are propagated.

The second type of interaction is electric. Salam showed that day who showed through experiments that electric and magnetic forces are connected with each other. He demonstrated this first in his life on Christmas morning. He showed that the revolution of magnetic needle around an electric current

Maxwell put the laws of electrodynamics so marvellous that when the great German physicist, Boltzmann, saw them he exclaimed, "Who was the God who made these things?" Salam's theory of electrodynamics is now known as photons. But efforts to unify gravity and electromagnetism have not

succeeded. Einstein attempted unification of gravitation for more than 25 years but confessed that he had failed. A little before his death, he told his son that he wished he knew forces between masses. The electrical forces between masses are enormously greater than the gravitational forces. The above two forces suffered to explain all of physics until about the year 1900 when the interaction of the atom was explored, and new types of fundamental particles even smaller than the smallest atoms were discovered, things changed.

Let us now come to the third force or the strong nuclear force. The nucleus is surrounded by particles which are much lighter than the nucleons. Each nucleon has the same proton but of more massive proton but of opposite sign. There is a lot of empty space between the nucleons and the electrons but the two charges are equal and the negative charges are electrically neutral as a whole.

The following question now arises. How does the nucleus not itself remain stable? Why does it not break up due to the well-known repulsion of like electrical charges to explain this stability is expressed in mathematics as follows:

It needs just four principles or laws to explain its entire mystic. Salam and Ghoshlow-Salam-Weisberg theory makes a bold bid to explain the ultimate laws to unify the forces of nature. Salam's theory can be explained in terms of the new theory of interactions or forces which create how things will happen. The four interactions are: gravitational, electromagnetic, strong, and weak. Salam's theory explains them in a very simple way. Salam's theory is based on the principle of symmetry. Salam's theory is based on the principle of symmetry. Salam's theory is based on the principle of symmetry.

1934. The interaction was later named as weak, because it was less than even the electromagnetic interaction.

Nearly 20 years elapsed before any significant development occurred. Suffice it to say here that Sudarshan and Salam both made important contributions in 1957. The formalism is called, and the later by his two-component theory of the neutrino. These ideas developed in the "charm" theory of Salam and Weinberg (G-S-W) who now presented a theory which brings under one umbrella, the electromagnetic and weak interactions.

A new theory must go beyond itself and predict new phenomena but not into the theory, or known particles. The G-S-W theory predicts the exchange of currents of neutral particles in addition to currents of charged particles in weak interactions. This prediction was verified by the Gargamelle experiment mentioned earlier. I might add with possible objections to the theory, the human

The verification of the new theory for which Abdus Salam, the Pakistani physicist, shares the Nobel Prize with two Americans, was based on the efforts of a multitude of scientists. Though there is no dearth of able scientists in India, we have neither the equipment nor an environment which can stimulate original contributions, says G. H. KESHWAN, a Jawaharlal Nehru fellow.

In another period of 10-12 minutes, half of the remainder of the remaining one-quarter and so on. This theory lives looks simple but it really involves causality because there is no way of telling which neutrinos of decay earlier. It is a matter of half-life of a neutrino. Neutrons left to themselves break up at the rate stated in a proton. Salam's theory is based on the principle of symmetry. Salam's theory is based on the principle of symmetry.

Some gratuitous assumptions have been made in the theory: for example, "spontaneous breaking of symmetry" which is really a mere "trick". While the principle is valid for electromagnetic interactions, it does not hold for weak interactions and yet the new theory is called a unified theory of weak interactions. Salam's theory is based on the principle of symmetry. Salam's theory is based on the principle of symmetry.

It is well known that the Indian (or Pakistani) scientists abroad, mostly through their own initiative, have acquired a reputation for their work. Salam's theory is based on the principle of symmetry. Salam's theory is based on the principle of symmetry. Salam's theory is based on the principle of symmetry.

1991. These particles within the smallest of atoms are supposed to have masses as high as that of the electron. Salam's theory is based on the principle of symmetry. Salam's theory is based on the principle of symmetry. Salam's theory is based on the principle of symmetry.

Let me comment on the question of priority. All too many scientists are human, all too human. For many years American physicists would not credit Salam who had developed his ideas in London but had received his Ph.D. from the University of Chicago in 1957. But Salam's lecture at the Nobel Symposium in 1968 clearly showed how deeply he had thought about the subject. It was only in 1972, at the Gargamelle Conference, in the presence of Weinberg, that Salam's simultaneous formulations of 1967 were conceded after a battle royal.

Salam has always been a good friend. As I said earlier, some people are not very understanding of weak interactions. Salam had been taken by E.C.G. Sudarshan. So, when a mutual friend visited Salam after the award, he sent a friendly message to Sudarshan. Salam is a very young man, but he is not a young man.

Finally, I must mention the sociological aspects of the search in physics. First-rate work is now possible only in a certain milieu. This means sophisticated and costly equipment and stimulating intellectual atmosphere. There are a few centres in India, notably TIFR, Indian scientists are far, far away from this milieu.

It is up to our government to make the conditions propitious for participating in large scale programmes available for the European community and similar programmes in the U.S.A. Our embassies in these countries should be active in these matters.

It is well known that the Indian (or Pakistani) scientists abroad, mostly through their own initiative, have acquired a reputation for their work. Salam's theory is based on the principle of symmetry. Salam's theory is based on the principle of symmetry. Salam's theory is based on the principle of symmetry.

My point is that there are many times over, our scientists in India were given opportunities to work under the full gaze of the world.



Cours/Lecture Series

1982-1983 ACADEMIC TRAINING PROGRAMME

Title "Electroweak Interactions"

Lecturer L.M. SEHGAL (Institute of Physics, RWTH, Aachen)

Dates November 18, 19, 22, 23, 24, 25 & 26, 1982

Time 11h to 12h

Place Auditorium

Abstract We shall review the theoretical foundations and empirical status of the standard model of weak and electromagnetic interactions.

The following topics will be covered (tentative) :

1. Theoretical Perspective
2. Charged Currents
3. Neutral Currents
4. Forbidden Reactions
5. Vector Quanta (Intermediate Bosons)
6. Scalar Quanta (Higgs Particles)
7. Problems on the Frontier

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EXPERIMENTAL OBSERVATION OF ISOLATED LARGE TRANSVERSE ENERGY ELECTRONS
WITH ASSOCIATED MISSING ENERGY AT $\sqrt{s} = 540$ GeV

UA1 Collaboration, CERN, Geneva, Switzerland

G. ARNISON^j, A. ASTBURY^j, B. AUBERT^b, C. BACCIⁱ, G. BAUER¹, A. BÉZAGUET^d, R. BÖCK^d,
 T.J.V. BOWCOCK^f, M. CALVETTI^d, T. CARROLL^d, P. CATZ^b, P. CENNINI^d, S. CENTRO^d,
 F. CERADINI^d, S. CITTOLIN^d, D. CLINE¹, C. COCHET^k, J. COLAS^b, M. CORDEN^c, D. DALLMAN^d,
 M. DeBEER^k, M. DELLA NEGRA^b, M. DEMOULIN^d, D. DENEGRI^k, A. Di CIACCIOⁱ,
 D. DiBITONTO^d, L. DOBRZYNSKI^g, J.D. DOWELL^c, M. EDWARDS^c, K. EGGERT^a,
 E. EISENHANDLER^f, N. ELLIS^d, P. ERHARD^a, H. FAISSNER^a, G. FONTAINE^g, R. FREY^h,
 R. FRÜHWIRTH¹, J. GARVEY^c, S. GEER^g, C. GHESQUIÈRE^g, P. GHEZ^b, K.L. GIBONI^a,
 W.R. GIBSON^f, Y. GIRAUD-HÉRAUD^g, A. GIVERNAUD^k, A. GONIDEC^b, G. GRAYER^j,
 P. GUTIERREZ^h, T. HANSL-KOZANECKA^a, W.J. HAYNES^j, L.O. HERTZBERGER², C. HODGES^h,
 D. HOFFMANN^a, H. HOFFMANN^d, D.J. HOLTHUIZEN², R.J. HOMER^c, A. HONMA^f, W. JANK^d,
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 R. KINNUNEN^e, H. KOWALSKI^d, W. KOZANECKI^h, D. KRYN^d, F. LACAVA^d, J.-P. LAUGIER^k,
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 J. RICH^k, M. RIJSSENBECK^d, C. ROBERTS^j, J. ROHLF^d, P. ROSSI^d, C. RUBBIA^d, B. SADOULET^d,
 G. SAJOT^g, G. SALVI^f, G. SALVINIⁱ, J. SASS^k, J. SAUDRAIX^k, A. SAVOY-NAVARRO^k,
 D. SCHINZEL^f, W. SCOTT^j, T.P. SHAH^j, M. SPIRO^k, J. STRAUSS¹, K. SUMOROK^c, F. SZONCSO¹,
 D. SMITH^h, C. TAO^d, G. THOMPSON^f, J. TIMMER^d, E. TSCHESLOG^a, J. TUOMINIEMI^e,
 S. Van der MEER^d, J.-P. VIALLE^d, J. VRANA^g, V. VUILLEMIN^d, H.D. WAHL¹, P. WATKINS^c,
 J. WILSON^c, Y.G. XIE^d, M. YVERT^b and E. ZURFLUH^d

Aachen^a—Anncy (LAPP)^b—Birmingham^c—CERN^d—Helsinki^e—Queen Mary College, London^f—Paris (Coll. de France)^g
 —Riverside^h—Romeⁱ—Rutherford Appleton Lab.^j—Saclay (CEN)^k—Vienna¹ Collaboration

Received 23 January 1983

We report the results of two searches made on data recorded at the CERN SPS Proton–Antiproton Collider: one for isolated large- E_T electrons, the other for large- E_T neutrinos using the technique of missing transverse energy. Both searches converge to the same events, which have the signature of a two-body decay of a particle of mass ~ 80 GeV/ c^2 . The topology as well as the number of events fits well the hypothesis that they are produced by the process $\bar{p} + p \rightarrow W^\pm + X$, with $W^\pm \rightarrow e^\pm + \nu$; where W^\pm is the Intermediate Vector Boson postulated by the unified theory of weak and electromagnetic interactions.

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2. Understanding CP Violation : Kobayashi-Maskawa Hypothesis ('73)

Essential Idea : $SU(2) \times U(1)$
theory with 3 quark doublets

Opened up new vistas for exploration of CP violation.

CP no longer a dead-end street.

Focus moved from

K-mesons to **B**-mesons,
from

Strangeness to Beauty

Thirty-five years later, the K-M hypothesis had passed all crucial experimental tests.

⇒ Nobel prize 2008

(3rd major triumph of the $SU(2) \times U(1)$ theory)

1973 : Kobayashi-Maskawa

CP-violation in framework of $SU(2) \times U(1)$ gauge theory.

With two doublets of quarks, charged current interaction is

$$\mathcal{L}_{CC} = \frac{g}{2\sqrt{2}} \overline{u \ c} \gamma_{\mu} \frac{1-\gamma_5}{2} U \begin{pmatrix} d \\ s \end{pmatrix} W^{\mu}$$

$U = 2 \times 2$ unitary matrix

$$= \begin{pmatrix} U_{ud} & U_{us} \\ U_{cd} & U_{cs} \end{pmatrix}$$

Effective Hamiltonian for $\Delta S = 1$ interaction

$$H_{\text{eff}}(s \rightarrow d) \approx U_{ud} U_{us}^* (\bar{d}u)(\bar{u}s) + U_{cd} U_{cs}^* (\bar{d}c)(\bar{c}s)$$

CP Violation requires a relative phase between $U_{ud} U_{us}^*$ and $U_{cd} U_{cs}^*$

However, unitarity \Rightarrow

$$U_{ud} U_{us}^* + U_{cd} U_{cs}^* = 0$$

\Rightarrow CP violation impossible.

$$\begin{array}{c} \xleftarrow{U_{cd} U_{cs}^*} \\ \xrightarrow{U_{ud} U_{us}^*} \end{array}$$

This can also be understood as follows:
The most general 2×2 unitary matrix is

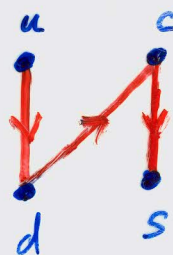
$$U = \begin{pmatrix} \cos \theta e^{i\alpha} & \sin \theta e^{i\beta} \\ -\sin \theta e^{i\gamma} & \cos \theta e^{i\delta} \end{pmatrix}$$

$$U^\dagger U = U U^\dagger = 1 \Rightarrow \alpha + \delta = \beta + \gamma \Rightarrow 4 \text{ real par.}$$

Choose 3 relative phases among 4 quarks
such that $\alpha = \beta = \gamma = 0$

$$\text{Unitarity} \Rightarrow \delta = 0.$$

$$\Rightarrow U = \begin{pmatrix} \cos \theta & \sin \theta \\ -\sin \theta & \cos \theta \end{pmatrix}$$



= Cabibbo matrix (real, orthogonal).

With three quark doublets

$$\mathcal{L}_{cc} = \frac{g}{2\sqrt{2}} \overline{\begin{pmatrix} u & c & t \end{pmatrix}} \gamma_\mu \frac{1-\gamma_5}{2} V \begin{pmatrix} d \\ s \\ b \end{pmatrix} W^\mu$$

$V = 3 \times 3$ unitary matrix

$$= \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix}$$

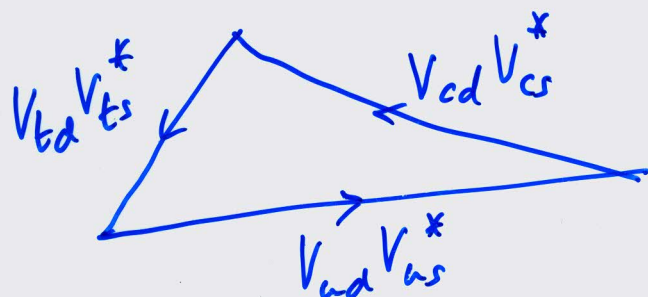
Effective Hamiltonian for $\Delta S = 1$ transitions now has the form

$$\begin{aligned}
 H_{\text{eff}}(s \rightarrow d) \approx & V_{ud} V_{us}^* (\bar{d} u) (\bar{u} s) \\
 & + V_{cd} V_{cs}^* (\bar{d} c) (\bar{c} s) \\
 & + V_{td} V_{ts}^* (\bar{d} t) (\bar{t} s)
 \end{aligned}$$

Unitarity condition:

$$V_{ud} V_{us}^* + V_{cd} V_{cs}^* + V_{td} V_{ts}^* = 0$$

This is a closed triangle in the complex plane:



(F1)

Conclusion: $H_{\text{eff}}(s \rightarrow d)$ contains terms whose coefficients are complex relative to one another \Rightarrow CP Violation!

The above figure (F1) is an example of a Unitarity Triangle.

Properties of Unitarity Triangles

- (i) There are six triangles corresponding to the effective Hamiltonians $H_{\text{eff}}(s \rightarrow d)$, $H_{\text{eff}}(b \rightarrow d)$, $H_{\text{eff}}(b \rightarrow s)$, $H_{\text{eff}}(t \rightarrow u)$, $H_{\text{eff}}(t \rightarrow c)$ and $H_{\text{eff}}(c \rightarrow u)$.

The relevant equations are

$$V_{ud} V_{us}^* + V_{cd} V_{cs}^* + V_{td} V_{ts}^* = 0 \quad (s \rightarrow d)$$

$$V_{ud} V_{ub}^* + V_{cd} V_{cb}^* + V_{td} V_{tb}^* = 0 \quad (b \rightarrow d)$$

etc.

- (ii) All unitarity triangles have the same area.

Reason: $\text{Im} (V_{\alpha j} V_{\beta k} V_{\alpha k}^* V_{\beta j}^*) = \pm J$

$\beta \neq \alpha$
 $j \neq k$

The parameter J is a universal measure of CP violation in all flavour-changing interactions. Area of triangle = $\frac{1}{2} J$.

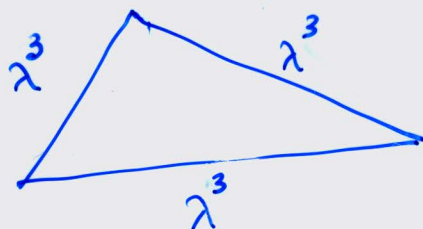
- (iii) Different unitarity triangles have different shapes. Reason: hierarchical structure of quark mixing matrix:

$$|V| \sim \begin{pmatrix} 1 & \lambda & \lambda^3 \\ \lambda & 1 & \lambda^2 \\ \lambda^3 & \lambda^2 & 1 \end{pmatrix} \quad \lambda \sim 0.2$$

Consequence: U_T for $s \rightarrow d$ transitions has the shape



while that for $b \rightarrow d$ has the form



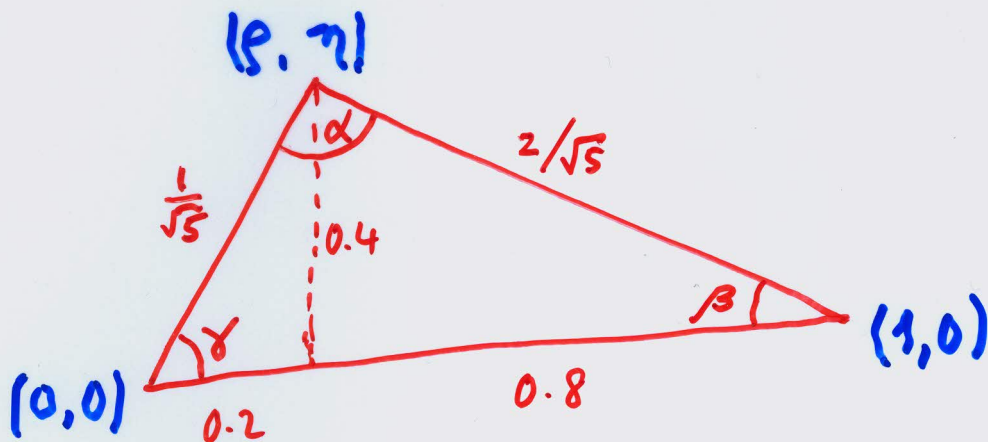
This accounts for the diversity of CP-viol. effects in various sectors, even though the areas of all triangles are universal.

(iv) Sides of a triangle are determined by the moduli $|V_{ij}|$, which can be measured in CP-conserving processes. Knowledge of sides fixes the angles of the triangle, which (if $\neq 0, \pi$) are measures of CP violation. Example of unification of CP-violating and CP-conserving phenomena.

Rough dimensions of Unitarity Triangle:

ca. 2000

$$\rho = 0.2, \quad \eta = 0.4$$



$$\alpha = 90^\circ$$

$$\beta = \tan^{-1}\left(\frac{1}{2}\right) \sim 25^\circ$$

$$\gamma = \tan^{-1}(2) \sim 65^\circ$$

Status 2011

$$\rho = 0.144^{+0.027}_{-0.018}$$

$$\eta = 0.343^{+0.014}_{-0.014}$$

$$\alpha = 89 \pm 4^\circ$$

$$\beta = 21 \pm 1^\circ$$

$$\gamma = 68 \pm 13^\circ$$

4

Date: Wed, 15 Oct 1997 11:30:06 -0400
From: cox@uvahep.phys.virginia.edu
To: sehgal@physik.rwth-aachen.de
Subject: Questions concerning asymmetries in $K^0_L \rightarrow \pi^+ \pi^- e^+ e^-$

Dear Professor Sehgal,

I attempted to get in touch with you in August and am trying again. Please let me know if you get this message.

My group has observed the $K^0_L \rightarrow \pi^+ \pi^- e^+ e^-$ decay in the data that we recent took in the KTEV experiment run at Fermilab. We have much greater sensitivity than previous experiments and see this mode quite easily. I expect to have between two and three thousand events eventually when the entire data sample is process from several months of running for rare K decays.

The bottom line is that we see very clearly the CP violating asymmetry in the angle between the normals to the $e^+ e^-$ and the $\pi^+ \pi^-$ planes that you predicted in PR D46 of August 1992. My problem is that we would like to have the non-integrated matrix element for our acceptance calculations rather than experession (16) of that paper which is already integrated over the angle of the positron in the $e^+ e^-$ center of mass with respect to the dirction of the $\pi^+ \pi^-$ system in the $e^+ e^-$ frame of reference and the angle of the positive pi with respect to the direction of the $e^+ e^-$ in the $\pi^+ \pi^-$ frame of reference. Is a non integrated expression available? It would help greatly if we could obtain this from you.

With a few thousand events, we are beginning to look at the other angles in the decay (other than the angle between the normals to the $e^+ e^-$ and the $\pi^+ \pi^-$ plane in the K^0_L CMS) to see if there is any hint of an asymmetry which would indicate an unusual source of direct CP violation. We have been using your PR D48 article with Heiliger as a guide to the search for such anomalous direct CP violation. However, there is a question concernring the coordinate systems. You give a description in words of the angle theta (essentially what I used above when describing the angle of the positron in the $e^+ e^-$ center of mass). However, you give a second definition in terms of cross products at a slightly later point in the paper. The two definitions appear to be different. Can you reiterate the definition of the angle theta for us?

I hope to hear from you soon. It would be good to get this result out. The data is very pretty and agrees with your predictions very well.

Brad Cox

CP violation in the decay $K_L \rightarrow \pi^+ \pi^- e^+ e^-$

L. M. Sehgal

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(Received 28 February 1992)

Direct and indirect CP violation in the decay $K_L \rightarrow \pi^+ \pi^- e^+ e^-$

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(Received 10 May 1993)

The decay $K_L \rightarrow \pi^+ \pi^- e^+ e^-$ is analyzed in a model containing (i) a CP -conserving amplitude associated with the $M1$ transition in $K_L \rightarrow \pi^+ \pi^- \gamma$, (ii) an indirect CP -violating amplitude related to the bremsstrahlung part of $K_L \rightarrow \pi^+ \pi^- \gamma$, and (iii) a direct CP -violating term associated with the short-distance interaction $s\bar{d} \rightarrow e^+ e^-$. Interference of the first two components produces a large CP -violating asymmetry ($\sim 14\%$) in the distribution of the angle Φ between the $e^+ e^-$ and $\pi^+ \pi^-$ planes. The full angular distribution contains two further CP -violating observables. Effects of direct CP violation are found to be numerically small.

PACS number(s): 13.20.Eb, 11.30.Er

I. INTRODUCTION

The decay $K_L \rightarrow \pi^+ \pi^- e^+ e^-$ can be envisaged, in the first instance, as a conversion process related to the decay $K_L \rightarrow \pi^+ \pi^- \gamma$. The latter is empirically known to contain two components: a bremsstrahlung piece related to the CP -violating decay $K_L \rightarrow \pi^+ \pi^-$ and a CP -conserving magnetic dipole component. Interference of these terms produces a CP -violating circular polarization of the photon in $K_L \rightarrow \pi^+ \pi^- \gamma$. The conversion process $K_L \rightarrow \pi^+ \pi^- e^+ e^-$ may be viewed as a means of probing this polarization by studying the correlation of the $e^+ e^-$ plane relative to the $\pi^+ \pi^-$ plane.

In a recent paper [1], a calculation of the decay $K_L \rightarrow \pi^+ \pi^- e^+ e^-$ was carried out in which the amplitude was determined by the two empirically known components of the radiative decay [2]. In addition, a virtual photon component $K_L \rightarrow \pi^+ \pi^- \gamma^*$ (absent for a real photon) was introduced, in the form of a K^0 charge-radius contribution. The branching ratio was determined to be $\sim 3 \times 10^{-7}$. A significant CP -violating asymmetry was found in the Φ distribution of the process, Φ being the angle between the $e^+ e^-$ and $\pi^+ \pi^-$ planes.¹

$$\mathcal{A} = \frac{\int_0^{\pi/2} \frac{d\Gamma}{d\Phi} d\Phi - \int_{\pi/2}^{\pi} \frac{d\Gamma}{d\Phi} d\Phi}{\int_0^{\pi/2} \frac{d\Gamma}{d\Phi} d\Phi + \int_{\pi/2}^{\pi} \frac{d\Gamma}{d\Phi} d\Phi}$$

$$= 15\% \sin[\Phi_{+-} + \delta_0(m_K^2) - \bar{\delta}_1]$$

$$\approx 14\%$$

(1)

Here Φ_{+-} is the phase of the CP -violating parameter η_{+-} , $\delta_0(M_K^2)$ is the $I=0$ $\pi\pi$ s -wave phase shift at $s_\pi = M_K^2$, and $\bar{\delta}_1$ is an average $\pi\pi$ p -wave phase shift in the domain $0 < s_\pi < M_K^2$. The result (1) represents one of the largest calculable CP -violating effects in the decays of the K^0 - \bar{K}^0 system.

The effect found in Ref. [1] arose entirely from the bremsstrahlung decay of the K_1 admixture in the K_L wave function. In this sense, it is an example of "indirect" CP violation. One of the purposes of the present paper is to examine the consequences of a "direct" CP -violating amplitude² in $K_L \rightarrow \pi^+ \pi^- e^+ e^-$ associated with the short-distance interaction $s\bar{d} \rightarrow e^+ e^-$. In addition, we extend the analysis of Ref. [1], by looking at the complete angular distribution of the final state. This enables us to identify two further CP -violating observables. The method of calculation adopted here is quite different from that followed in Ref. [1], and permits an independent check of the results presented there.

II. MATRIX ELEMENT

The decay amplitude of

$$K_L(P) \rightarrow \pi^+(p_+) \pi^-(p_-) e^+(k_+) e^-(k_-)$$

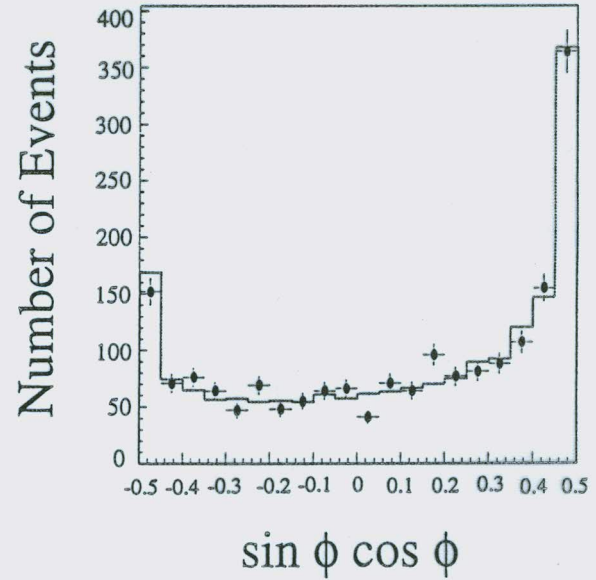
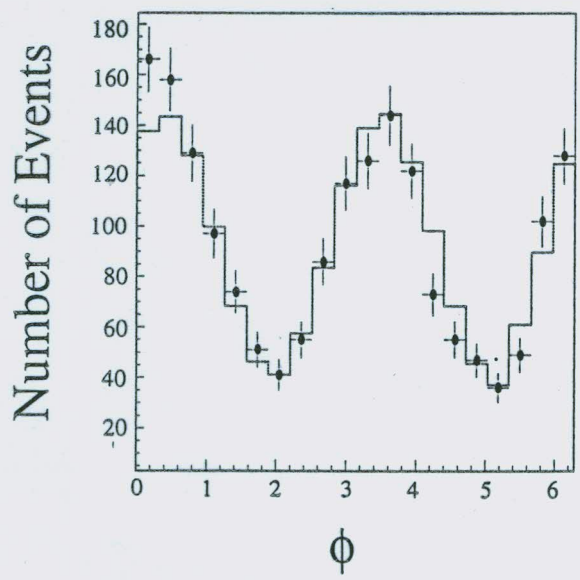
in our model has the form

$$\mathcal{M}(K_L \rightarrow \pi^+ \pi^- e^+ e^-) = \mathcal{M}_{\text{br}} + \mathcal{M}_{\text{mag}} + \mathcal{M}_{\text{CR}} + \mathcal{M}_{\text{SD}}^{V,A},$$

(2)

Measured Angular Asymmetry
in $K_L \rightarrow \pi^+ \pi^- e^+ e^-$ Decays

Black points are KTeV data
Red line is Monte Carlo prediction



Asymmetry = $(14.6 \pm 2.3 \text{ (stat)} \pm 1.1 \text{ (syst)}) \%$
(preliminary)

Agrees with prediction by Sehgal and Wanninger

PHYSICS

Particle Decays Reveal Arrow of Time

of the fossils. "Everybody would say yes, these are small shellies," agrees paleontologist Douglas Erwin of the National Museum of Natural History in Washington, D.C., who has seen Azmi's paper. The question is what they mean for the age of the tracks.

In the early 1980s, Azmi found similar fossils in another Indian basin, boosting its accepted age by 400 million years into the Cambrian. He thinks the new fossils hold a similar message about the sandstone layer they overlie. As he argues in a letter on page 627, there's not much rock separating the 540-million-year-old fossils from Seilacher's trace fossils—implying that the tracks must be about 600 million, not 1.1 billion, years old. That would make them no older than other known traces of early animals.

Azmi and others add that the radiometric dates aren't as impressive as they might seem. As geochronologist Samuel Bowring of the Massachusetts Institute of Technology notes, the dates might accurately reflect the age of individual mineral grains, but those grains may have formed long before they eroded from parent rock and washed into the sea to become part of the Vindhyan sedimentary rocks. Indeed, the radiometric dates of grains from the formation containing the Cambrian fossils are also about 1.1 billion years old, suggesting that the dates may not reflect the age of the rock layer itself.

Seilacher, Pflüger, and their colleague Pradip Bose of Jadavpur University in Calcutta are just now seeing the details of Azmi's paper, but they already have some reservations. Pflüger speculates that perhaps Azmi's Cambrian fossils are not close in time to the trace fossils after all. Thick layers of sediment may be laid down in one place but not in another, and rocks can be eroded away before the next layer is laid down, making it look as if little time has passed when in fact hundreds of millions of years have gone by. Pflüger also notes that Azmi's fossils come from a part of the basin different from the one that contained the tracks, increasing the chances that fracturing and jumbling of rock layers could confuse interpretations.

And Indian researchers, including paleontologists Anshu Sinha of the Birbal Sahni Institute of Paleobotany in Lucknow and B. S. Venkatachala of the Wadia Institute, say that they are reluctant to adopt a young age for Vindhyan rocks, given the radiometric dates. They also report signs of pre-Cambrian single-celled algae and other fossils in the rocks. To prove the age of the Vindhyan, geologists may have to find and date rocks such as volcanic ash layers, which offer secure dates because they are deposited as soon as they're formed. Until then, the age of the first animals remains in question.

—RICHARD A. KERR

With reporting from India by Pallava Bagla.

In the everyday world, time is a one-way street. Unlike characters in Martin Amis's novel *Time's Arrow*, we never exit a taxi and salute while it retreats down the street or awake in the evening and see our clothes come flying from the corners of the room. The microscopic level where particles collide and decay, however, has seemed indifferent to the direction of time. But two groups of researchers, at Fermi National Accelerator Laboratory (Fermilab) in Illinois and CERN in Switzerland, have now directly detected the forward march of time in the decays of subatomic particles.

Physicists once thought that the equations of the subatomic world would look the



Only in the movies. New findings would leave H. G. Wells's time machine (here, in a 1960 version) with nowhere to go.

same if time were reversed. A movie of an atom decaying into bits, when run in reverse, would show a process that—although unlikely—still obeys the laws of physics: the bits converging to form a full atom. But they also knew that this time-reversal symmetry was part of a larger, more powerful package known as CPT (for charge, parity, and time reversal) symmetry, which sits at the heart of modern physics: Swap antimatter for matter, view the universe (essentially) in a mirror, and reverse the direction of time, and all the experiments should come out the same way they do in the real world. The CPT theorem (which has now been tested to an impressive 18 decimal places) meant that time-reversal symmetry could hold only if charge-parity (CP) symmetry holds as well.

In 1964, physicists found that it doesn't. They noted that neutral particles called kaons occasionally decayed in a way that blatantly violated CP symmetry. The CPT theorem could be saved only if making

time flow backward changed things in a way that canceled out the CP asymmetry. No one could gather enough data to isolate the rare decays that would show this directly, however.

Now two groups have finally managed this feat, by measuring the rate of a particular decay and showing that it differs from the rate of the same process done in reverse. "I think it's truly spectacular work," says Alan Kostelecky of Indiana University, Bloomington. "This is the most important experimental advance since" 1964 for testing time symmetry.

One of the groups, the CPLEAR collaboration at CERN, collided antiprotons and hydrogen atoms to make kaons and their antimatter counterparts, antikaons. As they travel, antikaons can transform into kaons and vice versa. In results to appear in an upcoming issue of *Physics Letters B*, the team used

a large tracking chamber to count the kaons and antikaons as they decayed—each to an electron, a pion, and a neutrino. The charge of the electron revealed which type of kaon had decayed. The team found that the rate for antikaons transforming into kaons was a fraction of a percent higher than for what would be the time-reversed process—kaons becoming antikaons. "This shows that you can't turn the clock

backward" and always get the same results, says CPLEAR spokesperson Panagiotis Pavlopoulos.

The other group, the KTeV collaboration at Fermilab, also studied kaons, but watched for much rarer events—the 1-in-10-million decay of a single kaon into pairs of electrons and pions. The team, which presented its results at a Fermilab workshop earlier this month, mapped out the directions of the electrons and pions. Here, time asymmetry revealed itself in a subtler way. Because reversing time also reverses a particle's momentum, the team looked for time asymmetries by comparing the rates of some decays to others where the direction of the emerging particles looked as they would if time had been reversed. The rates differed by about 13%. "It's a huge effect," says Fermilab physicist and KTeV collaborator Vivian O'Dell.

Both experiments observe time asymmetry at about the level that would compensate for the CP asymmetry first observed over 3 decades ago. "I don't think anyone is sur-

3. CP Violation & Arrows of Time

(i) Conundrum :

Excluding CP-viol. interactions, Hamiltonian of universe (grav, em, strong, weak) is time-symmetric

$$T H T^{-1} = H$$

∴ All physical phenomena (other than CP viol) should be symmetric with respect to forward and backward directions in time.

Future and Past should be symmetric

This contradicts everyday experience:

Time seems to flow from past to future.

Unstable systems decay, don't rejuvenate.

Time has a direction (arrow)

⇒ **River of time**

(ii) Standard Explanations :

Entropy ? Cosmic Expansion ?

No one knows for sure !

(iii) Present investigation: Role of CP violation in Evolution of Elementary systems (K, B...)

- Consider observables that are monotonic (unidirectional) in time, when CP is conserved.
- Investigate in what way this unidirectionality is affected when CP viol. is switched on.
- We give examples where a system makes a transition from monotonic to non-monotonic behaviour when the strength of CP violation exceeds a critical value.

Reference:

Ch. Berger & L.M. Sehgal

Phys. Rev. D76, 036003 (2007)

Phys. Rev. D83, 037901 (2011)

Density Matrix of K^0, \bar{K}^0

$$\rho(t) = \frac{1}{2} N(t) \left[\mathbb{1} + \vec{S}(t) \cdot \vec{\sigma} \right]$$

$$N(t) = \text{Tr} \rho(t)$$

$$S_i(t) = \text{Tr} \rho(t) \sigma_i / \text{Tr} \rho(t) \quad i=1,2,3$$

Initial State : 1:1 incoh. mixture

$$N(0) = 1, \quad \vec{S}(0) = 0$$

$$\rho(0) = \frac{1}{2} \begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix}$$

Evolution :

$$K^0 \xrightarrow{t} \psi(t) = \frac{1}{2p} \left[K_S e^{-\lambda_S t} + K_L e^{-\lambda_L t} \right]$$

$$\bar{K}^0 \xrightarrow{t} \bar{\psi}(t) = \frac{1}{2q} \left[K_S e^{-\lambda_S t} - K_L e^{-\lambda_L t} \right]$$

where $K_{L,S} = p K^0 \mp q \bar{K}^0$

$$|p|^2 + |q|^2 = 1$$

Eigenvalues $\lambda_{L,S} = \frac{1}{2} \gamma_{L,S} + i m_{L,S}$

$\rightarrow \delta \equiv \langle K_L | K_S \rangle = \frac{|p|^2 - |q|^2}{|p|^2 + |q|^2} = 3.27 \times 10^{-3}$
~~etc~~

Same formalism applies to $B^0 - \bar{B}^0$

Solution

$$N(t) = \frac{1}{2(1-\delta^2)} \left[e^{-\gamma_s t} + e^{-\gamma_L t} - 2\delta^2 \cos \Delta mt \cdot e^{-(\gamma_L + \gamma_s)t/2} \right]$$

$$|\vec{\xi}(t)| = \left[1 - \frac{1}{N(t)^2} e^{-(\gamma_s + \gamma_L)t} \right]^{1/2}$$

$$\begin{aligned} \text{N.B. } \det \rho &= \frac{1}{4} N^2 (1 - |\vec{\xi}|^2) \\ &= \frac{1}{4} e^{-(\gamma_L + \gamma_s)t} \end{aligned}$$

(Monotonic, since $\gamma_{L,S} > 0$:
macroscopic arrow of time)

Eigenvalues of ρ are

$$\lambda_{1,2} = \frac{N}{2} (1 \pm \xi), \quad \xi \equiv |\vec{\xi}|$$

Question : Are $N(t)$, $\xi(t)$ monotonic functions of t ? Is there a phase transition as CP-violating parameter δ is varied ?

Note: as $t \rightarrow \infty$, $N(t) \rightarrow 0$ (state decays)
 $\xi(t) \rightarrow 1$ (state becomes pure K_L)

Phase transition in $N(t)$?

Monotonic for

$$\delta^2 \leq \left[\frac{\gamma_S \gamma_L}{(\gamma_S + \gamma_L)^2/4 + \Delta m^2} \right]^{1/2}$$

$$= \left[\frac{\lambda}{(1+\lambda)^2/4 + \mu^2} \right]^{1/2}, \quad \lambda = \gamma_L/\gamma_S$$
$$\mu = \Delta m/\gamma_S$$

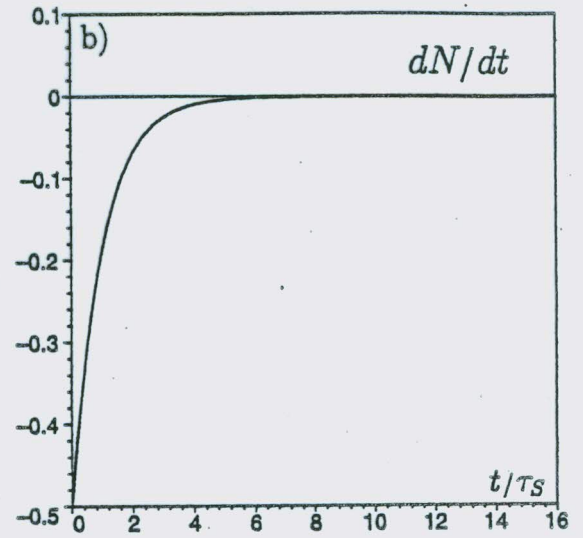
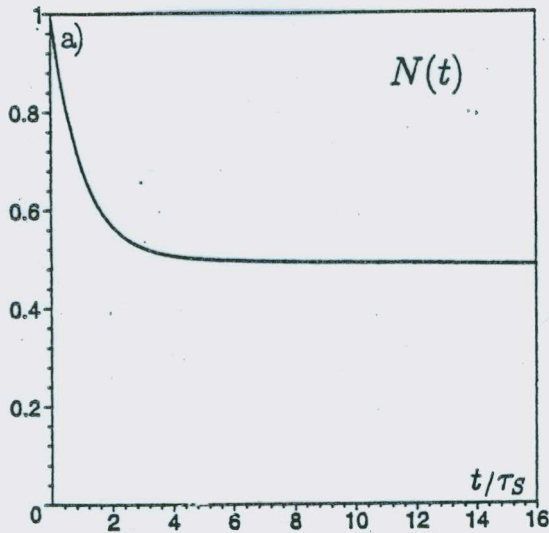
Stronger bound if one requires monotonic behaviour for norm of a pure state $|\psi\rangle = \alpha |K_L\rangle + \beta |K_S\rangle$

$$\delta_{\text{unit}}^2 \leq \frac{\lambda}{(1+\lambda)^2/4 + \mu^2}$$

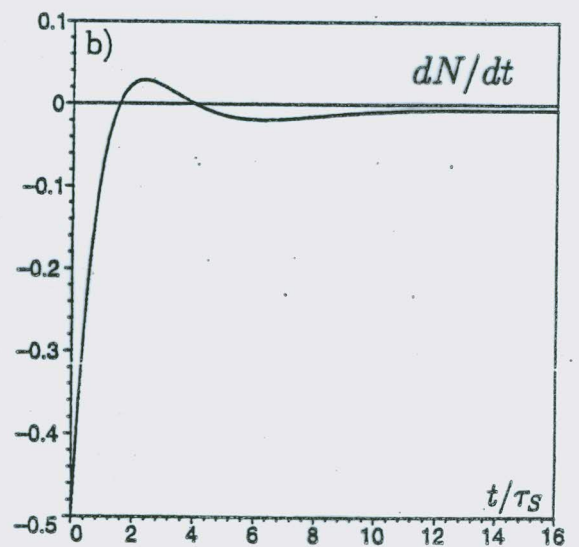
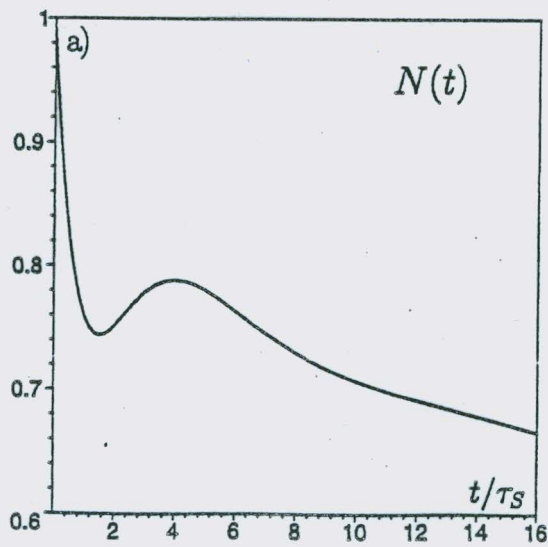
Called unitarity bound (derived by Lee & Wolfenstein, Bell & Steinberger)
Transition from monotonic to non-monotonic behaviour if δ exceeds this bound.

Empirical values for $K^0 - \bar{K}^0$, $B^0 - \bar{B}^0$, $B_s^0 - \bar{B}_s^0$ satisfy this bound.

$\delta \ll \delta_{crit}$



$\delta \gg \delta_{crit}$



Phase transition in $\zeta(t)$?

Require $d\zeta(t)/dt > 0$

$$\Rightarrow \delta^2 < \frac{1}{2} \left(\frac{1-\alpha}{\mu} \right) \sinh \left(\frac{3\pi}{4} \frac{1-\alpha}{\mu} \right)$$

Quite stringent for $B^0 - \bar{B}^0$, since $\alpha = \gamma_L/\gamma_S$ close to one!

In view of $\Delta\delta/\Delta m \ll 1$, approximate result is

$$\delta < \sqrt{\frac{3\pi}{8}} \left| \frac{\Delta\delta}{\Delta m} \right|$$

For $B_d - \bar{B}_d$ system, this gives

$$\delta < 0.0155$$

Empirical value is $\delta_{\text{exp}} = 0.005 \pm 0.005$, just below bound

For $B_s - \bar{B}_s$ system, monotonicity of Stokes parameter $\zeta(t)$ requires

$$\delta < 0.0038$$

Present data from D^0 -experiment violate this bound by factor 2!

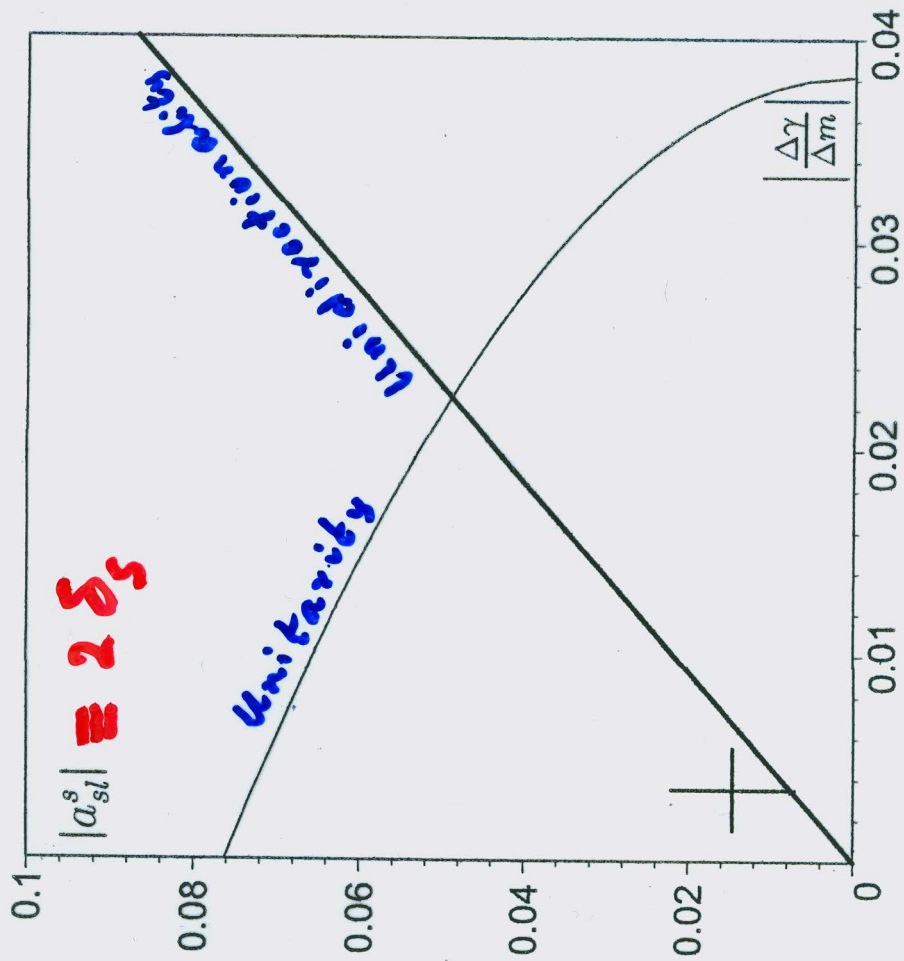
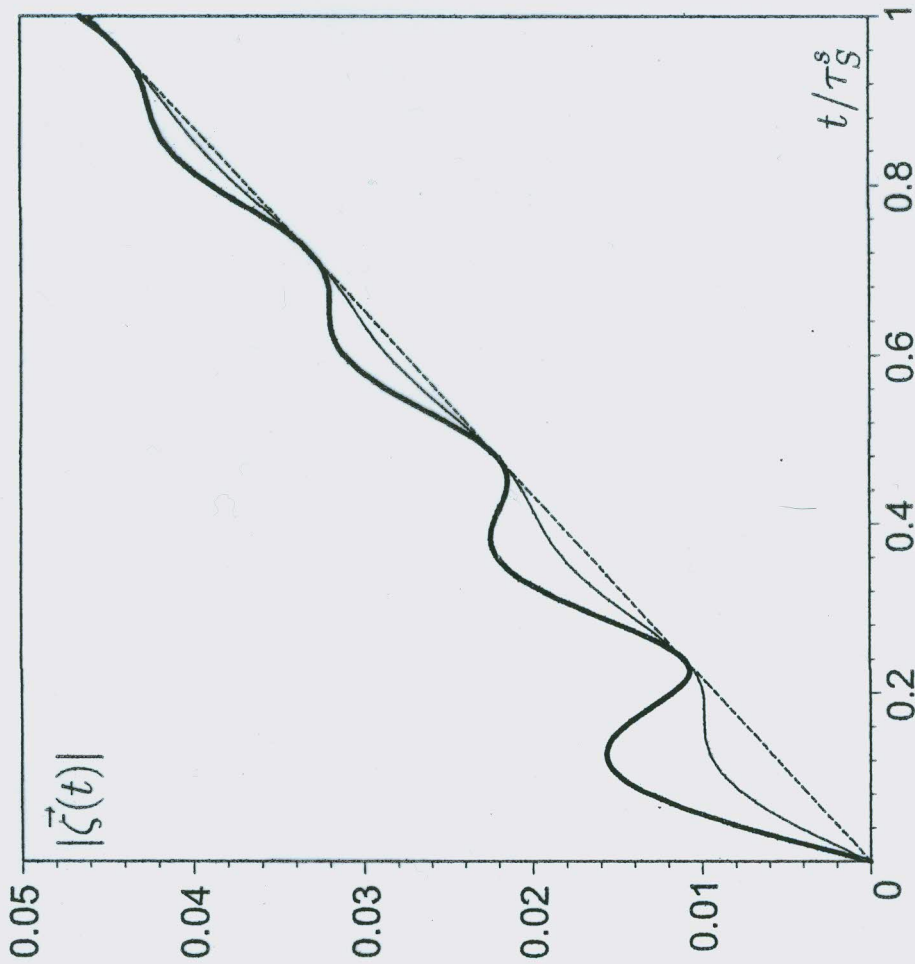


Figure 1: Constraints on $|a_{sl}^s|$ in the $|a_{sl}^s| - |\Delta\gamma/\Delta m|$ plane resulting from unitarity and monotonicity of $|\zeta(t)|$ for the $B_s^0 - \bar{B}_s^0$ system. The thin line represents the unitarity bound (7) with $\Delta m/\gamma_S = 26.2$ and the thick line our new bound evaluated from (8). The cross represents the experimental result of the D0 experiment for $|a_{sl}^s|$ with the horizontal error bar indicating the uncertainty of $|\Delta\gamma/\Delta m|$

bound following from (8). In this case the LV result – if true – implies the existence of a new type of quantum mechanical oscillation.



Phase
Transition
in
 $|\vec{\zeta}(t)|$

Figure 2: Plot of $|\vec{\zeta}(t)|$ versus t in units of the lifetime τ_S^s . The thick line is calculated for the nominal D0 value of $\delta = 0.0073$. The strictly monotonic dashed line is obtained for the standard model value of δ . The thin line represents the behaviour of $|\vec{\zeta}(t)|$ at the critical value $\delta_{\text{crit}} = 0.0038113$ i.e. the transition between monotonic and nonmonotonic regimes.

Alternative to Stokes Parameter $S(t)$:

Define "Entropy" (similar to von Neumann Entropy):

$$\text{"Entropy"} = -p_1 \log p_1 - p_2 \log p_2$$

$$p_{1,2} \equiv \frac{\lambda_{1,2}}{\lambda_1 + \lambda_2}$$

$\lambda_{1,2}$ = eigenvalues of density matrix $\rho(t)$:

$$\lambda_{1,2} = \frac{N(t)}{2} (1 \pm S(t))$$

Maximal mixing ($p_1 = p_2 = 1/2$)

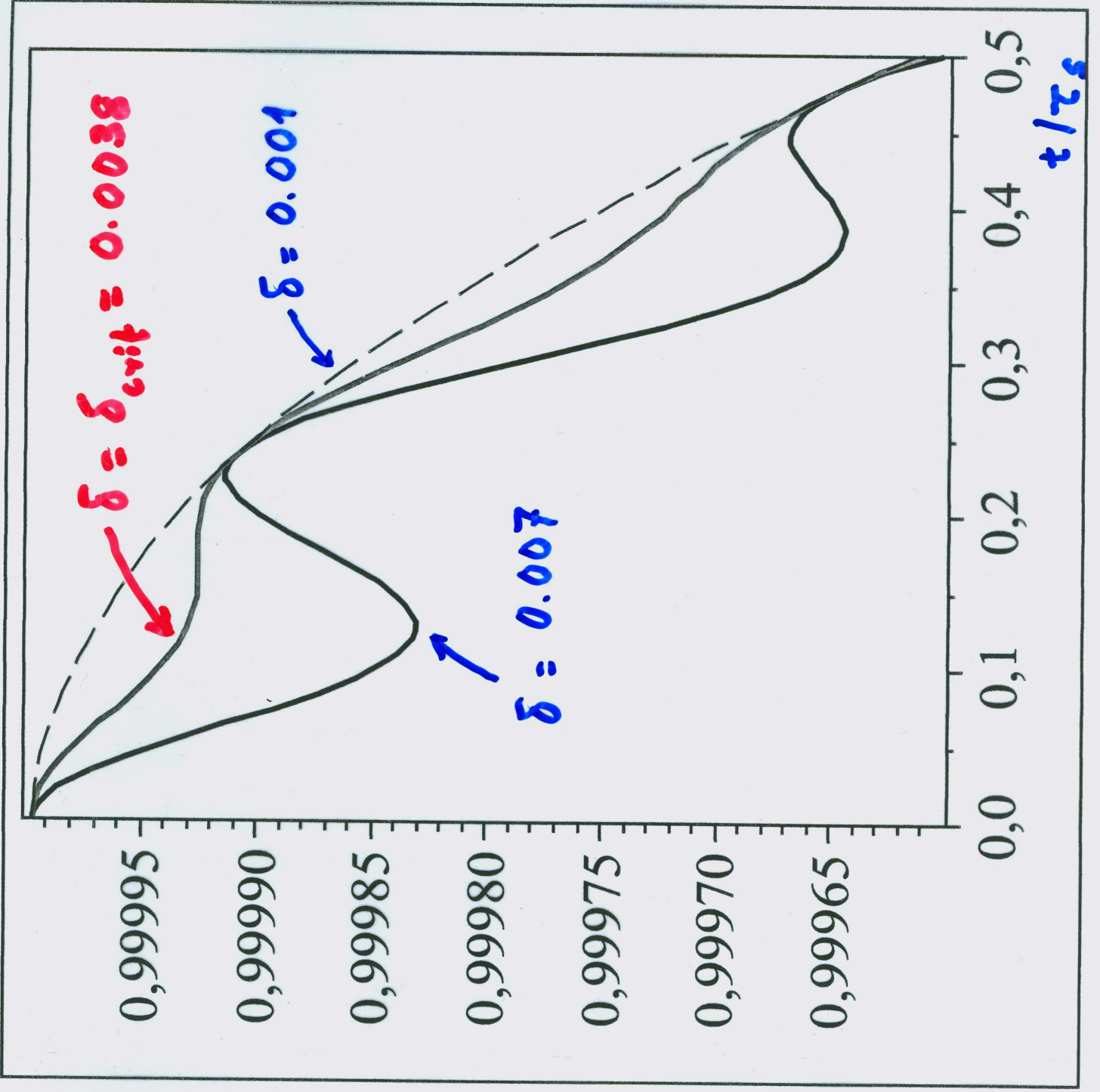
$$\Rightarrow \text{"Entropy"} = 1$$

Minimal mixing (pure state)

$$\Rightarrow \text{"Entropy"} = 0$$

"Entropy" of $B_s - \bar{B}_s$ decreases from one to zero.

Phase
Transition
in
"Entropy"



Implication for $B_s - \bar{B}_s$ System:

- Violation of Monotonicity of $\mathcal{I}(t)$?
 - Evolution of Coherence in a $B_s - \bar{B}_s$ mixture not unidirectional ?
 - Does the river of time have eddies ?
 - Is the macroscopic arrow of time dented in microscopic processes, as a consequence of CP violation ?
 - Is the $B_s - \bar{B}_s$ system special ?
- Is the CP violating parameter δ an order parameter ?

Contemplating Strange Beauty

$$B_S^0 = s\bar{b}, \quad \bar{B}_S^0 = \bar{s}b$$

$$\text{Mass} = 5366 \pm 0.6 \text{ MeV}$$

$$\text{Mean life } \tau = 1.47 \text{ ps}$$

$$\text{Two lifetimes: } \frac{\Delta\Gamma}{\Gamma} \sim 10\%$$

$$\Delta m = 17.77 \pm 0.12 \text{ ps}^{-1}$$

Oscillates between B_S^0 and \bar{B}_S^0
26 times before disappearing
in a cloud of quarks and leptons!

"There is no excellent beauty
that hath not some strangeness
in the proportion."

Francis Bacon

1561-1626